Mathematical

ELEMENTS

Natural Philosophy,

Confirmed by EXPERIMENTS;

OR, AN

INTRODUCTION

Sir Isaac NEW TON's Philosophy.

VOL. I.

By WILLIAM-JAMES 'SGRAVESANDES Doctor of Laws and Philosophy, Professor of Mathematicks and Astronomy at Leyden, and Fellow of the Royal Society of London.

Translated into ENGLISH,

Py J. T. Defaguliers, I.L. D. Fellow of the Royal Society, and Chaplain to his Grace the Duke of CHANDOS.

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TO

Sir Isaac Newton, Knt.

PRESIDENT

OF THE

ROYAL SOCIETY, &c.

SIR,

N dedicating this Translation to You, I do no more than what my learned Friend, the ingenious Author, would have done, if Custom and Gratitude had not obliged him

to offer the first Philosophical Work he has publish'd, since his being Profesior, to the Governors of the University that gave him the Chair. And as there are more Admirers of your wonderful Discoveries, than there are Mathematicians able to understand the two first Books of your Principia: So I hope You will not be displeased, that both my Author and myself have, by Experiments, endeavoured to explain some of those Propositions, which were implicitely believed by many of your Readers; at the same Time that the greatest Part of your third Book, and feveral of the Corollaries and Scholia in the other two, gave them the highest Satisfaction that an inquisitive Mind is capable of receiving. Mathematicians of the first Rank, who want no such Helps in reading your incomparable Works, take a fresh Pleasure in feeing those Experiments performed which you have made yourfelf: And

And though some of ours may not always prove, but sometimes only illustrate a Proposition; yet, such Mathematicians, as are of a communicative Temper, will be glad to use them, as a new Set of Words, to give Beginners so clear a Notion of the System of the World, as to encourage them to the Study of the higher Geometry; whereby they may know how to value your Solutions of the most difficult Phenomena, and learn from You, that a whole Science may be contain'd in a single Proposition.

For my own Part, fince I cannot enough acknowledge the Advantages which I have had by being admitted to your Conversation, and your generous Way of gratifying me for such Experiments as I have made by your Direction; therefore I shall here forbear to pay that Tribute which is due to You

You from all Lovers of Knowledge; and rather chuse to be thought singular, than, by praising, to offend You. I am,

SIR,

Your most Obedient,

AND

Very Humble Servant,

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THE

TRANSLATOR

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READER.

Thing in praise of it, either on Account of the useful Subject that it treats of, or the excellent Method and familiar Way in which our Author has handled it: only I thought proper to observe to the Reader, that the Numbers in the Margin express so many Propositions, which are referred to, as you go forward in the Book, to avoid Repetitions and Tautology. If what is printed in Italic Characters be read by itself, it will appear to be a Compendium of the whole Book; or the Doctrinal Part of it without the

the Experiments and Demonstrations. I have endeavour'd to an-Swer this End in my English Transtation, where you will find, that whatever is in Italic Characters, makes up the Sense of the rest of the Book; which also readily makes Sense by itself, though taken from Places where it seems irregularly

dispers'd.

The first Edition of this Translation had some Errors of the Press, and Faults in the Plates, which were occasioned by the Haste in which it was printed off, to prevent the Injury that must have been done to Dr.'s Gravefande, by a Translation that some Booksellers endeavour'd to get out before mine, which was so ill done, that no Body that had read the Latin Book would be able to know it again in their English.

I have, therefore, in this Second Edition, carefully review'd and corrected every Error, both in the Book and Plates. THE



THE

PREFACE.



Fwe compare the Writings of different Philosophers concerning Physics, we may easily see that they call different Sciences by the same Name, tho' they all profess to ex-

plain the true Cause of Natural * Phænomena. And no Wonder if they disagree among themselves, since even Mathematicians, who deal in Certainties, can hardly be kept from wrangling.

But that Diversity of Opinions should not deter us from searching after Truth; since Labour and Study will find it out; and the more we are in love with it, the less we are liable to Errors, excepting such as human Frailty renders unavoidable.

We must proceed cautiously in Physics, since that Science considers the Works of the Supreme Wisdom, and sets forth, * What Laws JEHOVAH to himself prefcrib'd,

And of his Work the firm Foundation made, When He of Things the first Design survey'd.

How the whole Universe is govern'd by those Laws, and how the same Laws run thro' all the Works of Nature, and are constantly observed with

a wonderful Regularity.

We must take care not to admit Fistion for Truth; for by that means we shut out all further Examination. No true Explanation of Phænomena can spring out of a false Principle: And what a wast Difference there is betwixt learning the Fistions of whimsical Men, and examining the Works of the most wise God! Since an Enquiry into Divine Wisdom, and the Veneration inseparable from it, is to be the Scope of a Philosopher, we need not enlarge upon the Vanity of reasoning upon fistitious Hypotheses.

Nature herself is therefore attentively and incessantly to be examined with indefatigable Pains. That Way indeed our Progress will be but slow, but then our Discoveries will be certain; and oftentimes we shall even be able to determine the Limits

of Human Understanding.

What has led most People into Errors is an immoderate Desire of Knowledge, and the Shame of confessing our Ignorance. But Reason should get the better of that ill grounded Shame; since there is a learned Ignorance that is the Fruit of Knowledge, and which is much preferable to an ignorant Learning.

Natural Philosophy is placed among those Parts of Mathematics, whose Object is Quantity ingeneral.

Mathe-

Pangeret, omniparens leges violare Creator Noluit, æternique operis sundamina fixit.

Mathematics are divided into Pure and Mixed. Pure Mathematics enquire into the General Properties of Figures and abstracted Ideas. Mixed Mathematics examine Things themselves, and will have our Notions and Deductions to agree both with Reason and Experience.

Physics belong to Mixed Mathematics. The Properties of Bodies, and the Laws of Nature, are the Foundations of Mathematical Reasoning, as all that have examined the Scope of this Science will freely confess. But Philosophers do not equally agree upon what is to pass for a Law of Nature, and what Method is to be followed in Quest of those Laws. I have therefore thought fit in this Preface to make good the Newtonian Method, which I have followed in this Work. What that Method is, I have briefly set desire in the first Chapter.

Position suberein Reason so perfectly agrees swith

Position wherein Reason so perfectly agrees with Scripture, that the least Examination of Nature will shew plain Footsteps of Supreme Wildom. It is confounding and oversetting all our clearest Notions, to affert that the World may have taken its Rife from some general Laws of Motion, and that it imports not what is imagined concerning the first Division of Matter. And that there can hardly be any Thing supposed, from which the same Effect may not be deduced by the fame Laws of Nature; and that for this Reason: That since Matter successively assumes all the Forms it is capable of by means of those Laws, if we consider all those Forms in Order, we must at last come to that Form wherein this present World is framed; so that we have no Reason in this Case to fear any Error from a wrong Supposition. This Affertion, I say, overthrows all our clearest Notions, as has been fully proved by many Learned Men; and is indeed so

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unreasonable, and so injurious to the Deity, that it will seem unworthy of an Answer to any one that does not know that it has been maintained by many ancient and modern Philosophers, and some of them of the first Rank, and far removed from any Suspicion of Atheism.

Then first laying it down as an undoubted Truth, that God bas created all Things, we must afterwards explain by what Laws every Thing is governed; and to mention only the Moon, we must

explain, why

* The Silver Moon runs with unequal Pace, Which yet Astronomers could never trace, Or fix in Numbers her uncertain Place:
What Force her Apsides has forward driven, And made her Nodes recede i'th' Starry Heaven. What is her Pow'r to agitate the Sea, Whose various Tides her Presence still obey; When th'Ocean swells, its topmost Bank to lave, Or ebbs from weedy Shores with broken V. ave, Leaving the Sands, the Sailor's Terror, bare:

In Order to explain more fully which Way we trace out the Laws of Nature, we must begin by some previous and preparatory Reslexions.

What Substances are, is one of the Things hidden from us. We know, for Instance, some of the

Pro-

Passibus haud æquis graditur; eur subdita nulli
Hactenus Astronomo numerorum fræna recuset.
Cur remeant Nodi, curq; Auges progrediuntur.
— quantis resisum vaga Cynthia pontum
Viribus impellit, dum fractis sluctibus ulvam
Deserit, ac nautis suspectas nudat arenas;
Alternis vicibus suprema ad littora pulsans.

Properties of Matter; but we are absolutely igno-

rant, what Subject they are inherent in.

Who dares affirm that there are not in Body many other Properties, which we have no Notions of? And who ever could certainly know, that, besides the Properties of Body which flow from the Essence of Matter, there are not others depending upon the free Power of Gop, and that extended and solid Substance (for thus we define Body) is endowed with some Properties without which it could exist? We are not, I own, to affirm or deny any Thing concerning what we do not know. But this Rule is not followed by those, who reason in Physical Matters, as if they had a compleat Knowledge of whatever belongs to Body, and who do not scruple to affirm, that the few Properties of Body, which they are acquainted with, constitute the very Essence of Body.

What do they mean by faying, that the Properties of Subffance constitute the very Substance?

Can those Things subsist when join'd together, that cannot subsist separately? Can Extension, Impenetrability, Motion, &c. be conceived without a Subject to which they belong? And have we any

Notion of that Subject.

We must give up as uncertain what we find to be so, and not be ashamed to confess our Ignorance. Tho we need not fear being too bold in affirming, that a Subject altogether unknown to us may perhaps be endowed with some unknown Properties. And those Men who at the same Time that they say, conformably to this Axiom, That we must not reason about Things unknown, lay it down as a Foundation of their Reasonings, that nothing relating to Body is unknown to us, are beholden to meer Chance, if they are not mistaken.

The Properties of Body cannot be known a priori; We must therefore examine Body itself, and nicely

consider all its Properties; that we may be able to determine what natural Effects do slow from

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those Properties.

Upon a farther Examination of Body, we find there are some general Laws, according to which Bodies are moved. It is past doubt, for Instance, That a Body once mov'd continues in Motion: that Reaction is always equal and contrary to Action, And several other such Laws concerning Body bave been discovered; which can no Way be deduced from those Properties that are said to constitute Body; and since those Laws always bold good, and upon all Occasions, they are to be looked upon as general Laws of Nature. But then we are at a Loss to know, whether they flow from the Essence of Matter, or whether they are deducible from Properties, given by Gon to the Bodies, the World confifts of; but no Way essential to Body; or whatever finally those Effects, which pass for Laws of Nature, depend upon external Caufes, which even our Ideas cannot attain to.

Who dares affirm any Thing upon this Point concerning all, or any Laws of Nature, without incurring the Guilt of Rashness? Besides, whoever examines the Phænomena of Nature will be fully persuaded, that many of its Laws are not yet discover'd, and that many Particulars are wanting to-

wards the compleat Knowledge of others.

The Study of Natural Philosophy is not however to be contemned, as built upon an unknown Foundation. The Sphere of humane Knowledge is bounded within a narrow Compass; and he, that denies his Assent to every Thing but Evidence, wavers in Doubt every Minute; and looks upon many Things as unknown which the Generality of People never so much as call in Question. But rightly to distinguish Things known, from Things unknown, is a Perfection above the Level of buman Mind. Though many Things

Things in Nature are hidden from us; yet what is set down in Physics, as a Science, is undoubted. From a few general Principles numberless particular Phænomena or Effects are explained, and deduced by Mathematical Demonstration. For, the comparing of Motion, or in other Words, of Quantities, is the continual Theme; and whoever will go about that Work any other Way, than by Mathematical Demonstrations, will be sure to fall into Uncertainties at least, if not into Errors.

How much soever then may be unknown in Natural Philosophy, it still remains a vast, certain and very useful Science. It corrects an infinite Number of Prejudices concerning natural Things, and divine Wisdom; and, as we examine the Works of God continually, sets that Wisdom before our Eyes; and there is a wide Difference, betwint knowing the divine Power and Wisdom by a Metaphysical Argument, and beholding them with our Eyes every Minute in their Effects. It appears then sufficiently, what is the End of Physics, from what Laws of Nature the Phanomena are to be deduced, and wherefore, when we are once come to the general Laws, we cannot penetrate any further into the Knowledge of Causes. There remains only to discourse of the Method of searching after those Laws; and to prove that the three Newtonian Laws delivered in the first Chapter of this Work ought to be followed.

The first is, That we ought not to admit any more Causes of Natural Things, than what are true, and sufficient to explain their Phænomena. The first Part of this Rule plainly follows from what has been said above. The other cannot be called in Question by any that owns the Wisdom of the Creator. If one Cause suffices, it is needless to superadd another; especially, if it be considered, that an Effect from a double Cause is never exact-

ly the same with an Effect from a single one. Therefore we are not to multiply Causes, till it appears one single Cause will not do the Business.

In order to prove the following Rules, we must

premise some general Reflections.

We have already said, that Mathematical Demonstrations have no Standard to be judged by, but their Conformity with our Ideas; and when the Question is about Natural Things, the first Requisite is, that our Ideas agree with those Things, which cannot be proved by any Mathematical Demonstration. And yet as we have Occasion to reason of Things themselves every Moment, and of those Things nothing can be present to our Minds besides our Ideas, upon which our Reasonings immediately turn; it follows, that God has established some Rules, by which we may judge of the Agreement of our Ideas with the Things themselves.

All Mathematical Reasonings turn upon the Comparison of Quantities, and their Truth is evidenc'd by implying a Contradiction in a contrary Proposition. A rectilineal Triangle, for Instance, whose three Angles are not equal to two right ones, is a Thing impossible. When the Question is not about the Comparison of Quantities, a contrary Proposition is not always impossible. It is certain, for Instance, that Peter is living, though it is as certain that he might have died Testerday. Now there being numberless Cases of that Kind, where one may affirm or deny with equal Certainty; there follows, that there are many Reasonings very certain, tho altogether different from the Mathematical Ones. And they evidently follow from the Establishment of Things, and therefore from the pre-determined Will of GOD. For by forcing Men upon the Necessity of pronouncing concerning the Truth or Falfhood of a Proposition; he plainly shews they must affent to Agreements, which their Judgments weceffarily

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To return to Physics; we are in this Science to judge by our Senses, of the Agreement that there is betwixt Things and our Ideas. The Extension and Solidity of Matter, for Instance, asserted upon that Ground, are past all Doubt. Here we examine the Thing in general, without taking notice of the Fallacy of our Senses upon some Occasions, and which Way Error is then to be avoided.

We cannot immediately judge of all Physical Matters by our Senses. We have then Recourse to another just Way of reasoning, though not Mathematical. It depends upon this Axiom; (viz.) We must look upon as true, whatever being denied would destroy civil Society, and deprive us of the Means of Living. From which Proposition the second and third Rules of the Newtonian Method most evidently follow.

For who could live a Minute's Time in Tranquillity, if a Man was to doubt the Truth of what passes for certain, wherever Experiments have been made about it; and if he did not depend upon seeing the like Effects produced by the same Cause?

The following Reasonings, for Example, are daily taken for granted as undoubtedly true, without any previous Examination; because every Body sees that they cannot be called in Question without

destroying the present OEconomy of Nature.

A Building, this Day firm in all its Parts, will not of its self run to Ruin to Morrow. Thus, by a Parity of Reason, the Cohesion and Gravity of the Parts of Bodies, which I never saw altered, nor heard of having been altered, without some intervening external Cause, will not be altered to Night, because the Cause of Cohesion and Gravity will be the same to Morrow as it is to Day. Who does not see, that the Certainty of this Reasoning depends

pends only upon the Truth of the fore-mentioned

Principle?

The Timber and Stones of any Country, which are fit for a Building, if brought over here, will ferve in this Place, except what Changes may arise from an external Cause; and I shall no more fear the Fall of my Building, than the Inhabitants of the Country, from whence those Materials were brought, wou'd do, if they had built a House with them. Thus the Power which causes the Cohesion of Parts, and that which gives Weight to Bodies, are the same in all Countries.

I have used such Kind of Food for so many Years, therefore I will use it again to Day with-

out Fear.

When I fee Hemlock, I conclude it to be poifonous, tho' I never made an Experiment of that very Hemlock I fee before my Eyes.

All these Reasonings are grounded upon Analogy; and there is no Doubt, but our Creator has in many Cases left us no other Way of Reasoning, and there-

fore it is a right Way.

Which being once prov'd, we may afterwards make use of the same Method in other Matters, where no absolute Necessity forces us to reason at all. When an Argument is good in one Case, there is no Reason why we should refuse our Assent to it in another. For who can conceive, that Things proved the same Way are not equally certain? Besides, tho' we conclude in general, that this Method of Reasoning is right from the Necessity of using it; yet it does not follow that particular Reasonings depend upon that Necessity. I conclude from Analogy, that Food is not poisonous; but is that Argument only good, when I ambungry?

In Physics then we are to discover the Laws of Nature by the Phænomena, then by Induction prove them to be general Laws; all the rest is to be hanfide fide now this

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dled Mathematically. Whoever will seriously examine, what Foundation this Method of Physics is built upon, will easily discover this to be the only true one, and that all Hypotheses are to be laid asside.

So much for the Method of philosophising. I have now a Word to say of the Work itself, of which

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The whole Work is divided into four Books. The first treats of Body in general, and the Motion of Solid Bodies. The Second of Fluids. What belongs to Light is handled in the Third. The Fourth explains the Motions of Celestial Bodies, and what has a Relation to them upon Earth. The two first Books are contained in this Tome.

In Order to render the Study of Natural Philofophy as easy and agreeable as possible, I have thought sit to illustrate every Thing by Experiments, and to set the very Mathematical Conclusions be-

fore the Reader's Eyes by this Method.

He, that sets forth the Elements of a Science, does not promise the learned World any Thing new in the main. Therefore I thought it needless, to point outwhere what is here contained is to be found. I have made my Property of whatever served my Purpose; and I thought giving Notice of it, once for all, was sufficient to avoid the Suspicion of Thest. I had rather lose the Honour of a few Discoveries, dispersed here and there in this Treatise, than rob any one of theirs. Let who will then take to himself what he thinks his own: I lay claim to nothing.

As to Machines which serve for making the Experiments, I have taken care to imitate several from other Authors, have altered and improved others, and added many new ones of my own Invention. And no Wonder I should be forced to that Necessity, having made Experiments upon many

Things

Things never tried perhaps by any one before. For Mathematicians think Experiments superfluous, where Mathematical Demonstrations will take Place: But as all Mathematical Demonstrations are abstracted, I do not question their becoming easier, when Experiments set forth the Conclusions before our Eyes; following therein the Example of the English, whose Way of teaching Natural Philosophy gave me Occasion to think of the Method I have followed in this Work. Ishall always glory in treading in their Footsteps, who, with the Prince of Philosophers for their Guide, have first opened the Way to the Discovery of Truth in Philosophical Matters.

As to the Machines, I will say thus much more by Way of Advertisement, That most of them have been made by a very ingenious Artist of this Town, and no unskilful Philosopher, whose Name is John van Musschenbroek, and who has a perfect Knowledge of every Thing that is here explained. Which Advertisement, I suppose, will not be displeasing to those who may have a Fancy to get some of those Machines made for themselves.



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ELEMENTS

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Natural Philosophy,

CONFIRMED BY

EXPERIMENTS.

BOOK I.

PART I. Of BODT in General:

CHAP. I.

Of the Scope of Natural Philosophy, and the Rules of Philosophizing.

Things, and their Phanomena.

DEFINITION I, and II.

Natural Things are all Bodies: And the Assem- the blage or System of them all is called the Universe.

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DEFINITION III.

Natural Phænomena are all Situations and all Motions of Natural Bodies, not immediately depending upon the Action of an intelligent Being;

and which may be observed by our Senses.

We do not exclude, out of the Number of Natural Phænomena, those which happen in our Bodies by our Will; for they are produced by the Motion of our Muscles, and their Action depends upon another Motion: In these, there is only that Motion which arises from the immediate Action of the Mind, and is intirely unknown to us, which is not a Natural Phænomenon.

All these Motions are performed by certain Rules, and always subject to the same Laws.

The Sun rifes and fets daily; and the Time of his Rifing and Setting may always be determined, according to the Time of the Year, and Latitude of the Place. Plants of the same Kind, under the fame Circumstances, are always produced and grow in the fame Manner: And fo on in other Cases. Nay, even in those things which appear to be wholly fortuitous and uncertain, certain Rules are without doubt observed.

Natural Philosophy explains Natural Phanomena; that is, gives an Account of their Causes.

In enquiring after those Causes. BODY in general is to be examined; and then the Rules which the Creator has established, according to which, Motions are to be perform'd. These Rules , are called Laws of Nature.

DEFINITION IV.

A Law of Nature then is, the Rule and Law, according to which God resolved that certain Motions should always, that is, in all Cases, be performed.

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Every Law does immediately depend upon the Will of God.

Also in respect to us, we call a Law of Nature, every Effect which in all Occasions is produced after the same Manner; although its Cause is unknown to us, and we do not see that it flows from any Law known to us.

For we make no Difference between a thing which immediately depends upon the Will of God, and what it produces by the Intermediation of a Cause of which we have no Idea.

The Laws of Nature are only deduced from an Examination of Natural Phænomena.

By Help of the Laws, thus discovered, other Phænomena must be explained.

In order to find out the Laws of Nature, Sir Isaac Newton's following Rules are to be obferved.

RULE I.

We are not to admit more Causes of Natural Things than such as are true, and sufficient for explaining their Phænomena.

RULE II.

Natural Effects of the same Kind have the same 6 Causes.

Such Qualities of Bodies, whose Virtue cannot be increased and diminished, and which belong to all Bodies upon which Experiments may be made, must be looked upon as Qualities of all Bodies.

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CHAP.

CHAP. II.

Of BODY in General.

8 WHAT we first consider in Body is Ex-

tension.

What is meant by Extension, no Body is ignorant of. Its Idea is most simple, and almost always obvious to our Mind; from whence it is very intelligible, tho' we want Words to describe it.

Every Body has Extension; without Extension there is no such thing as Body. And yet all that has Extension is not always a Body, although it is impossible to determine, how Body differs from mere Space; till the other Properties of Body shall first be ascertained.

John Second Thing to be examined in Body is Solidity. Body, having no Power to remove itself, will consequently exclude every other Body from the Place possessed by it; and the most fluid, as well as the hardest Bodies, have this Property.

because if a Body be extended, it is also divisible; for you may always conceive one Extension less than another. From whence we see, that there are Parts in all Extensions; which Parts in a Body may be separated from each other; Because,

Body hath a Fourth Property, that is, that it may be carried from one Place to another; whence

it is faid to be Moveable.

All Obstacles being removed, a Body yields to the least Blow: Nevertheless there is a greater Force required to move a Body with a greater Celerity than with a less, as also to move a greater than a smaller Body, allowing their Velocity to be equal. There is also a greater Force required

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bare conç required in the same Case to stop the Velocity of different Bodies in Motion. Hence it is, that Bodies at Rest, and Bodies in Motion, endeavour to continue in their State.

This arises from the Inactivity of Matter, (Inertia) which in all Bodies is ever proportionable to their Quantity of Matter, because it equally be-

longs to all the Particles of Matter.

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All Bodies have some Figure; whence Figura- 12 bility (that is, to be of some Shape or Figure) is commonly esteemed one of the essential Properties of Body, though it seems rather to be derived from other Properties.

If a Body be divided on every Side, and those Parts removed; what remains in the Middle is terminated on every Part, and consequently has a certain Figure. The same Body is capable of having different Figures; because it may be divided into Parts, and those Parts placed in different Order in respect to each other. Neither does it imply a Contradiction to say, that a Body, that should have no Figure, would be an infinite Body.

CHAP. III.

Of Extension, Solidity, and Vacuity.

The Learned) concerning a Vacuum, is to be confidered; namely, Whether there be an Extension void of all Matter; for this Extension is called a Vacuum, an Emptiness or mere Space.

That there is real a Vacuum, is proved from Phænomena: This Proposition therefore shall be

hereafter more fully treated of.

The Possibility of a Vacuum appears from the bare Examination of Ideas. For whatever we conceive to be possible may exist.

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The Question therefore amounts to this, viz Whether we have an Idea of an Extension that is not folid?

We feel that fome Bodies resist us; and indeed those Bodies resist us every Moment, that hinder us from descending to the lowest Places: From which Resistance it appears, that a Body excludes every other Body from the Place which itself takes up; that is, it appears that a Body is solid; which Idea of Solidity we transfer to those more subtile Bodies, which, by reason of the Smallness of their Parts, escape our Senses; and we find by Experience, that even those resist other Bodies, as well as the hardest.

14 Experiment.] The Air, in which we live, does almost always escape our Sight and Touch; yet in a Syringe, that is close shut at the End, it resists the Piston, so that it can be push'd to the Bottom of the Syringe by no Force.

The Idea of Solidity is not indeed contained in the Idea of Extension; that only follows from Contact, but this may be had without it; for if a Man had never touch'd a Body, he would have

no Notion of Solidity.

Let any one observe an Image projected in the Air, or represented between a Concave Mirror and the Object; such an Image does not resist, and yet it seems to be a Body as dense as the Object itself; for the Colours may appear more vivid in the Image than in the Object itself: If a Man had never seen any Thing else but such Images, and his own Body was like such an Image, could he have any Idea of Solidity? It does not appear that he could; and yet he would certainly have an Idea of Extension.

As

As we are here disputing of Ideas, we shall not consider what the above-mentioned Image is; it is enough that there is such a Thing.

All the Difference between Space and Body does 15

not confift in a Privation of Solidity.

That Space is infinite, and can be contained by no Limits, is plain to any one that attentively confiders it.

We plainly fee that Space has Parts, but they cannot be feparated from one another, being im-

moveable as Space itself.

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The Idea of Space is very simple; that of Body is more complex, it may be moved, its Parts are separated, and what is finite is easily conceived.

Solidity is by some call'd Impenetrability; and they endeavour to deduce it from the Nature of Extension: For Example, one cannot add one cubic Foot of Extension to another cubic Foot of Extension, without having two cubic Feet; for each of them has all that is required to constitute that Magnitude; therefore one Part of Space excludes all others, and cannot admit them.

Answer. This is all true, because the Parts of Space are immoveable; but it would be false, if it was not that it would imply a Contradiction, to suppose one Part of Space conveyed to another Place: And the Consequence follows only from the Immobility, not from the Impenetrability or

Solidity of the Parts of Space.

CHAP. IV.

Of the Divisibility of Body in infinitum; and of the Subtilty of the Particles of Matter.

HE Extension of a Body implies its Divifibility; that is, one may consider Parts
in it.

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Yet the Divisibility of Body differs from the Divisibility of Extension; for its Parts may be separated from one another. But, as this Property depends upon Extension, it must be examined under the Consideration of Extension. And then we may easily transfer to Body what is demonstrated.

18 Body is divisible in infinitum; that is, you cannot conceive any Part of its Extension ever so

small, but still there may be a smaller.

Let there be a Line AD perpendicular to BF, (Plate I. Fig. 1.) and another as GH at a small Distance from A, also perpendicular to the same Line, with the Centers C, C, C, &c. and Distances C A, C A, &c. describe Circles cutting the Line GH in the Points e, e, &c. The greater the Radius AC is, the less is the Part e G; the Radius may be augmented in infinitum, and therefore the Part e G may be diminished in the same Manner; and yet it can never be reduced to Nothing; because the Circle can never coincide with the Right Line BF.

Therefore the Parts of any Magnitude may be diminish'd in infinitum, and there is no End of

fuch a Division.

The fame Thing may be proved by a great ma-

ny other Mathematical Demonstrations.

The chief Objections are, — That an Infinite cannot be contained by a Finite; — That it follows from a Divisibility in infinitum, that all Bodies are equal, or, that one Infinite is greater than another.

But these are easily answer'd; for to an Infinite may be attributed the Properties of a finite and determined Quantity. Who has ever proved that there could not be an infinite Number of Parts infinitely small in a finite Quantity; or that all Infinites are equal? The contrary is demonstrated

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There are also other Objections proposed, suppoling that we affirm an actual Divilion of a Body into an infinite Number of Parts separated from We neither defend nor conceive one another. fuch a Division: We have demonstrated, that however small a Body is, it may still be farther divided; and, upon that Account, we believe that we may call that a Division in infinitum, because what has no Limits is call'd infinite.

There are no fuch Things as Parts infinitely fmall; but yet the Subtilty of the Particles of feveral Bodies is fuch, that they very much furpals our Conception; and there are innumerable Instances in Nature of such Parts that are actually

separated from one another.

Mr. Boyle has proved it by several Arguments.

He speaks of a silken Thread 300 Yards long, that weighed but two Grains and a Half.

He measured Leaf-Gold, and found by weigh- 22 ing it, that 50 square Inches weighed but one Grain: If the Length of an Inch be divided into 200 Parts, the Eye may diffinguish them all; therefore there are in one square Inch 40000 vifible Parts; and in one Grain of Gold there are two Millions of fuch Parts; which visible Parts no one will deny to be farther divisible.

A whole Ounce of Silver may be gilt with eight Grains of Gold, which is afterwards drawn

into a Wire thirteen thousand Foot long.

In odoriferous Bodies we can still perceive a greater Subtilty of Parts, and which are separated from one another; feveral Bodies scarce lose any sensible Part of their Weight in a long Time, and yet continually fill a very large Space with odoriferous Particles: Whoever will be at the Pains to make Calculations concerning those sub-

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tile Effluvia, will find the Number of Parts to be

amazing.

25 By Help of Microscopes such Objects, as would otherwise escape our Sight, appear very large: There are some small Animals scarce visible with the best Microscopes; and yet these have all the Parts necessary for Life, Blood, and other Liquors: How wonderful must the Subtilty of those Particles be which make up such Fluids!

We cannot end this Chapter more aptly than by the following Theorem, which is easily deduced from what has been said of the Subtilty of

Matter.

THEOREM.

and any finite Space, how large foever, being given; it is possible that that small Sand, or Particle of Matter, shall be diffused thro' all that great Space, and shall fill it in such Manner that there shall be no Pore in it, whose Diameter shall exceed a given Line.

CHAP. V.

Concerning the Cohesion of Parts, where we shall treat of Hardness, Softness, Fluidity, and Elasticity.

A LL Bodies, that are perceived by our Senfes, confift of very small Parts, no one of which is indivisible in itself; but all of them are in respect to us: For all the Division, we can make, is only a Separation of Parts.

When a great Force is required to make fuch a

Division, a Body is said to be Hard.

If the Parts yield more easily, and fall in by being press'd, such a Body is said to be Soft.

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But this great and lesser Force, in the common Signification, determine nothing; for a Body that is Hard, in respect to one Man, seems Soft to another.

DEFINITION I.

A Body is faid to be Hard, in a Philosophical Sense, when its Parts mutually cohere, and do not at 28 all yield inwards, so as not to be subject to any Motion in respect to each other, without breaking the Body.

DEFINITION II.

A Body is faid to be Soft, in a Philosophical Sense, when its Parts yield inwards, and slip in up-29 on one another, even tho' it may require a Blow with a Hammer to do it.

DEFINITION III.

A Body whose Parts yield to any Impression, and 30 by yielding are easily moved, in respect to each c-ther, is call'd a Fluid.

All these Things depend upon the Cohesion of Parts; the closer a Body is, the nearer it approaches to perfect Hardness.

But the Hardness of the smallest Parts does not differ from their Solidity; it is an essential Property of a Body, which is no more to be explained, than why a Body is extended, or a Mind thinks.

I do not know whether all Eodies confift of Parts that are equal and alike: And there are also several Things very difficult, in Relation to the Cause of the Cohesion of the small Parts of Bodies.

The Laws of Nature, which are admitted here, are deduced from Phanomena.

It is a particular Law of Cohesion, that all the 31 Parts have an attractive Force.

DEFI-

DEFINITION IV.

By the Word Attraction I understand, any Force by which two Bodies tend towards each other; tho'

perhaps it may happen by Impulfe.

But that Attraction is subject to these Laws; That it is very great, in the very Contact of the Parts; and that it suddenly decreases, insomuch that it acts no more at the least sensible Distance; nay, at a greater Distance, it is changed into a repellent Force, by which the Particles fly from each other.

By Help of this Law, feveral Phænomena are very easily explained; and that Attraction and Repulsion is fully proved by a vast Number of chymical Experiments. That there is fuch a Thing, appears also from the following Experiments.

- Experiment 1. We see that in all Liquors all the Parts attract one another, from the Spherical Figure that the Drops always have; and also because there is no Liquor whose Parts are not sticking to one another, which is evidently true even in Mercury itself.
- Experiment 2.] But this mutual Attraction of 33 Particles is much better proved; because in all Liquids, two Drops, as A and B (Plate I. Fig. 2.) as foon as they touch one another ever fo little, they immediately run into one larger Drop, as All which Things, as they also happen in liquified Metals, it follows, that the Parts of which they are compounded do attract one another, even when they are disjoined by the Motion of the Pire.

These Appearances do not depend upon the Presfure of the Air, because they also happen where there is no Air; neither do they depend upon the Pressure of any other Matter equally from all Sides; for though fuch a Pressure is able to keep the

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means bring them to it at first.

In the Oval Drop acbd, (Plate 1. Fig. 3.) the 34 Pressures upon the Surfaces ad and cb are less than the Pressures upon the Surfaces ac, db; for the Drop is supposed to be pressed equally from all Parts, therefore the Pressure is less in a less Space: Yet the Drop can never become round, till those lesser Pressures overcome the greater, which is absurd.

On the contrary, in Attraction, the greater the Number is of the Particles which attract one another between two Particles, the greater is the Force with which they are carried towards one another; which produces a Motion in the Drop, till the Diftances between the opposite Points in the Surface become every where equal; which can only happen in a Spherical Figure.

Several Bodies act upon other extraneous Bodies by this Attraction. I shall give a few Examples, in which the Effects of it are most remarkable.

Experiment 3.] Immerge in Water the Ends of 35 small Glass Tubes open at both Ends, in the Manner represented in Plate 1. Fig. 4. The Water will spontaneously ascend in them, and so much the higher as the Diameter is less. It is not required that the Tubes be extremely small; for the Experiments will succeed in Tubes whose Bore is the sixth Part of an Inch. That this is not to be attributed to the Pressure of the Air, appears from the following Experiment.

Experiment 4.] Having fixed the small Tubes A 36 to a Piece of Cork, and suspended them with the Brass Wire AB, (Plate I. Fig. 5.) pumpout the Air from the Recipient R, which stands upon the Brass Plate of the Air-Pump; then by moving the Wire

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AB, the Tubes may be immerfed in the Water which is contained in the Glass CD, and the Water in this Case will rise up into the Tube just as it did in the foregoing Experiment. How the Wire may be moved, without letting the Air into the Recipient, will be explained hereafter.

Planes, (Plate I. Fig. 6.) touching one another at AB, but a little feparated at CD, by thrusting a thin Plate of any Kind between them; they are sustained by the wooden Frame HIL M, in such Manner, that the Side DC is always at the same Height; the Planes may be brought to make any Angle with the Horizon, by raising the End AB where they are joined, the Cylinder NO likewise sustaining the Plane in any Position. The Screw

P makes fast the Cylinder at any Height.

A Drop of Water or Oil, G, is put between the Planes, fo as to touch both the Planes, which must before-hand be made wet with the same Liquor; this Drop is attracted by both Planes, but the Attraction has a greater Effect upon the Drop, where their Distance is the less; that is, a greater at e than at f, therefore the Drop is moved towards e; that is, afcends, and moves upwards the faster, in Proportion as it is higher, the Surfaces in which the Drop touches the Glasses growing very much, where the Distance between the Planes is diminish-The Angle of Inclination of the Planes may be so increased, that the Gravity of the Drop shall balance the Attraction, and then the Drop is at rest; and in that Case, if you raise the End A B of the Planes still higher, the Drop will descend by its Gravity, which will then overcome the Attraction.

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Experiment 6.] Let two Glass Planes, ABCD, Plate I. Fig. 7.) touch one another at AB, and at CD let them be a little separated by the Interposition of some thin Plate, and then let their Ends be immers'd into Water tinged with some Colour, in such Manner, that the Sides AB and CD may be in a vertical Position, the Planes having been moistened with the same Liquor before-hand. The Water will rise between those Planes by their Attraction, and rise highest where the Planes are nearest together; and as their Distance continually decreases from CD to AB, the Water rises up to different Heights in every Place, and makes the Curve Line efg.

Experiment 7.] Quickfilver unites itself to Tin 39 and Gold; also Water and Oil stick to Wood and clean Glass.

We have Instances of Repulsion between Water 40 and Oil, and generally between Water and all unctuous Bodies; between Mercury and Iron; as also between the Particles of any Dust.

than Water, is laid upon the Surface of Water, or Piece of Iron upon Mercury, the Surface of the Fluid will be depressed about the Bodies laid upon it, as it appears about the Ball A (Plate I. Fig. 8.) And after the same Manner, where the Attraction obtains, the Surface of the Liquor is higher about the floating Bodies, as about the Ball B, and does not run to a Level by its Gravity; so here where the repellent Force exerts its Action, Liquors, notwithstanding their Gravity, do not run down to fill up the Cavities which are made round the floating Bodies.

Upon this depend all the Phænomena of very 42 light Glass Bubbles (Plate I. Fig. 8.) which swim upon

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upon Water; when they are clean, the Water rifes about them all round, as at B; but, when they are made greafy, the Water makes an Hollow all round them, as at A; in the Glass Vessel where the Experiments are made, the Water also stands higher all round next to the Glass, as at C and D; but when the Glass is so fill'd that the Water runs down from all Parts, then, by the mutual Attraction of the Parts of the Water, it stands higher in the Middle than at the Sides, and forms the convex Surface ABC: (Plate I. Fig. 9.) From these Principles only can the following Experiments be explain'd.

Experiment 9, 10, 11, 12 and 13.] When a Glass is not quite full of Water, a clean Glass Bubble always runs to the Side, and there sticks, provided it be not laid on too far from it. The Bubble is press'd every Way by the Water, when it comes to the Side of the Vessel; the same Force, by which the Water is raised there, does in part take off that Pressure; so the Pressure on the other Side overcomes, and the Bubble is moved towards the Side of the Glass.

When the Glass is so full as to be ready to run over, the Bubble goes of itself from the Side to the Middle of the Glass, for the same Reason; because the Force, by which the Water is raised in the Middle, does also diminish the Pressure upon the Bubble towards the Middle.

Just the Reverse happens when the Bubble is greafy, because that Force, by which the Water and the Bubble repel one another, is greatest where

the Water is highest.

Two clean Bubbles, or two greafy ones, run towards each other. As to clean Bubbles, we have just given the Reason; when they are made greafy, there is a Cavity round each of them;

and

and where the Cavities join, the Pressure is diminish'd, and the Bubbles run that Way.

If one Bubble be clean, and the other greafy, they fly from one another, for the Reasons before

given.

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The Particles of any Salts attract one another 43 with a very great Force, as appears by several Experiments: The following will be sufficient to prove, that that Attraction exerts it self at a very small Distance, and the repellent Force at a greater.

Experiment 14.] Diffolve Salt in Water, and, when that Water is reduced into Vapour, the small saline Particles will unite together and form greater Lumps; which proves the Attraction.

These Particles are all equal, and of the same Figure: Whence it follows, that the least Parts, of which they are form'd, had every where the same Situation in respect to each other; that is, were every where diffused in the Water at equal Distances; which cannot be, unless they all repel one another with equal Forces.

The Elasticity of Bodies, namely, that Property 44 whereby they return to their former Figure, when it has been alter'd by any Force, is easily deduced from what has been said: For if a compact Body be dented in without the Parts falling into that Dent, the Body will return to its former Figure, from the mutual Attraction of its Parts.

We shall also in its proper Place shew, that 45 that Property of the Air, which is call'd its Elasticity, arises from the Force whereby its Parts repel one another.

And lest any one should imagine, because we 46 don't give the Cause of the said Attraction and Repul-

Repulsion, that they must be look'd upon as occult Qualities: We say here with Sir Isaac Newton, 'That we confider those Principles not as occult Qualities, which are supposed to arise from the specifick Forms of Things; but as univerfal Laws of Nature, by which the Things themselves are form'd: For the Phænomena of Nature shew that there are really such Principles, tho' it has not been yet explain'd what their Causes are. To affirm that the several Species of Things have occult specifick Qualities, by which they act with a certain Force, is just faying nothing. But from two or three Phænomena of Nature to deduce general Principles of Motion, and then explain in what Manner the Properties and Actions of all Things follow from those Principles, would be a great Progress made in ' Philosophy, tho' the Causes of those Principles should not yet be known.



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PART II.

Of the Motion of Solid Bodies.

CHAPIV.

Of Motion in general; where we shall speak of Place and Time.

HE Subject we are now entring upon has a large Scope in Physics: All that happens in natural Bodies belongs to Motion, and even what has been faid of the Cohesion of Parts, has a Relation to it: For though the Parts are not moved in their Cohesion itself, yet that Cohesion cannot be explain'd, nor can what is faid about it be confirm'd by Experiments, without Motion.

Motion is a Translation from one Place to ano- 47 ther Place, or a continual Change of Place. Every Body has an Idea of it; and Philosophers have invain laboured to find a Definition of the simple Idea, and proved with a great deal of Pains, that one may come to be ignorant of a Thing, which otherwise every Body knows.

Place is the Space taken up by a Body; of which 48 may be faid, what has just been faid concerning Motion.

It is Twofold; True or Absolute, and Relative.

DEFINITION I.

True Place is that Part of immoveable Space, 49 which a Body takes up.

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DEFINITION II.

by our Senses, is the Situation of a Body in respect of other Bodies.

True Place is often changed, whilst relative

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Place is not, and fo reciprocally.

Whence arises a True and Absolute Motion, and another Sort call'd a Relative Motion

Whilst a Body moves, Time goes on.

Time also is Twofold; True or Absolute, and Relative.

True Time has no Relation to the Motion of Bodies, nor to the Succession of Ideas in an Intelligent Being, but by its Nature it always flows equally.

DEFINITION III.

Relative Time is Part of the true Time meafured by the Motion of Bodies; and this is the

only Time that our Senses perceive.

All Motion may become fwifter, as likewise a Body may move slower than it did before; and it is very likely that there is no Motion of Bodies wholly equable; whence it follows, that relative Time differs from true Time, which never flows faster nor slower.

DEFINITION IV.

thro' a certain Space in a certain Time, is call'd Celerity or Velocity; which is greater or less, according to the Bigness of that Space, to which it is always proportionable.

DEFINITION V.

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Motion; and that Force is called the Quantity, or Momentum, of Motion.

DEFINITION VI.

The Direction of Motion is in a Right Line, 55 which we suppose drawn towards the Place where the moving Body tends.

DEFINITION VII.

A Power is any Force acting upon a Body to 56 move it.

DEFINITION VIII.

The Greatness of that Force is call'd, the In- 57 tensity of the Power.

CHAP. VIII.

Of Motions compared together.

AXIOMS.

THE Quantity, or Momentum, of Motion 58 follows the Proportion of the Cause producing the Motion.

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The whole Effects of Motions, produced at the 59 same Time, have the same Relation to each other, as the Momenta of those Motions.

If two equal Motions act in a contrary Directi- 60 on, they destroy each other; and the one can never overcome the other.

Bodies in Motion may differ in two Respects, 61 either in Respect to the Quantity of Matter in each, or in Respect of the Space gone thro' in the same Time, that is, in Respect of the Velocity, * and there is no other Difference: These *53.

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Two Things therefore, and only these two, are

to be confidered in comparing of Motions.

When the Velocities are equal, nothing is to be considered but the Quantities of Matter; and if it be double in one Body, the Quantity of Motion in that Body will also be double; because such a Body is made up of two Bodies, each equal to the least Body, and moved with the same Celerity as the little one. The same may be said of all other Relations between two Bodies; whence we deduce this general Rule:

In equal Bodies that move with the same Velocity, the Quantity of Motion is as the Quantity of

Matter in each.

When the Quantities of Matter are equal, the Velocities only are to be confidered: And then

In equal Bodies, the Momenta are as the Velocities: That is, as the Spaces gone thro' in the fame Time *. For the going thro' those Spaces are the whole Effects of the Motions produced in that Time, and are to one another as those Spaces; therefore the Momenta also are in the same

*59 Proportion. *

In Order to determine the Relation between two Motions, when the Velocities are unequal, and the Bodies different in Quantity of Matter; you must find two Quantities that are to one another as the Masses and as the Velocities. Multiplying the Velocities of each Body by its Mass or Quantity of Matter, the Products will be to each other in the said Proportion.

When, for Example, the Velocity is double, and the Mass triple, a double Quantity of Motion must be tripled; therefore it will be sextuple: This is the Case when in one Body the Velocity is two, and four in another; and the Mass of the first Five, the Mass of the other be-

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ing Fifteen; multiplying each Mass by its Velocity, the Products are 10 and 60, the last of which is six Times the first.

This is called a Ratio, compounded of the Ra-

tio of the Masses and the Celerities.

A greater Body may move more flowly than a lefs, in fuch a Manner, that the leffer Body may have an equal Quantity of Motion with, or a greater than the other.

When the Velocity in the lesser Body is to the 65 Velocity in the greater, as the Mass of the greater to the Mass of the lesser; the Quantities of Motion

are equal in the two Bodies.

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As much as the Quantity of Motion in the lesser Body is less, in Respect of its Mass, so much is it greater, in Respect of the Velocity: Whence an Equality arises. Likewise in that Case, the Products of the Mass of each Body by its Velocity are equal; and the Celerities are said to be in an inverse Ratio of the Masses, or reciprocally as the Masses.

When such Momenta of Motion att contrariwise, they destroy each other. *

CHAP. VIII.

How to compare the Actions of Powers.

THE Actions of Powers, acting upon Bodies, may be compared together, in the same Manner as the Quantities of Motion; and the same Rules serve for both.

We shall hereafter shew, that a Body once in Motion will continue in that Motion, tho' the Cause, that first gave it, ceaseth: So that if a Body should be continually acted upon by any Power, the Motion would become swifter every Moment.

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We do not here consider such an Action of Powers; but we take notice only of Powers that act against an Obstacle, in such Manner that, by the Resistance of the Obstacle the Action of the Power is continually destroyed, which is to be observed; for, in another Case, the following Demonstrations do not obtain. When therefore we speak here of an Obstacle to be removed by any Power, we speak of the greatest Obstacle that can be moved by that Power; for otherwise the Obstacle would not destroy the whole Action of the Power.

The Actions of Powers may differ from one another, both in Respect of the Greatness of the Obstacles, and in Respect of the Spaces run thro' by the Obstacles; (that is, by the Points to which the Powers are applied:) These two Things alone are to be consider'd in comparing of Powers.

The Obstacles, which may be removed by Powers, are to one another as the Intensities of

*57 the Powers. *

68

From whence it follows, that the Actions of Powers, equal in their Intensities, are to one another as the Spaces run thro'. For they only differ in that Respect, because the Obstacles are equal.

When the Spaces run thro' are equal, those Acti-

ons are as the Intensities.

69 When both the Spaces run thro, and the Intenfities, are different, the Actions of the Powers are to one another, in a Ratio compounded of the Intenfities and the Spaces gone thro?

When the Spaces gone thro' are in an inverse Ratio of the Intensities, the Actions are equal.

DEFINITION.

71 We call the whole Force of Power its Action, in Respect to Time; and therefore the whole Forces

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of Powers are to one another, as the Actions produced in the same Time.

These Things may be demonstrated in the same Manner, as what has been said in the foregoing Chapter.

CHAP. IX.

General Things concerning Gravity.

PHENOMENON I.

A LL Bodies near the Earth, if hinder'd by 72 no Obstacle, are carried towards the Earth.

DEFINITION I.

The Force, by which Bodies are carried towards 73 the Earth, is called Gravity.

DEFINITION II.

That Force, in Respect to a Body acted upon by 74 it, is call'd the Weight of a Body.

PHENOMENON II.

The Force of Gravity acts equally, and every 75 Moment of Time, near the Earth's Surface.

There is indeed a small Difference of Gravity in different Countries, which we shall take Notice of hereafter; but it is too small to be considered here, especially because it is wholly insensible in neighbouring Countries.

When the Descent of a Body is hinder'd by an 76 Obstacle, it continually presses that Obstacle equally, tending towards the Earth's Center; therefore it may be look'd upon as a Power acting upon an Obstacle; and therefore what has in the foregoing Chapter been demonstrated, concerning Powers, does obtain here also.

PHENO-

PHENOMENON III.

77 Bodies which descend by the Force of Gravity, (if all Resistance be taken off) fall with the same Velocity. Which is prov'd by an

Experiment.] Pump out the Air from the tall Recipient AB (Plate II. Fig. 1.) which is made up of two Glasses, and is about three Foot high: Then from the Top of the Glass within, by moving the Handle CD, let fall a Piece of Gold and a very light Feather just at the same Time, and they will always come down to the Brass Plate of the Pump upon which the Receiver stands, at the same Instant of Time.

of the Recipient is cover'd with a Brass Plate laid upon it. A thin Plate, bent into the Figure E, is fixed to the covering Plate at e, by Help of two Screws H, that go thro' two lesser Plates, one of which you see at gf, and are joined to the other Plate E.

The Ends of the Plate spring together, and so hold the Feather and the Gold, whilst the Receiv-

er is exhausting.

A Brass Wire runs thro' the Cover, which, by Means of the Handle C D, may be turned round without admitting the external Air; which we shall explain, when we come to speak of the Air-Pump.

The Wire goes thro' an Hole in the upper Part of the Plate e, and the End of the Wire, which comes down between the fpringing Plate, may be feen at L: It is fquare and hollow, that the O-

val Plate I may be joined to it,

You must observe, that the small Diameter of the Oval be small enough for this little Plate to be contained between the Springs E, when their Ends come together. Plat fere Spri pend Tim

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Now when the Brass Wire, and by it the Plate I i is turned round; by Reason of the Difference of Diameters in the Oval, the Ends of the Springs open; and then the Bodies, that are suspended, are let go at the same Moment of Time.

The same Phænomenon is also deduced from another Experiment, which we shall mention hereafter. *

Hence it follows, that Gravity in all Bodies, 79 that is, their Weight, is proportionable to their *62

Quantity of Matter.*

Therefore all Bodies consist of Matter that is 80 equally heavy; and the Reason, that Bodies do not appear equally heavy, is because some have more Matter than others under the same Bulk; that is, in the same Space.

When Weight is considered as a Power, the Intensity of the Power is proportional to the Quantity of Matter in the heavy Body; and the Direction of the Power is towards the Center of

the Earth.

CHAP. X.

Of the single Pulley, Balance, and of the Center of Gravity.

DEFINITION I.

A Single Pulley is a little Wheel moveable about 82 its Axis, overwhich goes a drawing or run-

ning Rope, d ce (Plate I. Fig. 10.)

By this Engine, the Direction of the Power is changed, neither is it of any other Use when fix'd; for in that Case, if the Force of Power apply'd to the 83 drawing Rope, as M, be equal to the Obstacle P, it balances that Obstacle *; for inthat Case the Power can't *71

move

move, unless the Obstacle does at the same Time go

through an equal Space.

*79 Matter in Bodies are compared together *, by a Balance, or a Pair of Scales, which is a well known Instrument.

DEFINITION II.

84. The Axis of a Balance is that Line about which the Balance moves, or rather turns round.

DEFINITION III.

When we confider the Length of the Brachia, or of the Beam, then the Axis is to be looked upon as a Point, and called the Center of the Balance.

DEFINITION IV.

We call Points of Suspension, or Application, those Points where the Weights really are, or from which they hang freely; or the Scales in which the Weights are placed.

Concerning this Machine, we are to ob-

ferve,

87 That the Weight does equally press the Point of Suspension, at whatever Height it hangs from it, and in the same Manner as if it was fixed at that very Point.

For the Weight, at all Heights, equally stretch-*74.75 es the Rope by which it hangs. * This is also

proved by

Experiment 1.] In the Balance AB, the Weight P, by Means of the Rope BD (Plate II. Fig. 2.) is suspended at different Heights: And the Position of the Balance is not changed by it.

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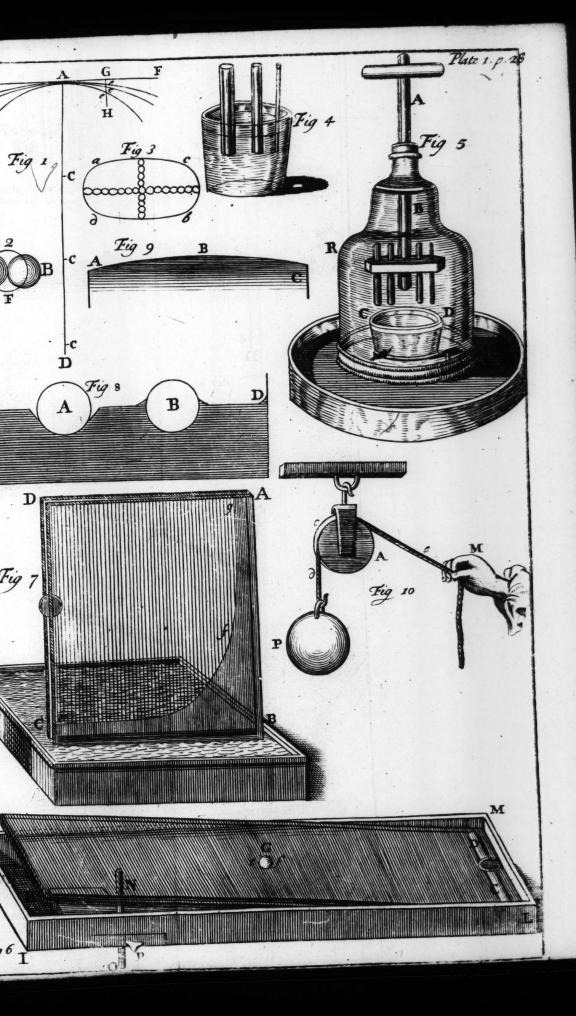
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The Action of a Weight to move a Balance is by 88 so much greater, as the Point pressed by the Weight is more distant from the Center of the Balance; and that Action follows the Proportion of the Distance of the said Point from that Center.

When the Balance moves about its Center, the Point B describes the Arc Bb (Plate II. Fig. 3.) whilst the Point A describes the Arc Aa, which is the biggest of the two; therefore, in that Motion of the Balance, the Action of the same Weight is different, according to the Point to which it is applied, and it follows the Proportion of the Space* gone through by that Point: At A there-*67.76 fore it is as Aa, and at B as Bb; but those Arcs are to one another, as CA, to CB.

Experiment 2.] The Brachia of the Balance AB (Plate II. Fig. 4.) are divided into equal Parts; and one Ounce, applied to the ninth Division from the Center, is as powerful as three Ounces at the third; and two Ounces at the fixth Division act as strongly as three at the fourth, &c.

The Construction of a Balance, for this and some other sollowing Experiments, is plain enough from the Figure, adding to it what is said at Numb. 102. Hence it sollows, that the Action of a Power to move a Balance is in a Ratio compounded of the Power it self, and its Distance from the Center*; for that Distance is * 69 as the Space gone through in the Motion of the Balance.

DEFINITION V.

A Balance is said to be in Equilibrio, when the 89 Actions of the Weights upon each Brachium, to move the Balance, are equal; so that they mutually defiroy each other; as appears by the foregoing Experiment.

DEFINITION VI.

When a Balance is in Æquilibrio, the Weights

on each Side are faid to æquiponderate.

Unequal Weights can aquiponderate. For this, it is requisite, that the Distances from the Center to be reciprocally as the Weights.* In that Case, if each Weight be multiplied by its Distance, the Products will be equal.

Experiment 3.] In the above-mentioned Balance (Plate II. Fig. 4.) one Ounce at the Distance of the ninth Division from the Center, æquiponderates with three Ounces at the third Division.

The Steel-yard, or Statera Romana, which weighs every Thing with one Weight, is made

upon this Principle.

Experiment 4.] The Steel-yard A B (Plate II) Fig. 5.) has two Brachia very unequal; a Scale hangs at the shortest; the longest is divided into mequal Parts: Apply such a Weight to it, that, at the first Division, it shall æquiponderate with one Ounce laid in the Scale; then the Body to be weighed is put into the Scale, and the abovementioned Weight is to be moved along the longest Brachium, till you find the Æquilibrium; the Number of Divisions, between the Body and the Center, shew the Number of Ounces that the Body weighs, and the Subdivisions the Parts of an Ounce.

Upon this Principle also is founded the deceitful Balance, which cheats by the Inequality of

the Brachia.

Experiment 5.] Take two Scales of unequal Weights, in the Proportion of 9 to 10 (Plate III. Fig. 1.) and hang one of them at the tenth Division

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Division of the Balance above described, and the other at the ninth Division, so that there may be an Æquilibrium: If then you take any Weights, which are to one another as 9 to 10, and put the first in the first Scale, and the other in the other Scale, they will æquiponderate.

one Side, may æquiponderate with a fingle Weight on the other Side. To do this, it is required, that the Product of that Weight, by its Distance from the Center, be equal to the Sum of the Products of all the other Weights, each being multiplied by

its Distance from the Center.

Experiment 6.] Hang three Weights of an Ounce each, at the second, third and fifth Divisions from the Center, and they will æquiponderate with the Weight of one single Ounce applied at the tenth Division of the other Brachium (Plate II. Fig. 6.) And the Weight of one Ounce at the fixth Division, and another of three Ounces at the fourth Division, will æquiponderate with a Weight of two Ounces on the other Side at the ninth Division.

Several Weights, unequal in Number, on either Side, may equiponderate. In that Case, if each of them be multiplied by its Distance from the Center, the Sums of the Products on either Side will be equal; and if those Sums are equal, there will be an Æquilibrium.

Experiment 7.] Hang on a Weight of two Ounces (Plate II. Fig. 7.) at the fifth Division, and two others, each of one Ounce, at the second and seventh; and on the other Side hang two Weights, each also of one Ounce, at the ninth and tenth Divisions; and these Two will æquiponderate with those Three.

DEFI-

DEFINITION VII.

The Center of Gravity is a Point in a Body about which all the Parts of the Body (whateve

Position it is in) are in aquilibrio.

When two or more Bodies are joined, whether they are contiguous or separated, they have common Center of Gravity.

When the Center of Gravity is fustained, the

Body remains at reft.

Experiment 8. The Body A (Plate III. Fig. 2.) is fustained and at rest, because its Center of Gravity is fustained by the Prop F.

When the Center of Gravity is not fustained, the Body moves till that Center comes to be

fustained.

Experiment 9.] The Body A, laid upon the Table, will fall, and the Body B will not remain in its Polition, because their Centers of Gravity are not fustained.

Hence may be known, why fome Bodies, laid upon inclined Planes, will foll off, whilft fome

only flide off.

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Experiment 10.] The Body A slides, because its Center of Gravity is fustained by an inclined Plane; (Plate III. Fig. 4.) that is, the Vertical Line, which goes through that Center, c cuts the inclined Plane within the Body. But the Body B rolls, because the Vertical Line, thro' its Center of Gravity, cuts the inclined Plane without the Body.

100 From what has been faid it follows also, that a Body descends, when its Center of Gravity descends, that is, is moved towards the Center

of the Earth.

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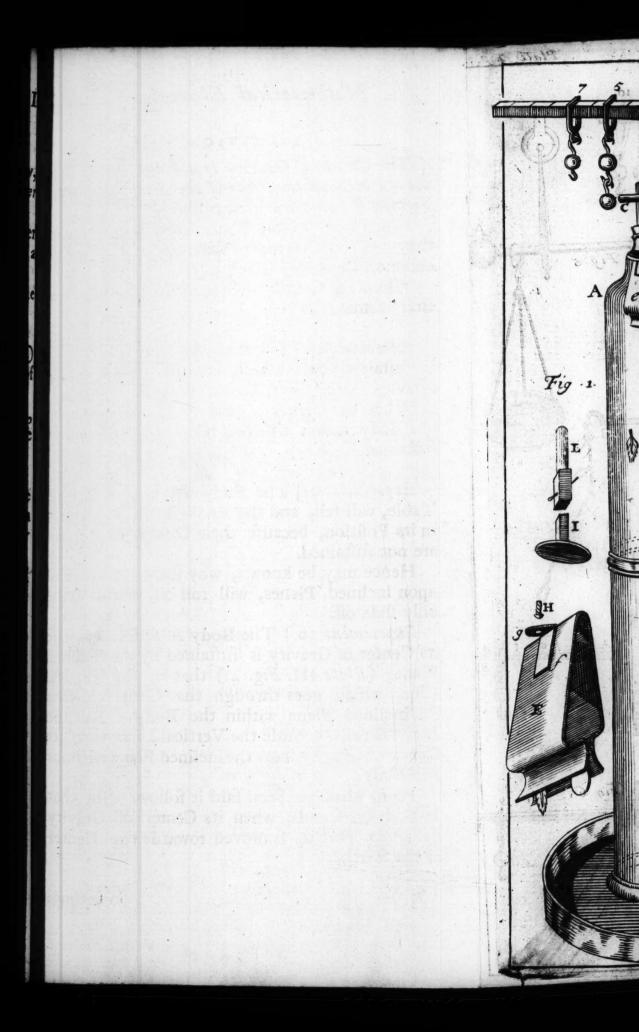
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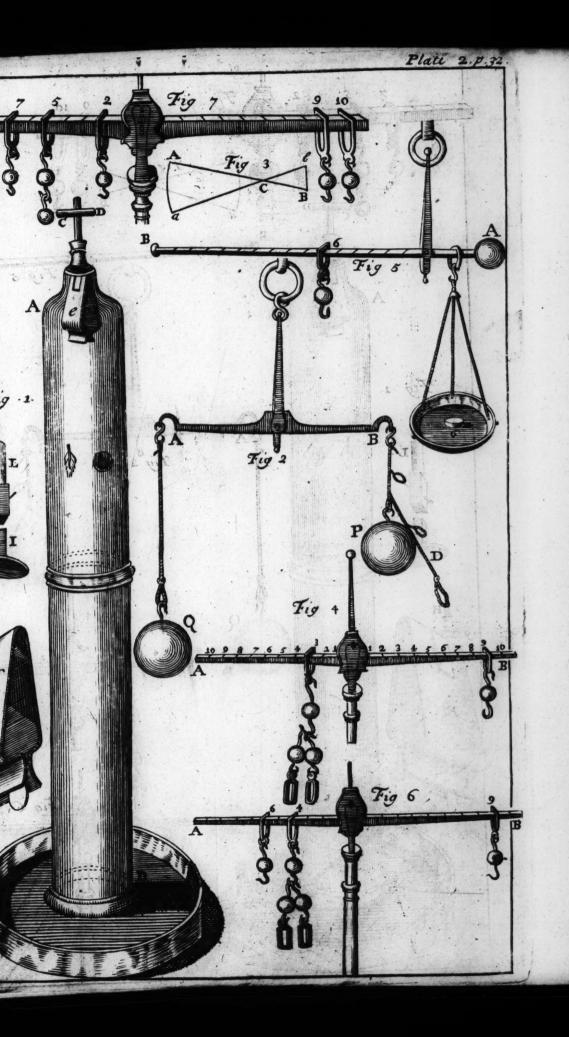
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Sometimes in that Case a Body seems to ascend, and oftentimes it does really afcend; but as all Bodies descend by Gravity, that is, their Centers of Gravity descend; it follows, that a Body feems to afcend by its Gravity, and can really ascend.

Experiment 11. The Wheel A (Plate III. Fig. 6.) whose Axis is made of two Cones, the Bases of which join to the Wheel, when put between two Planes, whose Sides DG, FH continued, make the Angle F C D, which has the Base, (supposing . a Triangle made) higher than the Vertex, will from H G, the lower Part of the Planes, roll towards F D, the highest Part of the Planes.

By reason of the greater Distance between the Planes at FD, the Wheel A, whose Axis is a Cone both Ways, descends more between the Planes, when it moves towards that Part, and is fo carried thither by its Gravity, provided that Defcent be greater than the Ascent from the Inclina-

tion of the Angle FCD with the Horizon.

Experiment 12. The Wooden Cylinder A (Plate III. Fig. 5.) has within it, near the Side, a Leaden Cylinder; their common Center of Gravity is in a Section parallel to the Base, which divides the Cylinder into two equal Parts, and in a Point answering to the Point c of the Bafe.

Whatever Position this Cylinder be laid in, it will move until the above-mentioned Center of Gravity be in the lowest Place which it can come to.

If it be laid upon an inclined Plane, in the Pofition described in the Figure; the Center of Gravity will descend whilst the Body rises along the Plane, if it be inclined in a fit Manner.

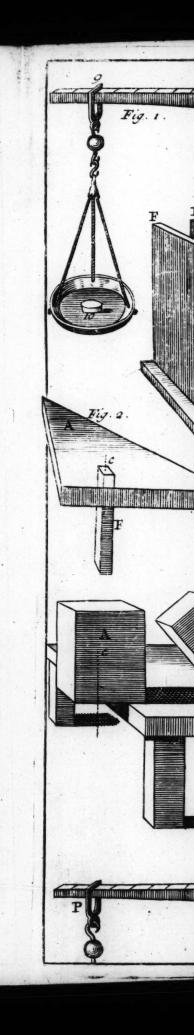
The Body ascends by rolling towards the upper Part of the Plane, but Care must be taken, that, whilst it is endeavouring to roll up, it does not slide down along the Plane; and therefore you must use a Rope, which goes in part round the Cylinder, one End of which is joined to the Cylinder at f, and the other is fixed to the Plane at d.

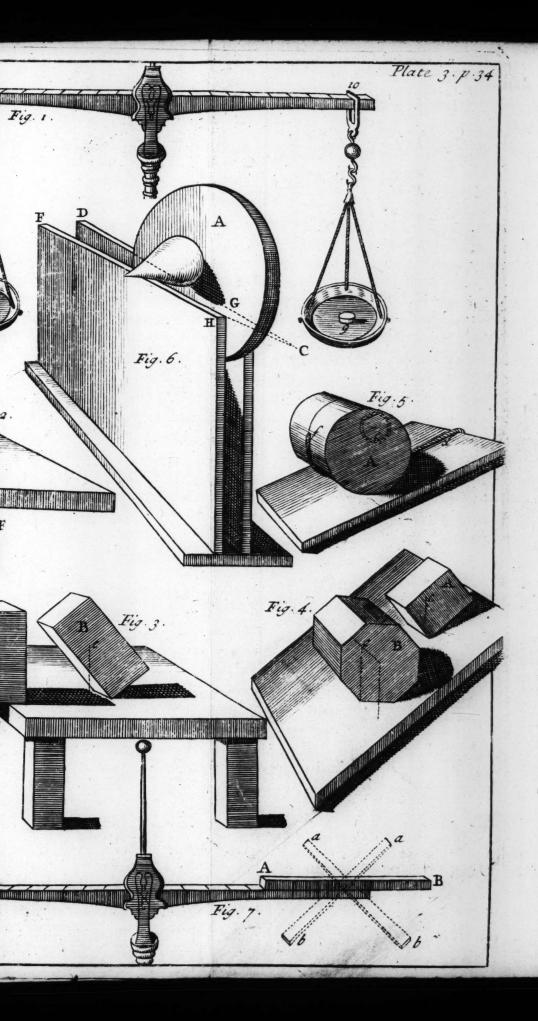
rom what has been faid of the Center of Gravity, it is farther deduced, that whatever Point of a Body or Machine fustains the Center of Gravity of any Weight, that Point sustains the whole Weight: So that the whole Force, by which any Body tends towards the Earth, is, as it were, collected in that Center.

Experiment 13.] If the Body A B (Plate III. Fig. 7.] whose Center of Gravity is laid upon the Brachium of a Balance, does in any Position equiponderate with any Weight P; it will in any other Position, as ab, ab equiponderate with it, provided the Center of Gravity be still at C.

1. That the Points of Suspension of the Scales or Weights be exactly in the same Line as the Center of the Balance. 2. That they be precisely equidistant from that Point on either Side. 3. That the Brachia of the Balance be as long as they conveniently can. 4. That there be as little Friction as possible in the Motion of the Beam and Scales. 5. And lastly, that the Center of Gravity of the Beam be placed a little below the Center of Motion.







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CHAP. XI. Of the LEVER.

DEFINITION I.

A Lever is call'd by Mathematicians, an in-103 flexible Right Line, made use of to raise Weights, either weighing nothing itself, or of such Weight as may be balanced. (Plate IV. Fig. 1.)

It is the first of those that we call Simple Machines (or Mechanical Powers) as being the most Simple of all; and it serves, when Weights are to be raised but to a small Height.

There are four other Simple Machines, which

we shall treat of in the three following Chapters.

Concerning the Lever, three Things are to be considered.

1. The Weight tobe raifed or fustained, as P.

2. The Power, by which it is to be raised or sustained, which here is represented by the Weight M, tho' commonly it is the Action of a Man. 3. The Fulcrum, or Prop, by which the Lever is sustained, or rather on which it moves round, whilst the said Point F remains fixed.

The Lever is threefold.

1. Sometimes the Fulcrum is placed between 104 the Weight and the Power. (Plate IV. Fig. 1.)

2. Sometimes the Weight is between the Fulcrum and the Power. (Plate IV. Fig. 2.)

3. And often also the Power acts between the Weight and the Fulcrum. Plate IV. Fig. 3.)

The same Rules serve in all these Cases, which follow from what has been said of the Balance *: * 88 And this shews the Analogy between the Lever and the Balance. The Lever of the first Kind is, as it were, a Steel-yard to raise Weights.

The Action of a Power and the Resistance of the 105 Weight increase, in proportion to their Distance from * 88 the Fulcrum*; and therefore, that a Power may be able to sustain a Weight, it is required, that the Distance of the Point in the Lever, to which it is applied, be to the Distance of the Weight, as the * 90 Weight to the Intensity of the Power*; which, if it be ever so little increased, will raise the Weight.

Experim. 1, 2, and 3.] This Rule is confirm'd by Experiments, in respect of the three Levers, as it appears from the first, second and third Figures of the fourth Plate; for there is an Æquilibrium, when the Weights P, and the Weights M, which represent the Powers, and also the Distances from the Fulcra, bear those Proportions to each other, as the Numbers written in the Figures express. A Sight of the Figures so plainly shews the Construction of the Machines wherewith the Experiments are made, that a further Explanation would be needless.

Workmen also make use of a Lever, to carry Weights; and there are several remarkable Cases of those Levers, the Demonstration of which may

be deduced from what has been faid.

that the Intensity of the Power, or the Intensities of the Powers taken all together (when there are more than one) must act as strongly as the Gravity of the Weights to be carried or sustained.

two Powers, it must be placed between the two Powers, and the Distances of the Powers on each Side of the Weight must be in an inverse Ratio of

the Intensities of the Powers.

Experiment 4.] This Proposition is confirm'd by the Experiment of Fig. 4. which requires no farther Explanation.

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Experiment 5. When two Weights are to be 108 fustained by one Power, that Power must be placed between the Weights, and then what has been faid before of the Powers must be applied to

the Weights. See Fig 1. Plate V.

Several Weights are often carried or fustained by one or more Powers. In which Cafes it is 100 to be observed, That all Weights, in whatever Pofition, have one common Center of Gravity; which Center is fuch, that if, on either Side, each Weight be multiplied by its Distance from that Point, the Sums of the Products on each Side will be equal.*

Let the Powers also be disposed in any Position, they have a common Center of Gravity; for they may be represented by Weights;* and here the * 76 Intensity of each Power is to be multiplied by its Distance from the Center, and the Sums of the Products will then be equal on both Sides: That the Powers may be able to sustain the Weights, it is required that the Center of Gravity of the Powers and the Weights be the lame.

Experiments 6, and 7.] What has been faid fufficiently explains the Figures, (Plate V. Fig. 2, and 3.) where C denotes the Center of Gravity common to the Weights and the Powers.

Experiment 8.7 What has been faid is true, if 110 the Lever is drawn (Plate V. Fig. 4.) by Powers on each Side; which we fee in the Lever of Fig. 4. which is drawn Horizontally on each Side; where the Æquilibrium only depends upon what has been laid down in the Rules above-mention'd.

We may also make use of a compound Lever III for raising Weights. In which Case, instead of a Power, a second Lever is applied to the first,

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and a third to that, and so on as far as you will, and a Power is applied to the last Lever; and then the Ratio of the Power to the Weight (when it sustains it) is compounded of the Ratio's of the Power to the Weights in each Lever, when they are used separately.

Experiment 9.] The three Levers A, B, D, are so disposed (Plate IV. Fig. 5.) that the Power M sustains the Weight P. In the Lever A, if it were used singly, the Power would be to the Weight as 1 to 5; the Lever B, as 1 to 4; and in the Lever D, as 1 to 6. The Ratio, compounded of all these, is as 1 to 120. For one Ounce M does here sustain the Weight P, of 120 Ounces. Observe, that in the Motion of this Engine, the Spaces gone thro' by the Weight and the Power are to one another, as 1 to 120; that is, in the said inverse Ratio, which is requir'd to make an Æquilibrium.*

CHAP. XII.

Of the Axis in Peritrochio, and Wheels with Teeth.

THE Lever, as was faid in the Beginning of the foregoing Chapter, serves to raise Weights to a small Height; when they must be raised higher, we use an Axis in Peritrochio.

DEFINITION.

112 We call Axis in Peritrochio, a Wheel which turns together with its Axis. (Plate V. Fig. 5.)

The Power in this Machine is applied to the Circumference of the Wheel, by whose Motion, a Rope, that is tied to the Weight, is wound about the Axis by which the Weight is raised.

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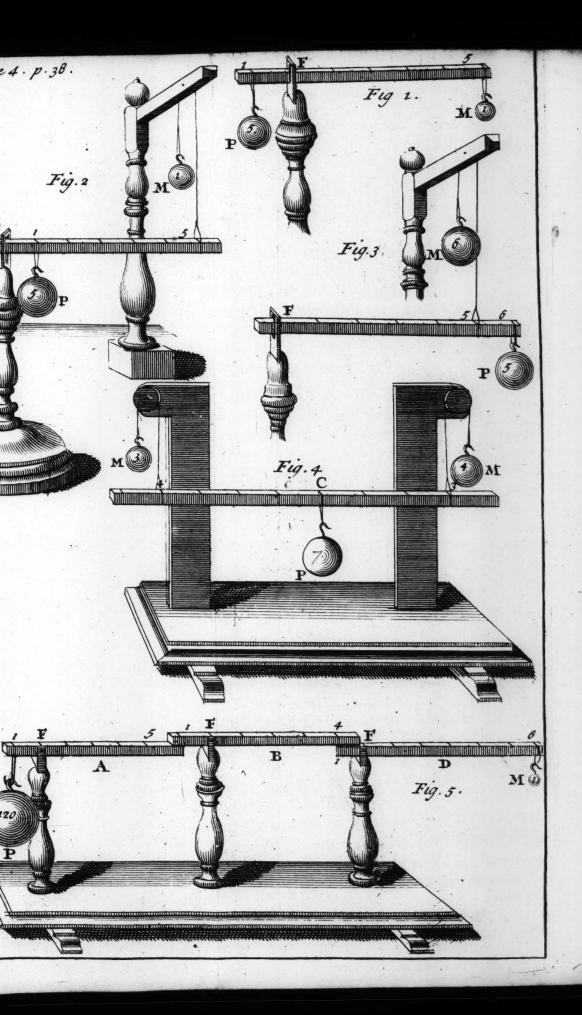
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fe ha Let ab be the Wheel, (Plate V. Fig. 6.) de the Axis, p the Weight to be raised, m the Power; as the Wheel is moved by the Power, the Points b and d describe similar Arcs, which are the Ways of the Power and the Weight, and are to each other, as cb to cd, that is, as the Diameter of the Wheel to the Diameter of the Axis;

whence the following Rule is deduced.

The Power has the greater Force, the greater 113 the Wheel is, and its Action increases in the same Ratio as the Wheel's Diameter. The Weight resists so much the less as the Diameter of the Axis is less, and its Resistance is diminished in the same Ratio as the Diameter of the Axis. And that there may be an Aquilibrum between the Weight and the Power, it is always requisite that the Diameter of the Wheelbe, to the Diameter of the Axis, in an inverse Ratio of the Power to the Weight. * *70

It is to be observed, that you must add the Diameter of the Rope to that of the Axis.

Experiment 1.] This Rule is variously confirm'd (Plate V. Fig. 5.) by Help of the Machine here represented. When the Axis is the twelfth Part of the Diameter of the Wheel, half a Pound sustains six Pounds; and so on.

The Power also may be applied to an Handle or Spoke; as at D, and then the Distance of the Point to which it is applied, reckon'd from the Center, must be look'd upon as the Wheel's Se-

midiameter.

The Wheels, that have Teeth, work in the same Manner as this Machine; they being, in respect of the Axis in Peritrochio, what the compound Lever is, in respect of the simple Lever.

If the Axis of the Wheel has Teeth also, it 114 ferves to move a Wheel, whose Circumference has Teeth; and this Axis of the last Wheel may

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again communicate Motion to a third Wheel, and so on. In that Case, that the Power may suftain the Weight, its Ratio to the Weight is compounded of the Ratio of the Diameter of the Axis of the last Wheel, to the Diameter of the first, and the Ratio of the Revolutions of the last Wheel, to the Revolutions of the same Time.

The Demonstration of which Rule is also deduced from the Comparison of the Ways run thro' by the Weight and the Power. (Plate V. Fig. 7.)

Experiment 2.] Let the Power represented by the Weight M be applied to the Wheel A B, and the Weight P to the Axis of the Wheel F G, the Diameter of that Axis is the eighth Part of the Diameter of the Wheel A B, and this Wheel goes round five Times, whilst the Wheel F G goes round once: Therefore the Ratio of the Power to the Weight is compounded of the Ratio's of I to 8; and I to 5: Therefore it is the Ratio of I to 40; half a Pound in this Case sufficiently go Pounds.

CHAP. XIII. Of the PULLET.

N several Cases, where the Axis in Peritrochio cannot conveniently be applied, Pullies must be made use of to raise Weights; a Machine, made by combining several of them, lies in a little Compass, and is easily carried about.

What a Pulley is, has been already explain'd. *

If the Weight be fix'd to the Pulley, so that it may be drawn up along with it, each End of the Drawing or Running Rope sustains Half the Weight. Therefore when one End is fix'd, either to a Hook, or any other Way, the moving Force or Power applied to the other End, if it be equal to half the Weight, will keep the Weight in Aquilibrio.

Expe

Experiment 1.] Make fast the Weight P of two. Pounds to a Pulley (Fig. 1. Plate VI.) yet so that the Wheel or Sheave may not be hindered from turning round; let one Part of the Rope ef be tied to a Hook; and the other End cd go round the fix'd Pulley, to change the Direction, * the *83 Weight M of one Pound, fix'd to this End of the

Rope, will fustain the eWight P.

several Sheaves may be joined in any Manner, 116 and the Weight be fix'd to them; then if one End of the Rope be fix'd, and the Rope goes round all those Sheaves, and as many other fix'd ones as is necessary, a great Weight may be raised by a small Power: In that Case the greater the Number of Sheaves fix'd in a moveable Pulley, or of moveable Wheels, (for the fix'd ones do not change the Action of the Power *) so much may the Power *3 be less, which sustains the Weight; and a Power which is to the Weight, as the Number One to twice the Number of the Sheaves, will sustain the Weight.

The Reason is, that the Number last mentioned is the Number of the Ropes that sustain the Weight, and the Power is applied only to one

Rope.

N.B. The Workmen in England call a Block, the Box or Piece of Wood that has one or several Wheels in it; and those Wheels, Sheaves or Sheevers.

Experiment 2.] Hang the Weight P of 6 Pounds to the Piece AB (Plate VI. Fig. 2.) in which three Sheaves turn freely round. Let one End of the Rope be fasten'd to an Hook, and let the Rope go round those three Sheaves, and three other fix'd ones: One Pound, fix'd to the other End of the Rope, will make an Æquilibrium.

Experiment 3, and 4.] The different Make of the Pullies, or the different Way of joining the Sheaves

Sheaves together, makes no Alteration; the last Sort is not very convenient for raising Weights, and therefore Workmen make use of unequal Sheaves, joined together in the Manner represented in Fig. 3. for the different Bigness of the Sheaves makes no Alteration. Oftentimes all the Sheaves move round the same Axis, as in the 4th Fig. and so the Pullies lie in the least Room. Now in both these Cases the Experiments answer as before.

When the End of the Rope, which in the foregoing Experiments was fix'd, is joined to the Weight, or to the moveable Wheels, then the Ratio of the Power to the Weight is no longer, as I to twice the Number of the Sheaves joined to the Weight; but this double Number must be increased by I; and then, where two Sheaves are joined to the Weight, the Ratio will be as I to 5; for there are just so many Ropes, which sustain the Weight. See Plate VI. Fig. 5.

with one Wheel in each, and each having its own particular Rope, be disposed in the Manner represented in *Plate VII. Fig.* 1. the Action of the Power will be very much increased; for every Wheel doubles it, and therefore it is four Times greater with two Wheels, and eight Times greater with three, and so on.

The Rule above-mentioned, (namely, that the Spaces gone thro' by the Power and Weight, when they balance each other, are to one another inversely as the Power to the Weight,) may be applied in all the Cases above-mentioned.

Here we always suppose the Ropes parallel; we shall hereafter shew what Difference is made by the Obliquity of the Ropes.

CHAP.

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CHAP. XIV.

Of the WEDGE and SCREW.

Rom what has been faid, it plainly appears, how great a Weight may be sustained, or even raised, by a little Power; but those are not the only Ways of producing the same Effect. Mechanicks are not confined only to those Methods; the Actions of Powers may be increased in all Cases: A very good Instance of it appears in the Wedge, which is contrived for cleaving Wood, and also useful in several other Cases.

DEFINITION I.

A Wedge is a Prism of a small Height, whose Ba-118 ses are æquicrural Triangles, as A, Plate VI. Fig. 6.

DEFINITION II.

The Height of the Triangle is the Height of the Wedge; as db.

DEFINITION III.

The Base of the Triangle is also called the Base of the Wedge; as ce.

DEFINITION IV.

The Edge of the Wedge is a Right Line, which joins the Vertices of the Triangles; as bf.

The Edge of the Wedge is applied for cleaving Wood; and the Power is the Blow of a Hammer or Mallet, which drives the Wedge into the Wood.

When the whole Wedge is driven in, the Space, gone thro' by means of the Blow or Blows, is the Height of the Wedge, which therefore may be look'd upon as the Space gone thro' by the Power; and the Space, which the Wood goes thro'

120

thro' as it yields on each Side, is half the Base of the Wedge. Whence it follows, That the Power is to the Resistance of the Wood (when its Action is equal to it) as the half Base of the Wedge is to its Height.

What is here faid, of the Resistance of the Wood, may be applied to all the other Uses of

the Wedge.

The two wooden Rules AA, AA, are kept up in a parallel and horizontal Situation by the Feet BB, BB. (Plate VI. Fig. 7.)

The Brass Rulers CC, CC, are fix'd to them

on the Infide.

Between them are moved the two Barrels, or Wooden Cylinders E E, which turn upon small Steel Axes that come out behind the Rulers, and have a small Return at their Ends, or the Bases are bigger than the Cylinders; each Return is a little convex on the Outside, that the Friction against the Rulers CC, CC, may be the less. In the Middle of each Ruler AA, there are two Pullies d, d, which almost touch one another, and whose upper Part is even with the Top of the Rulers CC.

The Rope, which in its Middle carries the Weight P, goes round the Pullies d, d, and each End of it is fixed to the Axis of one Cylinder E, by Means of a small Plate that has a Hole throwhich the Axis goes. The other Weight P hangs in the same Manner upon such another Rope.

Therefore the Cylinders EE must be carried towards one another in an horizontal Motion (their Axes remaining parallel) by the Weight

P, if they are equal.

Let there be a Wedge made of two wooden Planes FF, which make any Angle at Pleasure by Help of the Screw gg.

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Experiment. The Cylinders E E are separated by letting down the Wedge FF between them, which is drawn down by the Weight M, and you have an Æquilibrium, when the Weight M, together with the Weight of the Wedge, is to the Weights P, P, as the half Base of the Wedge to

its Height.

The Force with which the Cylinders are carried towards one another, and which must be overcome to separate them, is here instead of the Refistance of the Wood; the Force with which the Wedge is driven or drawn between the Cylinders, that is, the Weight of the Wedge, together with the Weight M, is here taken for a Blow with a Mallet; and so the foregoing Rule is reduced to Experiment, and confirmed by it.

The Screw has a great Affinity with the Wedge.

It confifts of two Parts.

DEFINITION V.

The first, which is called the Male Screw, or 121 Outside Screw, is a Cylinder cut in, in a Helical

Form, as AB (Plate VI. Fig. 8.)

The fecond, which is called the Female Screw, or Infide Screw, and fometimes the Nut, and is different according to the different Uses of the Machine of which it is made a Part, is a folid Body that contains an hollow Cylinder, whose Concave Surface is cut in the same Manner as the Male Screw, so that the Prominent Part of the one may fit the Cavity of the other; as DE.

N. B. The Prominent Helical Part is called the

Thread of the Screw.

These two Parts are to move one within another, when the Screw is applied to Use. It serves chiefly to press together such Bodies as must be joined and firmly united; for in this Machine

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Book I.

Pressure. The Screw may also be used for raising Weights. In every Revolution of it, one Part remaining at rest, the other is thrust out as far as the Interval between two Threads. The Power which moves the Screw is applied to an Handle or Hand-Spike; and then the Power, which acts as strongly as the Resistance, is to the Resistance as the said Distance between two Threads to the Periphery of a Circle, run thro' by that Point of the Handle to which the Power is applied. For the Way gone through by that Point or Plane, wherewith the Resistance is overcome, has the same

Ratio to the Way of the Power.

Here we must observe, that when the Power balances the Weight in any Machine whatever, where no Friction is supposed; that, by encreasing the Power ever fo little, it will over-balance the But when there is any Friction, that Weight. Friction must also be overcome by the Power; and how much must be added to it, to produce that Effect, cannot be determined mathematically. In the Machine last mentioned, this Friction is very fenfible, and also of a great Use; for by it the Machine is kept in its Polition, and cannot (either by the Action of the Bodies that are pressed, or the Gravity of the Weights) receive a contrary Motion, so as to be pushed back to its first Position.

CHAP. XV.

Of Compound Engines.

111 E have already shewn, how a Machine may be compounded of several Levers †; or several Wheels; and that in such Machines the Power is to the Resistance (when it counterbalances

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lances it) in a Ratio compounded of all the Ratio's, which the Powers in each simple Machine would have to the Resistance, if they were separately apblied. This Rule also obtains in all other Machines.

Not only simple Machines of the same Kind may be joined; but one may compound a Machine of several other Machines in different Manner: This will be plain enough by two Examples.

Experiment 1.] Join the running Rope of the Pullies to the Axle of the Wheel (Plate VI. Fig. 5.) and apply the Power to the Wheel: Now, as in his Case, the Action of the Power becomes five imes greater by Help of these Pullies, and the Diameter of the Axis is but the third Part of the Diameter of the Wheel; the Ratio of the Power to the Weight is compounded of the Ratio's of * 116 1 to *5, and 1 to † 3; it is therefore as 1 to 15; † 113 and therefore one Pound M fustains the Weight P of 15 Pounds.

The Axis in Peritrochio may be moved by a Screw: For this Purpose the Wheel must have Teeth, and those Teeth must stand askew, or be inclined, as you may fee in the Wheel A, (Fig. 9.) which is carried round by the Screw B C. Such a Screw is called an endless Screw, and very much increases the Action of the Power; for there are so many Revolutions of the Screw, or of the Handle of it, required to turn the Wheel once about as the Wheel has Teeth. And if another Wheel with Teeth be added to the first, the Action of the Power will still be much more increased.

Experiment 2. The Machine of Plate VI. Fig. 9. confifts of an endless Screw, which is moved by the Handle DE. Here the Ratio of the Power

to the Weight when it balances it, is compounded of the Ratio of the Semidiameter of the Axis of the last Wheel F, to the Length of the Handle D E, and the Ratio of the Revolutions of that Wheel to the Revolutions of the Handle or Screw. The first Ratio in this Machine is the Ratio of 1 to 30; the second is gathered from the Number of Teeth; the last Wheel F has in its Circumference 35 Teeth, and the Axis of the first Wheel 7; therefore the first Wheel goes round five times, while the second Wheel goes round once: But this first contains 36 Teeth; therefore the Screw goes round so many times, for one Turn of the Wheel*. The Ratio compound-

123 Turn of the Wheel. The Ratio compounded of these two is 1 to 180, which is the second Ratio sought; and the Ratio made up of that and the first (which is 1 to 30) is the Ratio of 1 to 5400, which would be the Ratio of the Power to the Weight, if there was no Friction; but as it is pretty great in all these Engines, the Power must be pretty much increased, to make it raise the Weight; tho' still a very small Power, applied to it, will raise a prodigious Weight. The Handle E D may be twice or three times as long, or still longer, which will double, or triple, or farther increase the Action of the Power: And, in that Case, a small Hair will overcome the Force of the strongest Man.

A great Number of other Compound Machines may be made, whose Forces are in the same Manner determined, by Computation, by the Rule mentioned in the Beginning of this Chapter; or also by comparing the Way gone through by the Power with that gone through by the Weight, or any other Obstacle; for their Ratio will be the inverse Ratio of the Power, and the Weight or

Resistance.

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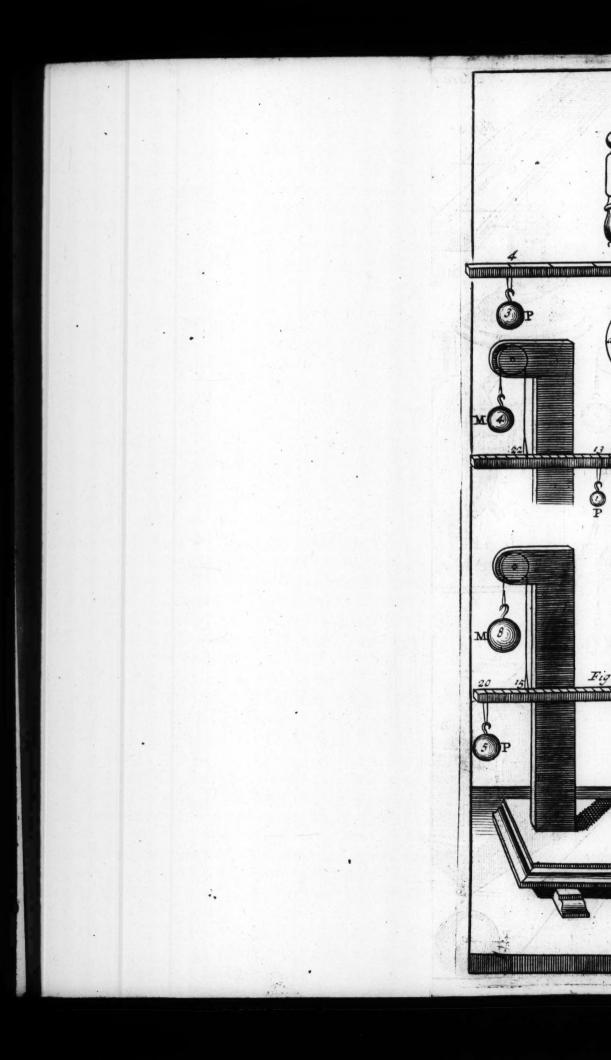
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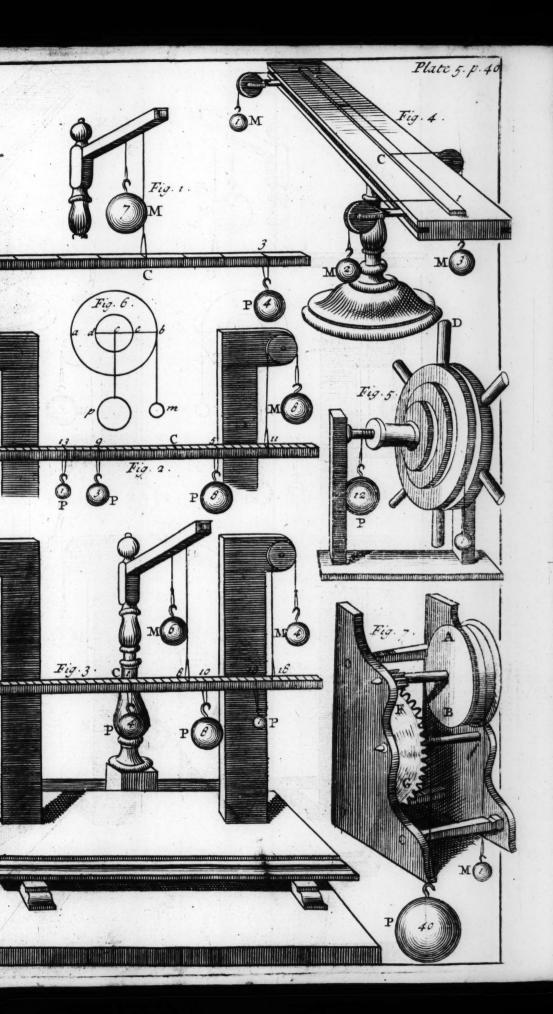
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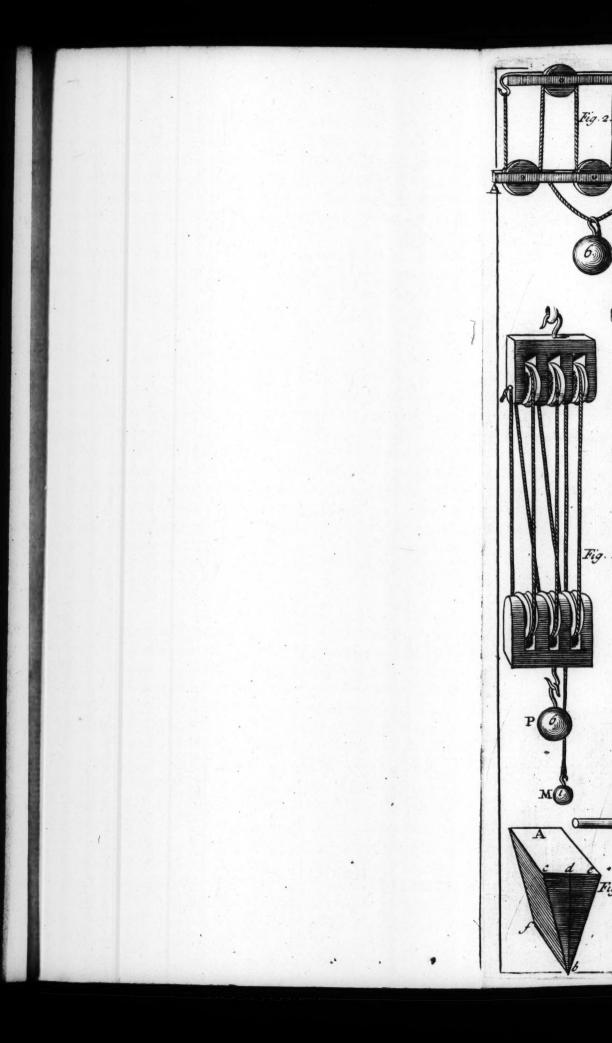
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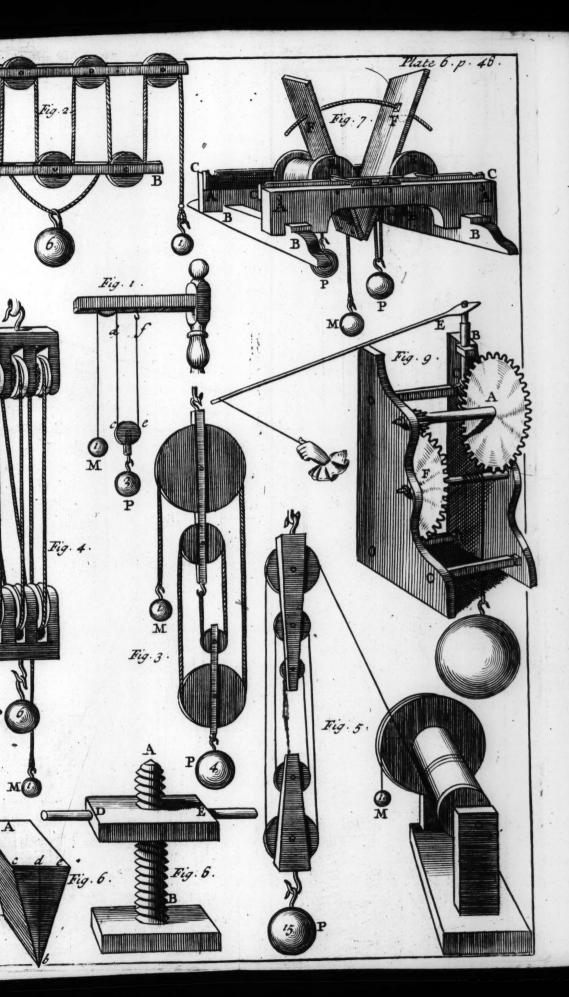
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fon Cha The Forces, which acting contrariwife balance one another, are always equal; if therefore the Intensity of a Power be less than that of the Resistance, it must run thro' a greater Space in the same Time; and that must always be, in Proportion as its Intensity is less; for the Forces can differ in no other Respect, neither can we compensate any other Way for the Difference of Intensity.

CHAP. XVI.

Of Sir Isaac Newton's Laws of Nature.

I N what we have faid of Machines, we have confider'd the Actions of Powers and Weights acting continually against Obstacles and other Resistance; now we shall consider Bodies left to themselves and continuing in Motion, or freely falling: And here we must reason from Phænomena, (as one must do in all Natural Philosophy) and from them deduce the Laws of Nature.

Sir Isaac Newton has laid down Three, by which we think that every Thing that relates to Motion

may be explained.

LAW I.

All Bodies continue in their State of Rest, or Mo-124, tion, uniformly in a right Line, except so much as they arefore'd to change that Stateby Forces impres'd.

We see that Bodies, by their Nature, are inactive and incapable of moving themselves; wherefore unless they be moved by some extrinsical Agent, they must necessarily remain for ever at rest.

A Body also, being once in Motion, continues in Motion according to the same Direction, in the same right Line, and with the same Velocity, as we see by daily Experience; for we never see any Change made in Motion, but from some Cause. But (since Motion is a continual Change of Place) how the Motion in the second Moment

Moment of Time should flow from the Motion in the first, and what should be the Cause of the Continuation of Motion, appears wholly unknown to me; but, as it is a certain Phænomenon, we must look upon it as a Law of Nature.

LAW II.

125 The Change of Motion is always proportionable to the moving Force impress'd, and is always made according to the right Line in which that Force is impress'd.

If to a Body, that is already in Motion, another Force be superadded to move it in the same Direction, the Motion becomes quicker, and that

58 in Proportion to the new Force impress'd. *

When a new Force impress'd is contrary to the Body's Motion, the Retardation follows the Proportion of the Impression; so that a Force which is double or triple, &c. produces a double or triple Retardation. And generally all Forces produce Changes in Motion, according to their Directions and Quantities; other Actions of Forces would imply a Contradiction: This will appear more clearly by such Experiments made upon oblique Forces, as we shall mention in some of the following Chapters.

LAW III.

Action is always equal, and contrary to Re-action; that is, the Actions of two Bodies upon each other are always equal, and in contrary Directions.

Which Way soever one Body acts upon another, we see that Body always suffers an equal and contrary Re-action. If I press a Stone with my Finger, my Finger is equally press'd by the Stone. A Horse, that draws a Cart forward, is as much drawn backward by the Cart; for the Geers or Traces are equally stretched both Ways.

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When a Body strikes against another, whatever the Stroke be, both suffer it equally; but the Impressions are contrary. This is clearly confirmed by the Experiments of the Congress of Bodies.

The Loadstone draws Iron, and is equally drawn by Iron.

Experiment.] Suspend the Loadstone M, (Plate VII. Fig. 2.) in such Manner that it may easily be moved; then, bringing a Piece of Iron within a small Distance of it, the Loadstone will come to the Iron: And if you pull back the Iron, before the Stone be come to it, the Stone will sollow the Iron; just as the Iron goes towards the Stone and sollows it, when then the Iron is suspended and moveable, and the Loadstone brought to the Iron.

When a Man sits in a Boat, and by a Rope pulls towards him another Boat, just as big and as much laden, both Boats will be equally moved and meet in the Middle of the Distance of the Places in which they were at first. If one Boat be greater than the other, or more laden, the Veoci ties in each will be different, when they have different Quantities of Matter; but the Quantities of Motion on both Sides will be equal, abstracting from the Resistance of the Water.

And this Law takes place generally in all the Actions of Bodies upon one another.

CHAP. XVII.

Of the Acceleration and Retardation of heavy Bodies.

DEFINITION I.

A N accelerated Motion is that Motion, whose 127 Velocity becomes greater every Moment.

2

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DEFINITION II.

A retarded Motion is that, whose Velocity is 128 diminished every Moment.

The Force of Gravity acts continually upon all Bodies, in Proportion to their Quantity of Mat-

*79 ter *. When a Body falls freely, the Impression made upon it the first Moment is not destroyed in the fecond Moment; therefore there is superadded to it the Impression made in the second

129 Moment and so on. The Motion then of a Body, that falls freely, is accelerated, and that equally in equal Times; because the Force of Gravity

*75 acts every Moment in the fame Manner *, and therefore communicates an equal Velocity to Bodies in equal Times. Whence that Celerity, which

130 is acquired in the Fall, is always as the Time in which the Body has fallen. For Example: The Velocity acquired in a certain Time will be double, if the Time be double; and triple, if the

Time be triple, &c.

Let that Time be expressed by the Line AB (Plate VII. Fig. 3.) and let the Beginning of the Time be A. In the Triangle ABE, the Lines If, 2g, 3 b, which, being parallel to the Base, are drawn through the Points, 1, 2, 3, are to one another as their Distances from A, A 1, A 2, A 3; that is, as the Times which are expressed by those Distances, and express the Velocities of a Body falling freely after those Times. instead of Mathematical Lines, others be taken with a very small Breadth equal to each of them; the Proportion will not be changed thereby; and those small Surfaces will in the same Manner denote the above-faid Velocities. In the least Time the Velocity may be looked upon as equable, and therefore the Space gone through in each

*53 that Time is proportionable to the Velocity. * In

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each of those small Surfaces above-mentioned, if the Breadth of the Surface be called the Time, the Surface itself will be the Space gone thro'. The whole Time AB consists of those very small Times; and the Area of the Triangle A B E, of the Sum of all those very little Surfaces, anfwering to those small Parts of Times: Therefore that Area expresses the Space gone through in the Time A B. After the same Manner the Area of the Triangle A I f represents the Space gone thro' in the Time A 1; those Triangles are similar, and their Areas are to one another as the Squares of the Sides A B, A 1: That is, the Spaces, gone through from the Beginning of the Fall, 131 are to one another, as the Squares of the Times during which the Body fell.

This is confirmed by Experiments made on the

following Machine.

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The Balance AB (Plate VII. Fig. 4.) which 132 has but one Scale, is exactly in Æquilibrio; when a Weight is put into the Scale, an Iron, made in the Form of a Gnomon, keeps fast the Brachium A, and the Balance is retained in a horizontal Position.

At f there is a thin Spring fg fixed to the Gnomon, and which, when extended, reaches to i, where the End g is retained by Help of the little Plate i, which is made fast to the Brachium A. Now by this means the least Motion of the Balance becomes sensible; because then the Spring fg, being free, flies out, and returns to the Figure fg.

At the End of the Brachium B, there is a Hole, thro' which the String fastened to the Hook D passes freely, that String is kept in a vertical Si-

tuation by hanging on the Weight N.

The Weight M has a Hole thro' it for the above-mentioned String to pass freely thro'; in E 3 making

making Experiments, the Weight M is raised up along the String, and, when you let it go, it falls

upon the same Point of the Brachium B.

Experiment.] Put the one Pound Weight P into the Scale; then the Body M, falling from the Height of three Inches, will move the Balance. When P is a two Pound Weight, let M fall from twelve Inches, and the Balance will be moved. If you lay on three Pounds in the Scale, the Body M must be let fall from a Height of 27 Inches, to move the Balance and raise P. And in all these Cases, if the Height from which M salls be taken but a little less, the Balance with the Weight in the Scale will not be moved.

In this Experiment, the Weight which is laid upon the Scale, and raifed by the Blow of the falling Body, is proportionable to the Stroke; the Quantity of Motion in the Body follows the Proportion of the Stroke: And that Quantity (because we make use of the same Body) is propor-

*63 tionable to the Celerity *; and lastly, the Celeri*130 ty here is proportioned to the Time of the Fall*:

Therefore the Weights above-mentioned follow
the same Proportion of the Time. The Weights
here are as the natural Numbers 1, 2, 3, and
therefore the Times are in that Proportion: But
the Spaces gone thro' in those Times are as 3,
12, 27, or as 1, 4, 9, which Numbers are the

Squares of the others.

Having divided the Time AB (Plate VII. Fig. 3.) into the equal Parts A i, 1 2, 2 3, 3 B, thro' the Divisions draw Lines parallel to the Base; the Spaces gone thro' in those Parts of Time, that is, in the first, second, and third Moment, &c. supposing the Moments equal, are to one another as the Areas A i f, i f g 2, 2 g b 3, 3 b E B; which Areas, as appears by the Figure, are to one another as the odd Numbers 1, 3, 5, 7.

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If the Body, after it has fallen, during the Time A B, should be no more accelerated, but with the Celerity B E, acquired by that Fall, should uniformly continue its Motion, during the equal Time B C, the Space gone thro' by that Motion is express'd by the Area B E D C, which is double the Triangle A B E. And therefore,

A Body falling freely from any Height, with that 134 Velocity which it has acquired by that Fall, will in a Time equal to the Time of the Fall (by an equable Motion) runthro' a Space double the said Height.

Which Proposition we shall also confirm by an Experiment.*

The Motion of a Body thrown upwards is retarded in the same Manner, as the Motion of a falling Body is accelerated by the second Law*: In this Case the Force of Gravity con-*124 spires with the Motion acquired; and in that it acts contrary to it. But, as the Force of Gravity is equal every Moment, the Motion of a Body thrown 135 up is equally diminished or retarded in equal Times.

The same Force of Gravity generates Motion in the falling Body, and destroys it in the rising Body; therefore the same Forces are generated and destroyed in equal Times. A Body thrown up rises till it has lost all its Motion; and so goes up 136 during the same Time, that a Body falling could have acquired a Velocity equal to the Velocity with which the Body is thrown up.

If a Body be thrown up with the same Velocity that it would acquire in falling down the Line B C (Plate VII. Fig. 5.) it would ascend in a Time equal to the Time of the Fall *, (and with an equable Motion) so as to * 136 come up the Height CA, the double of B C*; but * 134 as in the same Time, by the Force of Gravity, the Body goes thro' a Space equal to the Space A B, or B C: as these two Motions obtain here at E 4

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the same Time, and act contrariwise, the lesser must be substracted from the greater; therefore the Body, after the End of the Ascent, will be

137 at P. Whence it follows, that a Body thrown up will rife to the same Height from which, falling, it

138 would acquire the Velocity with which it is thrown up. And therefore, the Heights, which Bodies thrown up with different Velocities can rise to, are to one 131 another as the Squares of those Velocities.*

CHAP. XVIII.

Of the Descent of heavy Bodies upon inclined Planes. a Body through apparais to Holl to

to action of Derinition I. I all beliates

139 W E call an inclined Plane that which makes on oblique Angle with the Horizon.

CB in Plate VII. Fig. 6. represent a Line parallel to the Horizon; A B makes with it the oblique Angle ABC, and reprefents an inclined Plane; and the Perpendicular A C is let fall from A, the upper Part of the Plane, to the Horizon. drefore the fame Perces ato

DEFINITION H.

140 The Length A B is called the Length of the Plane.

DEFINITION III.

141 The Line AC is called the Height of the Plane.

Let two equal Bodies descend by the Force of Gravity from the Point A, the one along the Line A B, and the other along the Line A C; when they are come to the Points B and C, they have descended equally, that is, they will be got each equally near to the Earth's Center: Therefore the Forces with which they are impelled, as they are directed towards the Earth's Center,

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r, re are equal; but the Intensities of equal Forces are reciprocally as the Spaces gone through *; and * 70 therefore here the Intensity of the Force, by which the Body is impelled along an inclined Plane, is to the Intensity of it, by which it is directly impelled towards the Center of the Earth, as AC to AB. Therefore, A Body, laid upon an inclined Plane, loses Part of its Gravity; 142 and the Weight, required to sustain it, is to the Weight of the Body as the Height of the Plane to its Length.

The Plane NOQL (Plate VII. Fig. 7.) is placed 143 in an horizontal Situation; the Plane A B I H moves upon Hinges; and may be fixed at any Height, by Help of the Screw V, and Quadrant t.

The wooden Ruler E F has a Pulley C faflened at one End, and revolves about the other; the Head D, about whose Center this Ruler moves, may be fixed (in any Place of the Slit p s) to the Plane N O Q L, by a Screw under the Plane.

M is a wooden Cylinder, whose Axis is of Steel, and whose Bases somewhat exceed the Cylinder; so that, as it turns round along the Plane A B I H, the Bases only touch the Plane.

The Cylinder is sustained by a String that goes over the Pulley G; which String is fixed to a thin Brass Ruler, bent in such Manner, that the Axes of the Cylinder go thro' its Ends, and turn in them.

In making Experiments, the Pulley is fo plac'd by the inclining Ruler EF, and moving the Head D along the Slit rs; that the String, by which the Cylinder is fustained, is parallel to the inclined Plane ABIH.

Experiment 1.] Let the Plane ABIH be inclined in any Manner, the Weight of the Body M has the same Ratio to the Weight P, as the Length of the Plane AB to its Height AC; and the

the Body M, in what Part foever of the inclined Plane it be fet, will be fustained upon it by the

Weight P.

As the Force, by which a Body is made to defeend along an inclined Plane, arises from Gravity, it is of the same Nature with it; and therefore that Force every Moment, and in all Parts 75 of the Plane, is equal *: For the same Reason

144 the Motion of a Body, freely running down upon n inclined Plane, is of the same Nature with the Motion of a Body freely falling; and what has been faid of the one, may also be affirmed of the other. It is therefore a Motion equably accelera-

129 ted in equal Times; * and therefore the Propositions of Numb. 130, 131, 133, 134, 135, 136, 137, and 138, may be here applied, if we suppose

145 a Motion upon an inclined Flane, instead of a di-

rect Afcent or Descent.

The Forces by which two Bodies descend, one of which falls freely, and the other runs down an inclined Plane, if the said Bodies begin to fall at the same Time, are always to one another in the same

*:29, Ratio as in the Beginning of the Fall *; therefore 144 the Effect of those Forces, that is, the Spaces gone thro' in the same time, are in the same Ratio; name-

142 ly, that of the Length of the Plane to its Height *.

In the Plane A B (Plate VII. Fig. 8.) the Space gone through by a Body, whilst another falls freely down the Height of the Plane A C, is determined by drawing CG perpendicular to AB: for then the Length of the Plane A B is to its Height A C, as A C to AG. If a Circle be described with the Diameter A C, the Point G will be in the Periphery of the Circle; because an Angle in a Semicircle, as AGC, is always a Right Angle; and therefore a Point taken, as G, in any Inclination of the Plane, will always be in the Periphery of the said Circle: Whence it follows, that all the

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Chords, as A G, are gone thro' by Bodies running along them, in the Time that a Body, falling freely, would run down the Diameter A C; and therefore the Times of the Falls thro' those Chords are equal. Thro' the Point C there can be drawn no Chord, as H C, but what a Chord, as A g, may be drawn parallel to it, (that is, equally in-147 clined) and equal; therefore in a Semicircle, as A H C, whether a Body falls freely along the Diameter A C, or whether it falls down along any Chord, as H C, it will in the same Time come to the lowest Point of the Semicircle.

The Time of the Fall along the whole Plane A B may be compared with the Time of the Defect along the Height A C; which for that Time is equal to the Time of the Fall along A G; and so the Squares of those Times are to one another, as A B to A G*. But A B is to A C, as A C* 145 to A G: therefore the Squares of the Lines A B 131 and AC are to one another, as AB to A G; and therefore those Lines A B and A C are to one another, as the Times of the Fall along A B and A G, or AC; that is, the Times in that Case are, as the

Spaces gone throubg.

In the same Case, the Velocities, at the End of the 149 Descent, or equal; for after equal Times, when the Bodies are at G and C, the Velocities are in the same Ratio as in the Beginning of the Fall *, 129 that is, as the Forces by which the Bodies * 142 are impell'd, or as A C to A B *. When the Body descends from G to B, the Velocity increases as the Time; and the Velocity at G is to the Velocity at B, as A C to A B *: therefore the * 148 Velocities at B and C have the same Ratio to the Velocity at G, and so are equal. Hence it appears, that a Body acquires the same Velocity, 150 in falling from a certain Height, whether it falls directly down, or along an inclined Plane; and since

the Angle of Inclination causes no Alteration, a Body may run down several Planes differently inclined, and even along a Curve, (which may be consider'd as made up of an innumerable Number of Planes differently inclined) and the Celerity acquired will always be the same, when the Height is equal.

Experiment 2.] In this Experiment it is to be observed, that a Body hanging by a Thread, and describing a Curve by its Fall, falls in the same Manner, as if it was to run down such a Curve cut hollow in a solid Body without any Friction.

Let the Body P, (Plate VII. Fig. 9.) fuspended by a Thread, fall from the Height A C, in the Curve B C, and in the Curve D C, and in the Curve E F G C, made up of Parts of different Circles, and in each Case it will, with the same Force, strike against the Body Q, which is at rest; and always drives it to the same Height.

A Body that has acquired any Celerity in falling down along any Surface, whether Plane or Curve, will rise up to the same Height along another similar Surface, with the same Velocity, in the same Time.

152 A Body will, with the same Celerity that it has acquired in falling downfrom a certain Height, rise up to the same Height in any Curve whatever.

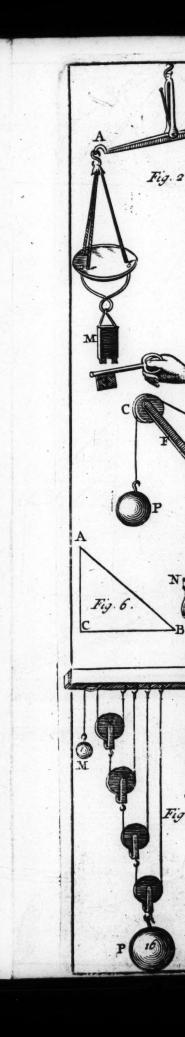
Experiment 3.] Let the Body P, (Plate VIII. Fig. 1.) hanging by a Thread, fall from the Height A C, along any Curve B C: with the Celerity which it has thereby acquired, it will ascend to the same Height on the other Side, in the Curves C D or C E, or C H G F.

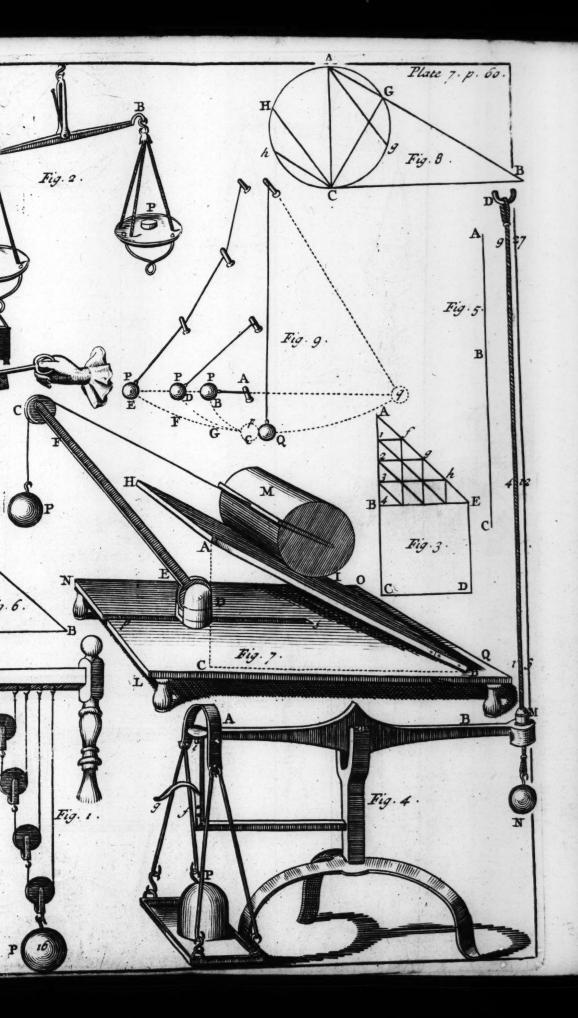
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CHAP. XIX.

Of the Oscillation or Vibration of Pendulums.

DEFINITION.

A heavy Body, hanging by a small Thread and 153 moveable with the Thread about the Point to which the Thread is fix'd, is call'd a Pendulum.

The Motion of a Pendulum is an oscillatory or vibratory Motion. When the Weight, the Thread being extended, is raised upon one Side, it descends by its Gravity, and, with the Celerity that it has acquired, rises up to the same Height on the other Side; * and then it returns *151 by its Gravity, and so continues in its Vibrations.

We here suppose the Motion about the Point of Suspension to be perfectly free, and that there is no Resistance of Air, which is very small in

great Pendulums.

The Body P (Plate VIII. Fig. 2.) does, in its 154 Motion, describe the Arc PBF; if, instead of that Motion, a Body should descend along the Chord PB, and again afcend along the Chord BF, and so should perform its Vibration in Chords; the Descent would be made in that Time in which the Body by its Fall would go thro' the Length of the Diameter AB; * that is, twice *147 the Length of the Pendulum: In an equal Time, it ascends along the Chord BF; * therefore in *151 the Times of one whole Vibration, the Body in falling might run thro' four Diameters; * that is, eight *131 Times the Length of the Pendulum. And as the Descent and Ascent in any Chord is performed in the same Time, all the Vibrations in Chords, whether great or fmall, are likewise performed in the same Time. In small Vibrations, the Arcs

Arcs of a Circle do not sensibly differ from the Chords; and the Vibrations of the same Pendulum, tho' unequal, are performed in the same Time, as far as our Senses can distinguish.

Experiment 1. Plate VIII. Fig. 4.] If the two equal Pendulums, CP and cp, are let fall from the Points P and p in the fame Moment of Time, they will at the fame Time come to B and b, and then to F and f; and fo they will continue their Motion, in the Arcs PBF and pbf, always in the fame Time.

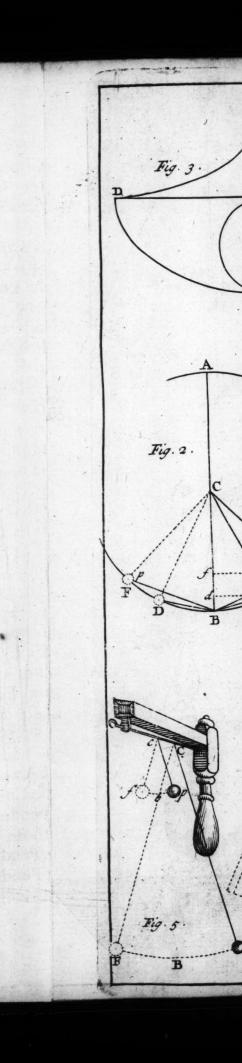
Here it is to be observed, that the Proposition 155 be true in all Pendulums, the Demonstration given is only to be applied to short Pendulums; in the longer Sort the Time of the Descent along a Chord differs sensibly enough from its Descent along an Arc; but in small Arcs the Differences are equal, the Chords be of dif-

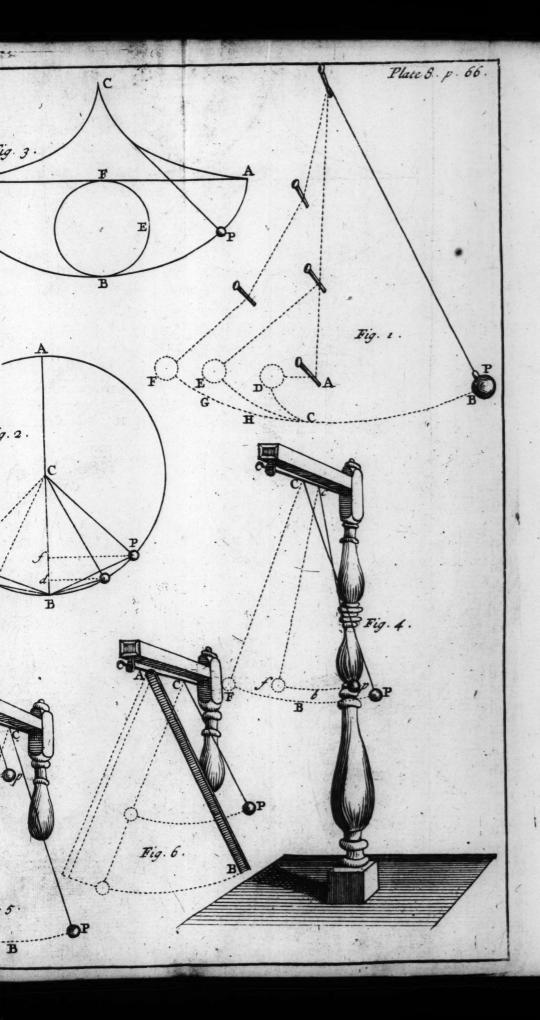
ferent Lengths.

Let the Circle FB (Plate VIII. Fig. 3.) roll along the Line A D, till the Point B comes to A in the same Line; by such a Motion the Point B describes a Portion of the Curve BPA. Such another Curve, BD may be described in the fame Manner, and the whole Curve ABD is call'd a Cycloid. Let it be divided into two equal Parts at B, and let the Parts BA and BD be fo disposed as to have the Points A and D fall in together at C; and let the Point B coincide with the Points A and D in the Line A.D. Let two Plates of Metal be bent according to these Curves, so that the Thread of a Pendulum, fuspended at C, may on either Side apply itself to those Plates, and fall in with their Curves as the Pendulum vibrates. Now if the Length of the Pendulum be CB, the Body P in its Vibrations will describe the Cycloid ABD.

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It is a Property of this Curve, that in what-156 ever Point of it the Body P be placed, the Force, with which it is carried by its Weight along the Curve, is proportional to the Part of the Curve which is between that Point and the lowest Point of the Curve B. Whence it follows, that if two Pendulums, as CP, be let fall in the same Moment from different Heights, the Velocities, with which they begin to fall, are to one another, as the Spaces to be run thro' before they come to B: If therefore they should be acted upon by those Forces alone with a Motion not accelerated, they would come to B at the fame Moment of Time; * after the fame Manner by the Forces *53 which are acquired, the fecond Moment, they also come to B at the same Time: The same may be faid in Relation to the following Moments; and the half Vibrations made up of all the Forces together, however unequal they are, as also the whole Vibrations, are performed in the fame Time.

It is moreover demonstrated by Geometri-157 cians, that the Time of each Vibration is to the Time of a vertical Fall, along the half Length of a Pendulum, as the Periphery of a Circle to its Diameter. In this Curve the lower Part coincides with a fmall Arc of a Circle, as to Senfe: And this is the true Reason, why in a Circle the Times of small Vibrations (however unequal those Vibrations be) are equal; and therefore also the Duration of those Vibrations has the above-mentioned Ratio to the Time of a vertical Fall. The Durations of the Vibrations of un-158 equal Pendulums may be compared together. When the Arcs are fimilar, the Deviations, in Respect of the Chords, are also similar, and the Times of the Vibrations in the Arcs are, as the Times of the Vibrations along the Chords; but they

they are, as the Times of the Descent along Lengths, eight Times greater than the Length of Pendulums; * and fo the Squares of the Durati. ons are as those eightfold Lengths, * or as the Lengths of the Pendulums.

Experiment 2.] Two Pendulums CP, cp, (Plate VIII. Fig. 5.) whose Lengths are as 4 to 1, are let fall at the same Time from the Points P and p, fo that in their Vibrations they describe fimilar Arcs; the longer Pendulum vibrates once, whilst the shortest vibrates twice; and so the Squares of the Durations of the Vibrations are as 4 to 1, namely, as the Lengths of the Pendulums.

When the Vibrations are small, this Ratio alfo holds, tho' the Pendulums should not vibrate in fimilar Arcs. *

*155 159

The Velocities of Pendulums in the lowest Point, when the Vibrations are unequal, are to one another, as the Subtenses of those Arcs, which the Body describes in its Descent. So the Velocity of the Body P, (Plate VIII. Fig. 2.) falling in the Arc P B, is to its Velocity when it falls along DB, as the Chord PB to the Chord DB: For if you draw in a Circle the Lines Pf, D d parallel to the Horizon, the Squares of the faid Chords are to one another, as the Lines fB, dB. The Squares of the faid Velocities are also, as those Lines f B, d B; therefore the Velocities are as the Chords .*

*150 131

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Concerning all that has hitherto been faid of Pendulums, it is to be observed, that it is no 160 Matter how big the Weight of the Pendulum is, or whether the Weights of two Pendulums be different in Magnitude or different Sorts of Bodies; fince Gravity is proportional to the Quantity of Matter in all Bodies, all Bodies in the same Circumstances are moved by Gravity with Book with by th

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with the same Velocity. Which is also confirm'd by the following Experiment.

Experiment 3. Take two equal or unequal Balls, the one of Lead, and the other of Ivory, hang them up by Threads, that they may make Pendula of equal Lengths; let them vibrate, and their equal Vibrations (or even all their unequal ones, provided they be finall Vibrations) are perform'd in the fame Time.

Oftentimes instead of a Thread, a small, but 161 stiff, Iron-Rod is made use of, and sometimes also two or more Weights are fix'd to it, and it is called a Compound Pendulum; in that Case the Rules above mentioned are not applicable; but those Pendulums are reduced to simple ones, by determining in them such a Point, that, if all the Weights were united in it, the Vibrations would be of the same Duration as those of the compound Pendulum. This Point is called the Center of Oscillation.

The Center of Percussion in a compound Pen-162 dulum is a Point, in which the whole Force of the Pendulum is as it were collected; so that if that Point strikes against an Obstacle, the Blow will be greater than if any other Point of the Pendulum should strike against it.

In a Vacuum, or a Medium that does not refift, these two Centers coincide. They also coincide in the Air, as to Sense, by reason of the small Resistance.

A Body of any Figure may be suspended, and vibrate about a Point, or rather an Axis; and in such a Body one may also determine the Center of Oscillation.

When a Right Line, such as is an Iron-Wire, vi- 163 brates about one End, the Center of Oscillation is F distant distant from the Point of Suspension two third Parts of the Length of the Wire.

Experiment 4.] The flat Iron A B (Plate VIII. Fig. 6.) must be so hung up, as to vibrate about the End A; let the simple Pendulum CP, whose Length is equal to two third Parts of A B, be suffered to descend at the same Time as the Iron; and the Vibrations of the Pendulum and the Iron will be perform'd at the same Time.

The Vibrations of Pendulums, as we have faid, tho unequal, are perform'd in the fame Time, and this Property of Pendulums is of great Use in Clocks, to which an equable Motion is com-

municated by fixing on a Pendulum.

By carrying Clocks to different Places, it has appear'd that the Force of Gravity is not equal in all Parts of the Earth, because the Vibrations of the same Pendulum, in divers Countries, have been found unequal, in respect to Time; and that Difference of Gravity is measured by Pendulums.

164 Let there be two Pendulums, whose Lengths are to one another, as the Forces of Gravity by which they are actuated; if they run out into similar Arcs, in correspondent Points, the Forces will always have the same Ratio to one another; and indeed the Ratio of the Spaces to be gone thro, (because similar Arcs are as the Lengths of Pendulums) which therefore will be run thro' in equal 5; Times, * that is, the Vibrations will be perform'd

in the same Time.

If they be reduced to the same Length by changing one Pendulum, the Square of the Time of the Vibration of the Pendulum, that is changed, is to the Square of the Time of the Vibration before the Change (that is, to the Square of the Time of the Vibration of the Pendulum

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dulum that is not changed) as the Length of the Pendulum after the Change to its first Length: * * 158 which Lengths are to one another, as the Force of Gravity in the Pendulum that is not changed, to the Force of Gravity in the Pendulum that is changed. And therefore the Squares of the Times 165 of the Vibrations in equal Pendulums are to one another, inversely, as the Forces of Gravity with which the Pendula are atted upon: which therefore are to one another, directly, as the Squares of the Vibrations perform'd in the same Time.

But whence this Difference of Gravity arises, shall be explain'd hereafter, when we speak of the Figure of the Earth.

CHAP. XX.

Of Percussion, and the Communication of Motion.

Every Body that is at Rest, and hinder'd by no Obstacle, may be push'd forward by any other Body in Motion; and, when once it is put in Motion, it will continue in it, till it is hinder'd by some external Cause. * That Cause is * 124 sometimes a Stroke of another Body against it, or a Stroke which itself gives another Body; or lastly a Stroke of both meeting.

The Laws, to be observed in that Percussion, are

here to be explain'd.

All Bodies, here taken notice of, are supposed spherical; because the Laws of Motion ought to be examin'd in the most simple Case.

DEFINITION I.

A Body is said to impinge directly against ano-166 ther, or two Bodies to strike or impinge against one another, when the Direction of the Motion, or Motions, (if both are moved) goes thro' the Centers of both Bodies.

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DEFINITION II.

lique. When elastic Bodies impinge against one another, the Parts that are struck yield inwards, and, by the Restitution of the Parts, the Bodies repel one another, and are separated from one another.

168 In Bodies that are perfectly soft, or perfectly bard, there is no such Action; and therefore, in a direct Stroke they are not separated after the

169 Blow, because after their meeting, as well as before, they are moved in the same Line; for nothing happens that can change the Direction.

I shall in this Chapter speak of the Percussion of Bodies that are not elastic, and here, as also in the whole following Chapter, I shall speak of direct Percussion; and confirm the Whole by Experiments made with the following Machine.

170 ABC is a vertical Plane of Wood almost triangular, about 4 Foot and a Half high, and 3

Foot wide at the Bottom. Plate IX.

In the upper Part there is a Slit st quite thro' it, which is horizontal, along which two fquare Pins (and fometimes more) are moved; these Pins, having a Shank that goes thro' the Plane, may be made fast in any Part of the Slit by Screws which take the Shanks behind the Plane or flat Board, as may be seen from the Figure of the Pins at V.

A little square Pipe of Iron X slips on upon each Pin, and may be fasten'd to it by a little Screw e, in the upper Part of any Place of the whole Length of the Pin. These little Pipes have Hooks in the under Parts, thro' which small Threads or Fiddle-strings run, and sustain such Balls as P and Q. Those Strings go round the wooden Keys l, l, by turning which, the Balls are rais'd or lower'd.

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The Pin, from which any Ball hangs, is fix'd to such a Part of the Slit st, that its Center is distant from the Line AD (which divides the Machine into two Parts vertically) just one Semidiameter of the Ball; and that is to be done for all the Balls, by means of Marks in the Surface of the Board.

The little Pipe and Hook, from which the Ball hangs, is fix'd to fuch a Part of the Pin, that the Thread hangs but a little farther from the Surface of the Board than a Semidiameter of the Ball: There are Divisions in the Pins, to determine the Place of the Iron Pipes upon the Pins, according to the Bigness of the Balls.

When you use two Balls, the Line A D separates them, and in that Case (as also when several at once are made use of) if they are of different Bigness, the great Ball always determines the Distance of the little Ball from the Board; and the little Pipes are fix'd at such Divisions of the Pins, that the Centers of all the Balls may be equally distant from the Board. The Keys I bring all those Centers to the same Heights; which is to be observed in all the Experiments.

There are two Brass Rulers E G, E G, which slide horrizontally in the Board, whose Surface is hollow'd to receive them, so that their Surface may lie even with it. Behind each Ruler there is a Slit in the Board of about 5 Inches, to transmit a Screw coming from the Backside of the Ruler, which is fix'd behind a Nut in any Part of the Slit. In making Experiments, the End G of each Ruler is distant from the Line A D, one Semidiameter of the Ball, which hangs on the same Side.

These Rulers are so divided as to shew equal Angles, run thro' by the Threads which carry the Balls.

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To measure those Angles in making the Experiments, there are four Indices, two great ones

MM, and two less NN.

These Indices, sliding in a Groove, are moved along the Slits or, or, and are fasten'd behind the Board, where you please, in the same Line by Screws. The longer Indices reach to the Edge of the Board, tho' the Slits want about 3 Inches of it.

The separated Figure M represents the greater Indices, in which a b is a Plate, which slides in the Groove of the Board; c d is the Index, perpendicular to that Plate, and about 3 Inches

long.

The other separated Figure N represents one of the lesser Indices, whose Length is equal to the Semidiameter of the smaller Balls, which are applied to the Machine, and whose Diameter may be about I Inch and a Half: These Indices are put among the great ones, because they don't hinder the Motion of the Balls: Sometimes the two small ones are put in the same Slit, when three Angles are to be measured on one Side.

In that Case the Ball Q is raised up, or rises after its Fall towards the Side of the Board B. That the Index may be placed right for measuring that Angle, the End G of the Ruler E G, which is on the Side B, must be joined with the End G of the other Ruler, placed as above-men-

tioned.

The three Iron Screws FFF serve to set the Machine or Board truly vertical, so as to bring the Line A D perpendicular to the Horizon; which may be easily done by hanging on any one of the Balls, and putting on one of the great Indices; so that the Thread, cutting any Mark on the Index, may hang parallel to the Line A D.

For making Experiments on Bodies that have no Elasticity, you must use Balls of soft Clay, made in the wooden Mould L.

This Mould confifts of five Parts, four of which may be feen at H, H, H, H; thefe, being join'd, contain a fpherical Cavity of an Inch and a Half Diameter, with a Hole in the lower Part: there is a Screw on the Outfide, by which they are press'd together by means of the Ring I, that has a Screw on the Infide.

L represents all the Parts join'd together; there is a Hole in v, which has a Communication with the Infide of the Mould: thro' this Hole must go a Thread, which lies irregularly in the Clay, almost thro' it. Before you put the Clay into the Mould, you must anoint the Inside of it with Oil; then, when all the Parts have been join'd and press'd together by screwing on the Ring, take them afunder again, and you will find a fmooth and round Clay Ball, to the Thread of which you may fasten another Thread, and immediately hang it upon the Machine.

The Experiments, relating to elattick Bodies, are made with Ivory Balls. You must have fix fmall ones, of an Inch and half Diameter. Befides those, one of double the Weight, another of three times the Weight, and a fourth of four times the Weight.

In the 11th Experiment of the following Chapter, the fix equal Balls above-mentioned are hung on to the Machine at the same Time, fo as to touch one another. And this is done (fee Fig. Z) by means of the Plate m n, which is fix'd to the Machine by Help of the Screws q q, which go thro' the Slit st. This Plate contains four Pins, p, p, p, in whose Ends are Holes, thro' which the Threads pass that carry the Balls. The Threads are brought to a pro-

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per Length, and staid by the Keys l, l, l, l. The two other Balls hang from the two Pins V, already described.

To make the 13th Experiment of the next Chapter, there must be three such Pins as V.

In this Machine the Percussion of the Balls, in the lowest Part of it, is always direct; and the Balls (whether you let them go from different Heights, the same Way or contrary Ways) will

and so in that Case the Percussion is always direct; the Celerities at the Bottom are mark'd

in Arcs no greater than fuch as the Balls describe in this Machine, the Ratio between the Arcs and Chords does not sensibly differ. The Heights, from which the Balls are let fall, determine the Celerities before the Stroke; and the Heights, to which the Balls rise, their Celerities after the Stroke.

All, that relates to the Percussion of Bodies not elastic, may be referr'd to the four following Cases.

that is at rest, both together will continue their Mo
* 168 tion in the same Direction as the first Motion; * and

169 the Quantity of Motion, in the two Bodies, will be the

same after the Stroke, as in the single one before it.

For the Action of the Body in Motion, upon the other, communicates to it all the Motion that it acquires; now the Re-action of this last in the first retards its Motion; and as Action and Re-action are equal, * therefore the Quantity of Motion, acquir'd by one Body, is equal to

* 126 ty of Motion, acquir'd by one Body, is equal to the Quantity of Motion lost by the other; and fo the Quantity of Motion is not changed by the Stroke,

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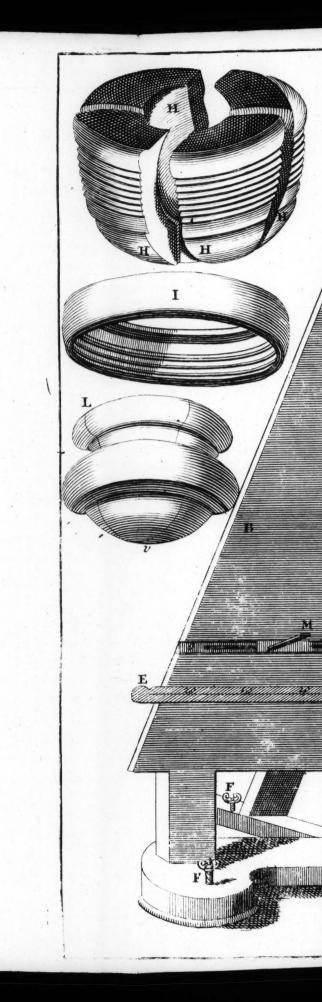
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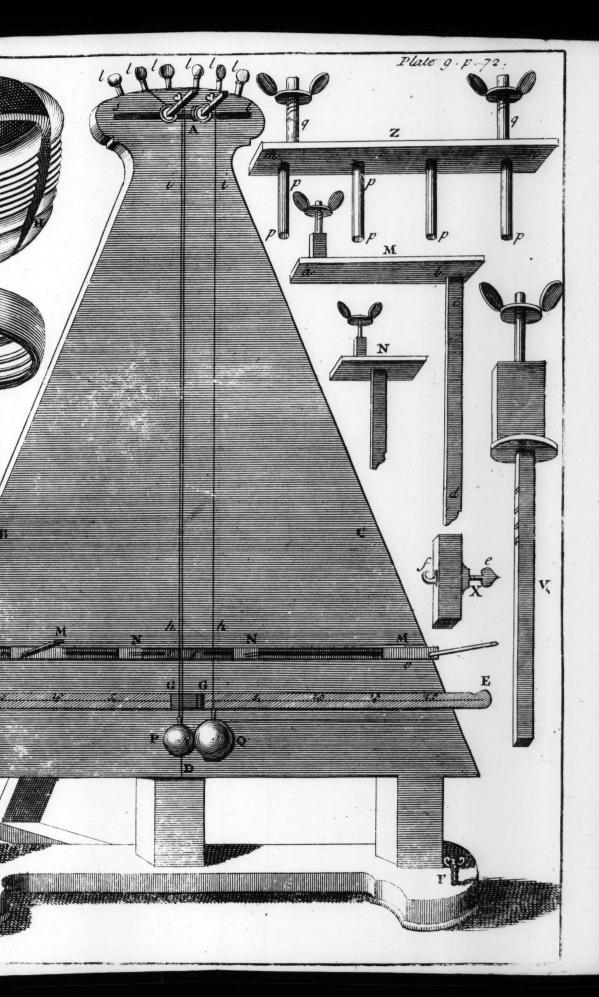
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This Quantity of Motion is found by multiplying the Mass of the first Body by its Velocity; * and dividing that Quantity by the Mass of * 64 both Bodies, you will have the Velocity after the Stroke.

For Example, take two equal Bodies, in each of which the Quantity of Matter may be express'd by One; let the Velocity of the moving Body be Ten, the Quantity of Motion will also be Ten, which must be divided by Two, the Mass of both Bodies, and Five, the Quotient of the Division, will be the Celerity of the Bodies after the Stroke.

Experiment 1. Take the two foft Clay Balls P and Q, and hang them upon the Machine of

Numb. 170. See Plate X. Fig. 1.

Let fall the Ball P from the Height answerable to the tenth Division of the Ruler E G, so that it may strike against the Ball Q, which is at rest; after the Stroke they will both move together, and rife up on the other Side to the fifth Division of the other Ruler E G: The rest of the Experiments in this Chapter are made with the fame Sort of Balls.

Case 2.] If one Body strikes another that moves 172 the same Way, but slower, they will both continue their Motion in the same Direction as before; and the Quantity of Motion, after the Stroke, will be the same as before.

The Reason of this Proposition is the same as

that of the foregoing.

In this Case the Celerity of the Bodies, after the Stroke, is determined by multiplying each Body by its Celerity, the Products of which Multiplications will give the Quantities of Motion in each Body; * by collecting them into one *64. Sum,

Sum, you have the Quantity of the whole Motion; which if you divide by the Mass of both Bodies, the Quotient will be the Celerity required.

Experiment 2.] Take the equal Bodies P and Q (Plate X. Fig. 2.) and let them go towards the fame Side, P with the Velocity 10, and Q with the Velocity 6; as the Mass of each Body is 1, the

* 63 Quantity of Motion in both together will be 16;*
whice if you divide by 2, the Mass of both Bodies, the Quotient will be 8; and the Experiment will shew the Velocity to be answerable to
this.

173 Cafe 3.]- When two Bodies, with equal Quantities of Motion, are carried towards contrary Sides, the whole Motion will be destroyed by their meeting, and the Bodies will be at rest.

The Bodies are not separated after the Stroke, * and the Line in which they move cannot be

in the same Line, it is required that one Motion should overcome the other, which implies a Con-

* 60 tradiction. *

Experiment 3. Plate X. Fig. 3.] Let two equal Bodies P and Q fall from contrary Sides with equal Velocities, and as foon as they meet they will be at rest.

174 Case 4.] Iwo Bodies moved with different Velocities contrariwise, after having struck one another, will both together continue their Motion in the same Direction, towards that Side where there is most Motion; and the Quantity of Motion, after their meeting, is equal to their Difference of Motion before the Stroke.

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The greatest Motion overpowers; therefore the Bodies must be carried together the Way that that Motion is directed; * and a Body, which * that a less Quantity of Motion, is carried in the same Line (but in a contrary Direction) as before the Stroke; for this it is required that, by the Action of one Body, the whole Motion of the other be destroyed, which cannot be done, unless that Body by the Re-action loses an equal Quantity of Motion; there remains therefore only the Difference of the Motions.

Multiplying the Mass of each Body by its Celerity, we have the Quantities of Motion; the least of which must be substracted from the greater to have the Difference of the Motions; which Difference, if it be divided by the Mass of both Bodies, will give the Celerity after the

meeting of the Bodies.

Experiment 4. Plate X. Fig. 4.] Let the Body Q be moved with the Celerity 14, and an equal Body P in a contrary Direction with the Celerity 6; after meeting, the Body Q continues its Motion, and carries along with it the Body P with the Celerity 4.

Because of the Equality of the Bodies, the Quantities of Motion will also be 14 and 6; * * 63 and their Difference is 8; which Number being divided by 2, the Mass of both Bodies, the Quo-

tient 4 will be the Celerity after the Stroke.

DEFINITION III.

We call Relative Celerity, that with which one 175 Body is carried towards another, or with which two Bodies are separated; in Motions directed the same Way, it is the Difference of the Celerities of the Bodies; and, in contrary Motions, it is the Sum of the Celerities.

In

176 In the Congress of Bodies, the Stroke is proportional to that Relative Celerity. For the Force of Bodies, striking against each other, is increased or diminished, according to the Celerity with which two Bodies come towards one another.

CHAP. XXI.

Of the Congress of Elastic Bodies.

A N Elastic Body, whose Figure is changed by any Force, will, when the Action of that Force ceases, by its Elasticity or Spring, re-* 44 turn to its first Figure. *

DEFINITION.

177 A Body has perfect Elasticity, when it returns to its first Figure, with the same Force with which it was press'd in.

178 In that Case, the Stroke, arising from the Restitution of the Spring, is equal to the Stroke by which the Figure of the Body was alter'd.

In this Chapter we suppose this Sort of Elasticity, tho' we know no Bodies persectly elastic: in different Bodies, the Force by which the Parts return to their former Figure is very unequal; for which Reason we can give general Rules only, concerning persect Elasticity; the nearer Bodies approach this Elasticity, the more exactly will their Motion agree with these Rules.

The Experiments, that we shall mention in this Chapter, are to be made with the same Ma170 chine * that the Experiments of the last Chapter were made with; and here we are to use Ivory Balls, such as are mention'd in the Description of the Machine; for the Want of perfect Elasticity, and the Resistance of the Air, do not make a sensible Error in the Experiments; which also, when

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when Necessity requires, may be corrected by determining the Difference arising from it.

Which Way foever two Bodies strike against each other, the mutual Actions of the one against the other are always equal *. By that Action * 126 the Parts of Bodies are puth'd inwards, and that with equal Force in both Bodies; by their Elasticity also they return with equal Force to the The Action of Bodies upon each first Figure. other, from their Restitution by their Spring, is equal to the first Action from the Stroke; * * 178 whence it follows, that the Action of Bodies upon 179 each other is double in elastic ones; that is, double in respect of each Body consider'd singly, because of the Equality of the Action in each. The Change therefore, which in that Case is produced in the Motion of each Body by the Stroke, is double that which the Stroke would by the same Motion produce in Bodies that have no Elasticity; and as, in respect of these Bodies, the Change (both in respect to the Quantity of Motion, and in respect to the Celerity) is determined in the foregoing Chapter; we may also determine what the Change will be in those, that is, in elastic Bodies: In which the following Rules are to be observ'd.

RULE I.

When Bodies that are not elastic strike against 180 each other, if one Body acquires a certain Quantity of Motion, it would require twice as much, if the Bodies were elastic; and this double Quantity is to be added to the first Motion, in order to determine the Motion after the Stroke.

RULE II.

When two Bodies that are not elastic strike against 181 each other, if one Body loses a certain Quantity of Motion, it would lose twice as much, if the Bodies were elastic;

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elastic; and that double Quantity must be substracted from the sirst Motion, in order to determine the Motion after the Stroke.

What is faid of Motion must also be understood of Velocity; because in the same Body the Mo-

* 63 tion is proportionable to the Velocity *:

P, whose Mass is 2, and Celerity 9, strike against Q a Body at rest, whose Mass is 1; after the Stroke Q moves with the Velocity 12, and P continues its Motion with the Velocity 3; which agrees with the former Rules: For if the Bodies were not elastic, the Celerities of both as-

* 171 ter meeting would be 6; * and fo the Body Q would acquire 6 Degrees of Velocity, and by

* 180 Rule I. * therefore it must acquire 12 Degrees; the Body P losing 3 Degrees of Velocity, by the

the former Velocity, there remain 3 Degrees of Velocity.

Experiment 2. Plate X. Fig. 6.] If the Body P whose Mass is 2, and Velocity 8, strikes the Body Q, whose Mass is 1, and which is carried the same Way with the Velocity 5; after the Stroke the Body Q moves with the Velocity 9, and P with the Velocity 6; which again might have been determined by the foregoing Rules.

If the Bodies had not been elastic, both would have moved after the Stroke with the Celerity

* 1727: * the Body Q would acquire 2 Degrees of Celerity, which by Rule I. must be doubled, and added to 5, the first Celerity, which gives us 9: The Body P lost one Degree of Velocity, and by Rule II. it must lose 2, therefore it has 6 left.

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RULE III.

When a Body loses its whole Motion, and acquires 182 a Motion the contrary Way, those two Motions must be collected into one Sum, in order to have the Motion that is lost.

When the Quantity, which is to be substracted by Rule II. exceeds the Quantity of Motion before the Stroke, from which it must be substracted, that whole Quantity of Motion is destroyed, and what remains (that is, its Difference from that which it should have been substracted from) gives the Motion the contrary Way.

Experiment 3. Plate X. Fig. 7.] Let the Body P strike with the Velocity 12 against another Body Q, which is three times as heavy, and at rest, and it will return with the Velocity 6. In this Case, Bodies not elastic would move with the Celerity 3, therefore the Body P would have lost 9 Degrees of Velocity, but by Rule II. * it must * 181 lose 18; which if you substract from the former Velocity 12, you have 6 Degrees the contrary Way by Rule III. * In this Manner may be de-* 182 termined, by the following Experiments, what is laid down in the Rules.

Experiment 4. Plate X. Fig. 8.] Let the Body P be carried with the Velocity 19, the same Way as Q, that is three times as heavy, and move with the Velocity 3; after the Stroke the Body returns with the Velocity 5.

Experiment 5. Plate X. Fig. 9.] Let the two Bodies P and Q come towards one another with equal Quantities of Motion; after the Stroke both will return with the fame Celerities with which they come upon each other,

Exte-

Experiment 6. Plate X. Fig. 10.] Let P with the Velocity 3, and Q of triple the Weight, with the Velocity 11, move in contrary Directions; after the Stroke, Q continues its Motion with the Celerity 3, and P returns with the Celerity 19.

Experiment 7. Plate X. Fig. 11.] Let the same Bodies P and Q be carried in contrary Directions, P with the Celerity 16, and Q with the Celerity 8; both will be reflected after the Stroke, P with 20, and Q with 4 Degrees of Velocity.

All the Cases of the Percussions of elastic Bodies may be determin'd by the Rules above mention'd; the following remarkable Observations are also de-

duced from them.

When the Bodies are equal, and move the same Way, they continue their Motions, interchanging their Velocities; if they move contrariwise, then they are reflected from each other, likewise interchanging their Velocities.

Case 1. Plate XI. Fig. 1.] Let the Bodies move the same Way, and let AB be the Velocity of one Body, and BC the Velocity of the other; the Velocities here are as the Quantities of Mo-

* 63 tion. * Let the Line A C be divided into two equal Parts at D, and let D b be equal to D B; A D or DC gives the Celerity of each Body af-

* 172 ter the Stroke, if they are not elastic; * so the Celerity B C is increased by the Quantity D B, but as it must be doubly increased because of the

* 180 Elasticity, * it will become bC: the Celerity

A B, in Bodies not elastic, is diminished by the

Quantity, D B; but it must be diminished by

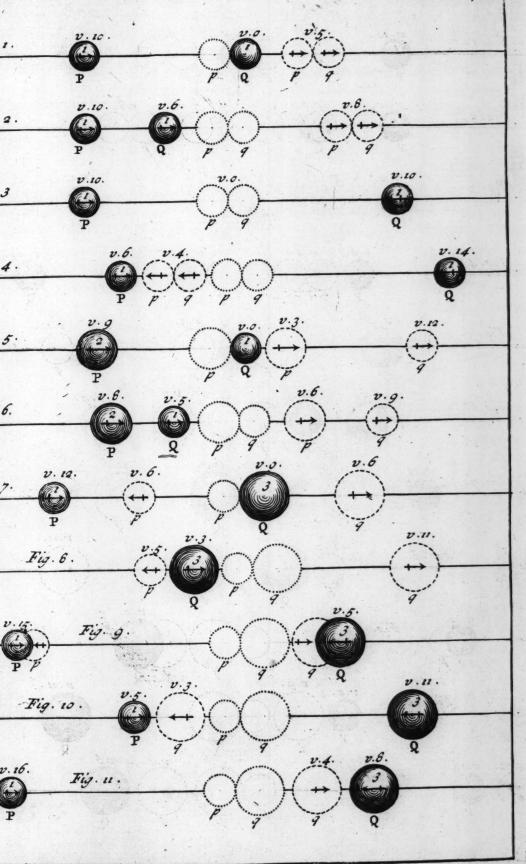
double that Quantity, for the Reason above men-

* 18: tioned; * and therefore it will now become A b.
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Fig. 1. Fig. 2. Fig. 3 Fig. 4. Fig. 5. Fig. 6. Fig. 7. Fig. 10



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Therefore the Velocities AB and BC are changed into the Velocities Ab and bC; but AB and bC, as also BC and Ab, are equal to one another.

Experiment 8.] Let two equal Bodies P and Q3 the first with the Velocity 10, and the other with the Velocity 5, be carried the same Way; they will continue their Motion after the Stroke, interchanging their Velocities: Which also agrees with the Computation by the foregoing Rules.

Case 2. Plate XI. Fig. 2. Let AB be the Celerity of one Body, CB the Celerity of the other; let the Difference A C be divided into two equal Parts at D, and let A b be equal to C B. When the Bodies are not elastic, the Velocity of each of them, after the Stroke towards the same Side, is AD; * therefore the first Body has lost the Velo- *174 city DB, and the other has loft the whole Velocity C B, and acquired D C the contrary Way; therefore the whole Quantity loft is also DB; **182 if this Quantity be doubled, it will be bB, the Quantity of Celerity loft by both Bodies; * the Difference of that Velocity with the Velocity of each Body, does in each Body give a Velocity the contrary Way; * that Difference for the Motion A B is b A, and for the Motion CB is Cb; but Cb and AB, as also bA and CB, are equal to each other.

Experiment 9.] If the equal Bodies P, with the Celerity 10, and Q with the Celerity 5, are carried contrariwife, they will both be reflected after the Stroke, interchanging their Velocities.

When an elastic Body strikes another equal to it 184, that is at rest, that the Velocities may be changed, the percutient Body will be at rest after the Stroke,

and the other will go on with all the Velocity of the Percutient: Which is confirmed by

Experiment 10.] Let the Body P, with the Velocity 10, strike the Body Q which at rest; P will be at rest after the Stroke, and Q will go forward with the Velocity 10. And this serves to explain the following

Experiment 11.] Ist, Let several equal Bodies P, Q, R, S, T, V, (Plate XI. Fig. 3.) be placed in the same Line, and touching one another; if the Body strike against Q with any Velocity, after the Stroke P, Q, R, S, and T, will remain at rest, and V only be moved.

2dly, Let P and Q move with equal Velocities, fo that Q may strike against R; after the Stroke P, Q, R, and S, will be at rest; but T and V

will move forward together.

3dly, If Three are let go together, they will al-

fo strike off Three.

4thly and lastly, If P, Q, R and S be moved at once, so that S strikes T, after the Stroke P and Q will be at rest, and R, S, T, V will move together. In general, let the Numbes of Balls be what it will, how many soever move on before the Stroke, so many also will move off in the same Direction after the Stroke.

In the first Case, the Body P (Plate XI. Fig 3.)
*184 strikes Q, and then is at rest, *Qstrikes R, and is also at rest after the Stroke; and so it happens to the others, till at last T strikes V, which, having no Obstacle to stop it, does alone continue in Motion.

In the second Case, the Body Q (Plate XI. Fig. 4.) does in the same Manner drive forward the Body V; P immediately follows, and strikes Q, which, on account of the first Stroke, was

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at rest, but now communicates its new Motion forward to T, (in the Manner above-mentioned) which is not able to strike V, that is already in Motion; and as the Motions of P and Q are equally fwift, and those Bodies follow one another very close, there is no sensible Time between those two Communications of Motion; which is the Reason that the Bodies V and T are moved equally swift, and not separated from each other.

The relative or respective Velocity, with which 185 two elastic Bodies whatever recede from each other after the Stroke, is the same as the respective Velocity with which the Bodies came against one ano-

If the Bodies were not elastic, they would jointly continue their Motion; * and in that Case, by the Action of the Bodies upon each other, the whole respective Celerity, by which they come to one another, is destroyed; the Action from the Restitution of the Spring is equal and contrary, * and therefore it must generate the *178 fame respective Celerity, with which they recede from each other. Let the Inequality of the Bodies be what it will, nothing is changed thereby, because of the Equality of the first and second Action upon each Body.*

The Quantity of Motion towards the same Side, 186 or the same Way, is the same after as before the

For Bodies that are not elastic, this Proposition is proved in all Cases; *from when the Mo- *171 tions do not conspire, the contrary Motion must 172 be substracted from the Motion one Way, in or- 174 der to determine the Motion that Way. Restitution on account of the Elasticity, equal Quantities are generated towards each Side, * *129 by which the Quantity of Motion towards one Side is not changed. These two last Propositions

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are fully confirmed by the above-mentioned Ex-

periments.

When a small Bodystrikes against another greater Body, which is at rest, the great Body acquires a greater Quantity of Motion than the small one had before the Stroke.

The Quantity of Motion, acquired by the great Body, is double the Quantity which the little one would lofe, if the Bodies had no Elasticity; but in that Case, the little Body would lose more

*180 than Half its Motion *.

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Experiment 12. Plate XI. Fig. 7.] Let the Body P, with the Velocity 15, (which Number alfo does here express the Quantity of Motion) strike the Body Q, which weighs four Times as much, and is at rest; the Body Q acquires the

*171 Velocity 6; * that is, 24 Degrees of Motion.

150 But the Body P returns with 9 Degrees of Velocity; and fo the Quantity of Motion, towards that

Way where P was first directed, continues to be

*186 15. *

The Motion is more increased in the Body Q, by the Interposition of a Body of mean Bigness between the Bodies P and Q.

the two Bodies P and Q before-mentioned, and between them the Body R double the Body P; if the Body P, with 18 Degrees of Velocity, comes upon R which is at rest, it will communicate to it

171 12 Degrees of Velocity; * with which if this Body
180 strikes upon Q that is at rest, it will communicate to it the Celerity 8, that is 32 Degrees of
180 Motion; but in this Experiment, because of the
180 double Percussion, the Error, arising from the
180 Want of perfect Elasticity, is more sensible than
181 in the others, where there is but one Percussion,

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and so the Quantity of Motion, acquired by the Body Q, is about 30.

The greater the Number is of unequal Bodies, 189 which are interposed between two Bodies, if the Masses always increase from the first to the last, so much the greater will the Quantity of Motion be in the greatest; and it will be the greatest of all (the Number of Bodies interposed remaining the same) when the Masses of all the Bodies increase in a Geome-

Tho' the Quantity of Motion, directed the fame Way in the Congress of Bodies, whether elastic or not elastic, remains the same, the Quantity of the Motion itself does not always remain the same, but is often diminish'd, * and also often increased; * so that there is no Reason to say, * that there is always the same Quantity of Motion in the World.

CHAP. XXII.

Of compound Motion, and oblique Percussion.

A Body in Motion may be acted upon by a new Force, and driven according to another Direction, in that Case the Change of Motion follows the Proportion and Direction of that Force: * And as the first Motion is not destroy'd * 125 by that Action, from these two Motions a third arises, according to a new Direction.

Let the Body P (Plate XI. Fig. 9.) be driven 190 by any Force, according to the Direction PC, and at the same time let it be driven by another Force, according to the Direction PB; and let the Celerities, arising from those Forces, be as those Lines PC, PB. In order to determine what will happen, let the Parallelogram PB AC be compleated, by drawing the Lines BA, CA, parallel to the Lines above-mention'd; let PA be the Diagonal of G3 that

that Parallelogram. Let the Body be supposed by the first Force, that is, with the Celerity PC. to describe the Line P C, and let that whole Line be carried along in the Direction, and with the Celerity P B; when that Line is come to b a, the Body will be at p, fo that P b will be to P B, as b p to b a, or A B, that is, it will be in the Dia. gonal PA, and fo always. When the Line PC is at B A, the Body will be at A; therefore from a Motion compounded of the two Motions above. mentioned, there arises a Motion along the Diago. nal PA, whose Celerity is proportional to the Length * 53 of the Diagonal; * for the Diagonal will be run thro' in the fame Time by the Body P with 1 compound Motion, as the Line P B or PC would have been gone thro' by the same Body, by only one Motion; that is, acted upon by one of the

To confirm this Proposition experimentally, we must make use of the following Machine.

CDE, CDE, (Plate XII. Fig. 1.) of the Figure of a right-angled Triangle, whose Side CD is in Length about 3 Foot and a half, and the Side DE about 1 Foot and a half; these Boards are fixed so to move in a vertical Situation about the

Hinges A and B.

The Experiments upon this Machine are made with Ivory Balls of an Inch and a half Diameter. The Planes are so join'd, that if you conceive two other Planes to run parallel to them, at the Distance of a little more than a Semidiameter of the Balls; the Lines, in which these imaginary Planes intersect, shall be the Axis of their Circumvolution: Which is brought to pass by the Contrivance of the Hinges, (Fig. 2.) whose Pares b, b, are let into the Wood to be the firmer. In the Center of the upper Hinge A, there

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there is a fmall Cylinder a, (Fig. 2.) in whose Case there is a Hole, which meets another in the Side, thro' which the Thread ib is to run; at one End of this Thread a Ball, as P hangs, and the other End is join'd to the Key l. By Help of the Screws F, F, F, F, F, this Machine is set perpendicular; so as to have the Thread b i hang in the Axis of the Machine.

At m, m, there are two Pins fix'd to the two Planes, from which Pins the Balls Q, Q, hang, at fuch a Distance from the Planes, that they may almost touch them; so that if you suppose a Line to pass thro' the Centers of the Balls P and Q, it shall be parallel to the Plane on that Side: besides, it is required, that, when those Balls hang at the same Height, they shall touch one another.

The Threads which are tied to the Balls go thro' the Holes in the said Pins, and are fix'd to the Keys 11, so that the Balls may be raised or let down easily, and have all their Centers brought to the same Horizontal Plane. There is a Brass Ruler, or graduated Limb R, bent up in an Arc of a Circle, so as to have the Ball P rise along it in its Motion; and this Limb turns one of its Ends on a Center, which is in the Axis of the Machine. This Piece of Brass serves to shew to what a Height the Ball P ascends.

Each Ball Q, when it swings, moves along the Plane to which it is applied; and the Height, from which it is made to fall, is shewn by an Index fixed to the Plane; to which End there are four Holes in each Plane, containing equal Angles, in respect to the Motion of the Threads.

When the Ball Q is let fall from any Height, it strikes upon the Ball P, and drives it to the same Height in the same Direction.*

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Experiment 1.] The Horizontal Section of this Machine is here represented, (Plate XII. Fig. 3. and 4.) the Body P may be driven by either of the Bodies Q, with any Direction and Velocity. If the Bodies Q and Q are let fall at the same time, the Body P has two Motions impress'd upon it at the same time, * and therefore runs in the Discrepance of the Berellelegreen made in the

agonal P p of the Parallelogram made in the Manner above-mentioned, * to express those two Motions, and runs up to an Height proportionable

to the Length of that Diagonal.

The Experiment answers very exactly, whether the Balls Q and Q are let fall from the same Height, or from unequal Heights, and whatever the Angle be that is made by the two Planes, that is, by the Directions of the Motions, whether the Angle be right, acute, or obtuse.

PA, (Plate XI. Fig. 10.) may always be consider'd as afted upon by two Motions: and that as many Ways as you please; for you may draw as many different Parallelograms as you please, as PB AC, pb ac, pb ac, whose Diagonal is the Line above-mentioned; and, in every one of them, if there be supposed two Forces acting in the Directions PB and PC, from which the Celerities, which the Body would have, are as the Sides PB and PC, a Motion will always be produced by the Action of them both at once, which will give a Celerity proportional to the Diagonal.

From this Refolution of Motion into two other Motions, may be determined the Motion of Bo-

dies that strike one another obliquely.

Let Q (Plate XI. Fig. 11, and 12.) be at rest, and P with the Direction and Celerity P A, strike against it. When P is come to A, draw thro' the Centers of both Bodies the Line D B,

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and then PB perpendicular to it, and compleat the Parallelogram ABPC, the Motion along PA is resolved into two others along PB and PC, or BA, CA: By the Motion in the Direction CA, the Body P does not act upon the Body Q; the Action therefore arises solely from the Motion in the Direction along BA, that is, the Body P, by the oblique Stroke along PA with the Celerity PA, acts upon the Body Q, in the same 193 Manner, as if it should strike it directly along BA with the Celerity BA. And so the Motion of the Body Q from that Action, whether the Bodies be elastic or not, is determined from what has been said of direct Percussion.

The Motion of the Body P(Plate XI. Fig. 11, and 12.) after the Stroke, is deduced from the fame Principle; the Motion along C A is not changed; therefore by that Motion, with an equal Celerity, the Body P is carried in the Direction A E. Now let A E be equal to C A; the Change in the Motion B A is determined, in respect of the Body P, in the same Manner as the Motion of Q, by the two foregoing Chapters; let the Celerity of that Motion be AD, in Fig. 11. when the Body goes forward, and in Fig. 12. when it returns back; from that Motion, and the Motion along A E, arifes a compound Motion in the Diagonal Ap, which, by its Situation and Length, denotes the Direction and Celerity of the Body P after the Stroke.*

When Bodies are equal and elastic, the whole 194 Motion along B A is destroyed by the Percussion,* and only the Motion along C A is left, and the Body P also is carried in that Direction. In * 184 that Case, both the Bodies do always fly from each other in Directions that are at Right Angles with one another, which Way soever the Body P comes upen the other Body.

Expe-

Experiment 2. Plate XII. Fig. 5.] In the Machine described Numb. 191. let the Ball Q and P hang; having set the Planes at Right Angles, let the Body Q with any Direction, and from any Height, come down upon P, and strike against it: after the Stroke the Bodies will follow the Directions of the Planes, and rise to Heights, which may be determined by what has been said 195 hitherto.

We may also thesame Way determine the Motion of two Bodies after the Stroke, when both Bodies are moved, which Way soever they come upon one another. The chief Cases are represented in *Plate* XIII. and all them are explained

exactly the fame Way.

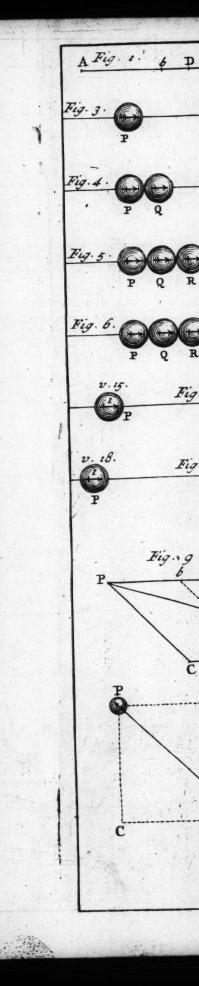
Plate XIII. Fig. 1, 2, 3, 4, 5, and 6.] Let the Body P be moved with the Direction and Celerity P A, and the Body Q, with the Direction and Celerity Qa; draw the Line Bb, which goes thro' the Centers of both Bodies where they touch one another, and let C A and ca be drawn perpendicular to the Line above-mentioned, and let the Parallelograms PB AC and Q b a c be compleated. The Motion of P is refolved into two others, of which the Celerities and Directions are express'd by C A, B A. The Motions, into which the Motion of Q is refolved, are express'd by ca, ba; by the Motions along C A and c a the Bodies do not act upon one another; therefore these Motions are not changed, and after the Stroke are express'd by A E and a e, which are equal to A C and a c; the Percussion, from the Motions in the Lines B A b a, is direct, and determined in the foregoing Chapters: Let the Body P move towards D, and its Celerity be A D, and the Body Q move towards d with the Celerity ad. After the Stroke therefore, the Motion

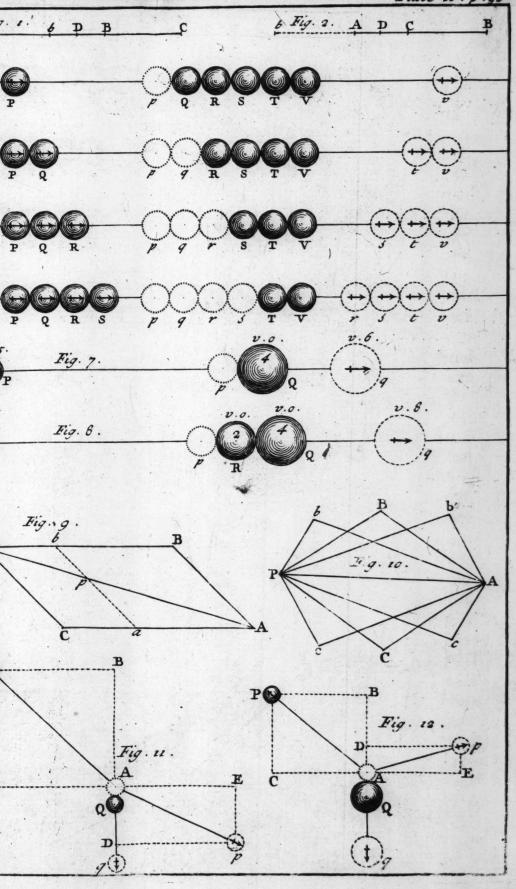
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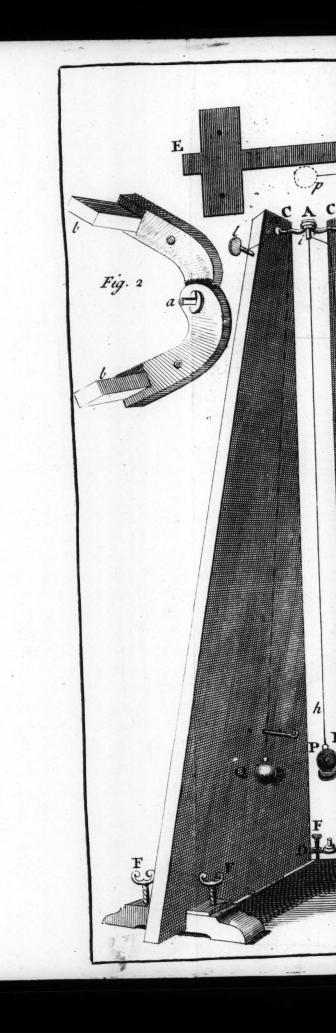
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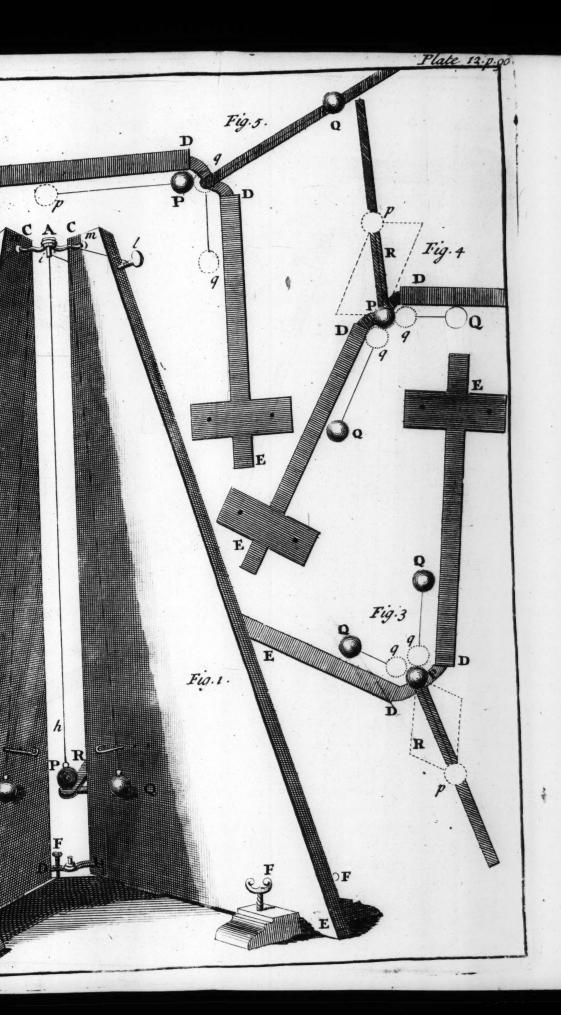
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Motion of the Body P is compounded of the Motions along AE and AD, and moved in the Diagonal A p. The Motion of the Body Q, after the Stroke, is compounded of the Motions along a c and a d, whence that Body is carried in the Diagonal ae; and the Lengths of those Diagonals express the Celerities of the Bodies after their Meeting. In the 1st, 2d, and 3d Figures the Bodies are supposed not elastic; and in the 4th, 5th, and 6th, the same Bases are put, supposing the Bodies elastic. There are some Letters wanting in the first Figure, because the Points, which are marked with those Letters in the other Figures, do here coincide with other Points, and are not necessary for determining the Motions.

CHAP. XXIII.

Of Oblique Powers.

HE Body P(Plate XIII. Fig. 7.) being driven in the Directions P B and P C, with Celerities proportionable to those Lines; from thence arises a Motion along P, the Diagonal of the Parallelogram P B A C, with a Celerity that is denoted by that Diagonal *; if there be a third Force acting along the Line P a, fo that the Celerity arising from it be P A; by that Action the Actions of both the faid Forces are destroyed, and the Body comes to rest: If the aforesaid Actions continue, the Body will continue at rest; which happens when the Body is drawn towards C, B and a, with the faid Forces pulling by Threads. Whence it follows, That a Body will be 196 at rest, which is drawn by three Powers, that are to one another, as the Sides of a Triangle made by Lines parallel to the Directions of the Powers. This

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by the Machine represented in Plate XIII. Fig. 8. It consists of a round Board of about 8 Inches Diameter, which is in a horizontal Position, and sustain'd by a Foot: Round the Edge of it, within the Thickness of the Wood, is a Groove whereby Pullies are applied at Pleasure to any Part of the Circumference; for each Pulley has a Brass Plate perpendicular to it, which fits into the Groove, when the Pulley is applied. See the Pulley with the Plate represented by F.

The Board above-mention'd is a little hollowed in, in the upper Part, so as to receive a less orbicular Board D F A, whose Thickness is about a Quarter of an Inch, and its Surface rises a little above the first Board; so that a Thread that runs over any of the Pullies, being extended horizon-

tally, may just touch the faid Surface.

You must have several of the lesser round Boards, for making different Experiments. They have Paper pasted upon them on both Sides, that the Lines (to be mentioned hereafter) may be the more easily drawn upon them.

Experiment 1. Let C be the Center of the fmall Board, and let there be drawn upon it the Triangle A B C, whose Sides are to one another as 2, 3, and 4: Let C E be parallel to the Side A B of the Triangle, and let the Side A C be continued towards D.

Now if there be three Threads joined together at C, and stretched over the Pullies sastened to the greater Board, so as to be in the Lines CD, CE, and CB; if to the Thread CD you hang 4 Pounds, to CE 3; and, lastly, but 2 to the Thread CF, the Threads will not be mov'd, and the Knot remains over C; but, if it be mov'd out of that Point, it will not be at rest.

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In this Proposition any two Powers are balanced by a third, that is, act but as one; which acts contrariwise in the Direction of that third. Therefore the Actions of two Powers may be re-198 duced to the Action of one.

So, when a Point is drawn by four Powers, there will be an Æquilibrium, if reducing two Powers to one, this new Power, with the other two remaining, be in the Position of Numb. 196; that is, if those remaining Powers being also reduced to one, the Power arising thence be equal with, and acts contrary to the new Power mentioned.

Experiment 2. Plate XIII. Fig. 9. The Point 190 C is drawn by four Threads; towards B by the Weight of I Pound, towards F by 3 Pounds, towards E by 2 Pounds; and, lastly, towards D by 4 Pounds; and this produces an Æquilibrium. Having drawn the Triangle CFa, or the Parallelogram CF a E, the abovefaid Powers, drawing in CF and CE, are reduced to one that acts in the Direction Ca, with the Force of 4 Pounds; and then the three Powers, drawing in the Lines CB, CD, Ca, give us the Cafe of Numb. 196: And therefore if the Powers, drawing along CB and CD, be reduced to one drawing along CA, it will act in the fame Direction, but pull against the Power pulling in Ca, and be equal to it.

What is here faid of the four Powers, might be faid of five or more; for of five, if two be reduced to one, we come to the last mentioned Case.

Experiment 3. Plate XIV. Fig. 1.] The Point 200 C is drawn by 5 Powers, pulling by the Threads CA, CB, CD, CE, and CF; the Powers

are

are to one another as the Weight by which the Threads are drawn, and they have the same Proportion to one another as the Numbers that you see at the Pullies in the Figure, and you have an Æquilibrium.

The Powers, drawing in CB and CD, are re-

duced to one drawing in CG.

The Powers, drawing in CE and CF, may be reduced to one acting in CH; which brings us to the Case of Numb. 196. Lastly, those two newPowers, drawing in CH and CG, are reduced to one acting in Ca, which are equal to the fifth drawing along CA, and pulls in the same Line, but contrariwise.

- Besides this, we deduce from the Proposition mentioned Numb. 169, that the same Thing may be said of the Action of the Power, which has been said concerning Motion in the foregoing Chap-
- *192 ter; * namely, that it may be resolved into the Actions of two other Powers, and that in numberless Manners, because Triangles of numberless Kinds may be made, tho' you keep one Side still the same. Thus in all Engines we can reduce a Power, that acts obliquely, to a direct one; and can determine the Proportion between a direct and an oblique one: Which will appear by the following Examples, that are confirmed by Experiments.
- Lever A B, whose Brachia are equal, apply at B the Weight P of two Pounds, and at A a Power acting obliquely in the Direction A D, and which is represented by the Weight M. If you imagine a Line, as D E, parallel to the Lever in a horizontal Position, and A E perpendicular to that Lever; and if A D be to A E as 3 to 2, and

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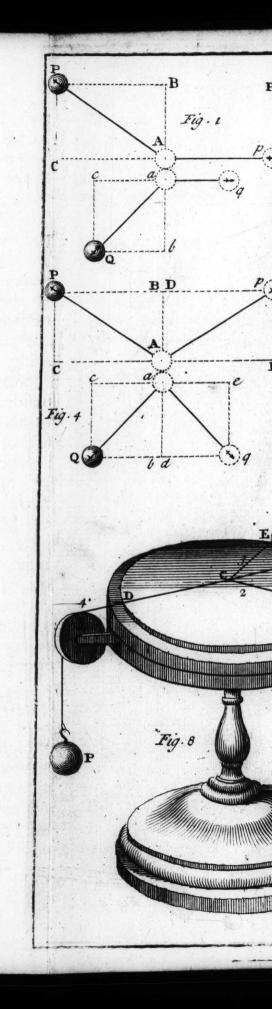
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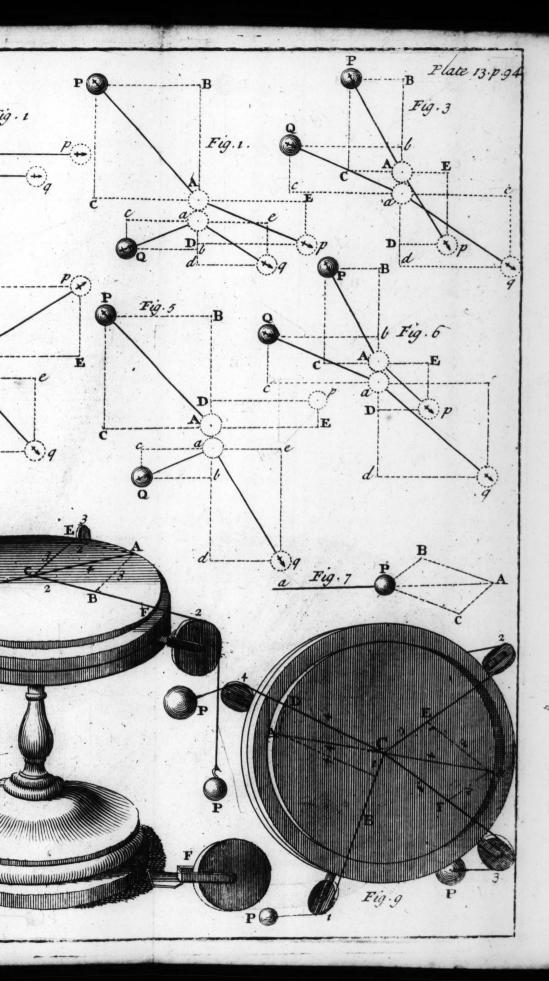
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the Weight M be of three Pounds, there will be an Æquilibrium.

The Direction of the Motion of the Point A, by the Motion of the Lever, is perpendicular to the Lever, therefore it acts in the Line E A produced. As the Distance B A always remains the same, in the second Figure A is hindered from coming towards B, and as it were repelled in the Direction B A; in Fig. 3. the Point A is hindered from receding from B, and so A is as it were drawn towards B. Besides, the Point A is by M drawn towards D; therefore that Point is drawn by three Powers, whose Directions are parallel to the Sides of the Triangle A E D; which therefore, to produce an Æquilibrium, must be to one another as those Sides.

The Point A, by reason of the Equality of the Distances of the Points A and B from the Fulcrum, moving along E A, is drawn with the same Force as P descends, that is, with the Force of two Pounds; the Force therefore along A D must be of three Pounds, because the Sides A D and A E are to one another as 3 to 2. The Side D E expresses what the Fulcrum sustains by the Force with which the Point A in Fig. 2. is pushed towards B, or is drawn from it in Fig. 3.

The fame also may be faid of an oblique Power to the Axis in Peritrochio.

Properiment 5. Plate XIV. Fig. 4. Let the Weight 203 P, fixed to a Pulley, be sustained by Powers applied on both Sides to the running Rope, but drawing obliquely in the Directions CA and CB; these Powers are equal to one another, because no Part of the Rope, that goes about the Pulley, can be at rest, unless it be equally drawn on both Sides. * The Weight P is as it were a *33

third Power, and so the Point C is drawn by three Powers; suppose the Line C E perpendicular to the Horizon, and the Line A E parallel to CB: If CE be to A E or A C (for these two Lines are equal, because of the above-mentioned Equality of the Powers drawing along CB, CA;*) as 6 to 5, the Weight P of 6 Pounds

will be fustained by the Weight P of 6 Pounds will be fustained by the Weight Q and Q of 5 Pounds each; the Reason of which is evident by Prop. 196.

If one End of the running Rope is fastened to a Pin, the Weight P will be sustained by only one

of the Weights Q.

P be not joined to the Pulley, but sustained by the Rope CA and CB sastened to it, it may be sustained by two unequal Powers. Draw the Triangle CAE, as was done in the foregoing Experiments, and let AE be 11, and CA 12; and CE 12; you shall have an Æquilibrium, if the Weights Q and Q are to P, as the first Numbers to the last; the Reason of which Experiment

is also evident from Numb. 196.

205 Here we are to observe, that from the given Inclinations of the Threads C A and C B to the Horizon, the Proportion of the Weight Q and Q to the Weight P may be determined by Trigonometrical Tables. If in the Triangle ACE you conceive a Line A e drawn thro' the Point A parallel to the Horizon, and that Line be taken for a Radius of a Circle, CA will be the Secant, and e C the Tangent of the Angle which CA makes with the Horizon, and AE will be the Secant, and e E the Tangent of the Angle of Inclination of the Thread CB to the Horizon: Whence it appears that the Weights Q, Q are proportional to the faid Secants, and that the Weight

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Weight P follows the Proportion of the Sum of the aforesaid Tangents.

On the Machine with which these last Experiments are made, (the Make of which the Figure alone sufficiently expresses, especially if it be compared with the 4th Fig. of Plate IV.) draw Lines along which the Threads that go over the Pullies may be stretched; in the Middle of the Lines write down the Numbers, which express the Secants of the Angles which those Lines make with the Horizon; and, at the Ends of the Lines, write down the Numbers expressing the Tangents of these Angles.

Now in every Case where there is an Æquilibrium, the Weights Q and Q are as the Numbers in the Middle of the Lines along which the Threads are stretched; and the Weight P as the Sum of the Numbers at the Ends of those two Lines.

periment 7. Plate XIV. Fig. 6.] For this Ex-206 periment we must make use of the Machine of Numb. 143. Plate VII. Fig 7. The Body M, being laid upon an inclined Plane A B, is sustained by a Power drawing along MS; let MR be a Line perpendicular to the Horizon, and ASR perpendicular to the Surface of the Plane; in every Case where the Weight P is to the Weight of the Body M, as MS to MR, the Body will be at rest.

The Body M by its own Weight is drawn in the Directions R M, by the inclined Plane it is fustained in a Direction perpendicular to the Plane, and so that Experiment is reduced to the Proposition of Numb. 196.

Experiment 8. Plate XIV. Fig. 7.] The Brachia 207 of the Lever ACB are equal, and form such an Angle

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Angle, that if A C be continued towards D, and BD be drawn perpendicular to CD, DC shall be the Half of BC or CA. At A hang one Pound p, and at B the two Pound Weight P; then fetting the Brachium C A in a horizontal Position, you will have an Æquilibrium; * because the

Weight P hangs, as it would do upon a streight

Lever hanging at the Point D.

Change the Weights, and let the greater hang at A, and the leffer be laid upon the Brachium BC at B; (Plate XIV. Fig. 8.) if by a vertical Plane you hinder this last Weight from falling

off, you will again have an Æquilibrium.

The Brachia of the Lever are equal, and by the Motion of the Lever move equally; therefore, by the Force of the Weight P, the Weight p is as it were drawn towards E, in the Direction perpendicular to the Brachium BC; by the Action of the vertical Plane, that Weight is push'd horizontally; and at last is push'd vertically by the Force of Gravity. Therefore the Weight p is drawn by three Powers, which are to one another as the Sides of the Triangle B E D. * Therefore the Force tending towards the Earth, (that is, the Weight p to the Force drawing towards E, namely, the Weight P) is as BD to BE, or DC to CB or CA; that is, as I to 2. Which is also the Ratio between the Weights p and P. And here therefore the Reason of the Experiment is deduced from the often mentioned Proposition of Numb. 196; to which all other Cases imaginable, relating to oblique Powers, also belong.

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CHAP. XXIV.

Of the Projection of heavy Bodies.

Body, moved by two Impressions, has a 208 Motion compounded of both; * if a Body * 190 be projected, or thrown in the Line AB, (Plate XV Fig. 1.) in the Time in which it could run the Length AB, it is by the Force of Gravity carried towards the Center of the Earth the Length BF, and fo, by a Motion compounded of both, it is moved in AF; and by that Motion the fecond Moment it would run through FC, equal to AF, if that fecond Moment it was not by the Force of Gravity carried in CG, fo that the Motion in the fecond Moment is in FG: After the same Manner, the Motion in the third Moment is in GH, and the fourth Moment in HI; but as Gravity acts continually, those Moments of Time are to be look'd upon as infinitely finall, and fo you will every where have a Motion compounded in different Directions; that is, an Inflection of Direction in the Body's Motion; in that Case therefore it will move in a Curve Line.

This Motion of a projected Body, or Projectile, 209
may be consider'd more simply in all Projections
which we make; because all Lines, which tend towards the Center of the Earth, may be look'd
upon as parallel, and the Direction from that
Motion is always the same; when the projectile
Motion is made up of two Motions, the first equable in the Line of the Projection, and the second
accelerated towards the Earth. *

Let a Body be projected in the Line A D, parallel to the Horizon; in equal Times, by that H 2 Motion

Motion, it will run thro' the equal Spaces A B, B C, C D: By Gravity it will, in a Motion perpendicular to the Horizon, be carried in the Direction B F, C G, or D H, which here are supposed parallel; this Motion is accelerated, and therefore if after the first Moment the Body be at the Point F, after the second it will be at G, after the third at H; so that if you call BF one, C G will be four, and D H nine. * The Body will run in a Curve, which goes through all the Points that may be determined in the same Manner as F, G, H, and that Line is called a Parabola.

The Machine made use of, for proving this Proportion experimentally, is made of three Parts, as may be seen in *Plate* XV. Fig. 3. A b is 6 Inches high, DE is exactly of the same Height: The Length bH is of 12 Inches, supposing the Point H to be distant 1 Inch from the End of the Cavity in which it is taken.

Let E A be hollowed circularly; or in any other Curve; and let this hollow Channel be overlaid with a Plate of very smooth Tin or Brass, that a Brass Ball may freely roll down it; but Care must be taken that the lower Part of the Curve, at A, shall have a horizontal Direction, that the Ball may quit it in that Direction.

Ab must be divided into 9 equal Parts, of

which Af is 1, and Ag contains 4.

When, to this first Part of the Machine, you add the second B, (*Plate XV. Fig.* 4.) it reaches to g, and gG is 8 Inches long: If upon this you lay the third Part C, this last reaches to f, and fF is of 4 Inches.

The Diameter of the Ball P, which in making the Experiments is to be let fall along the Curve E A, is of about half an Inch; neither must a less

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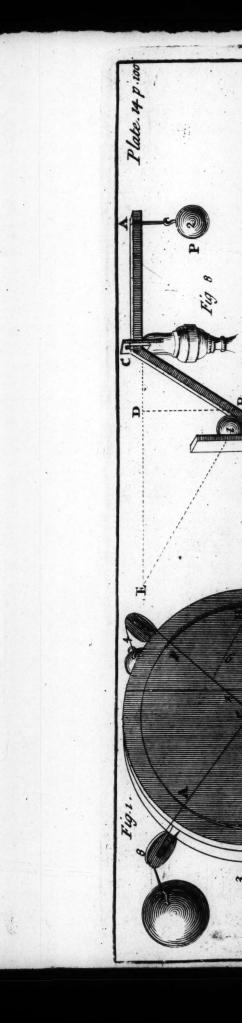
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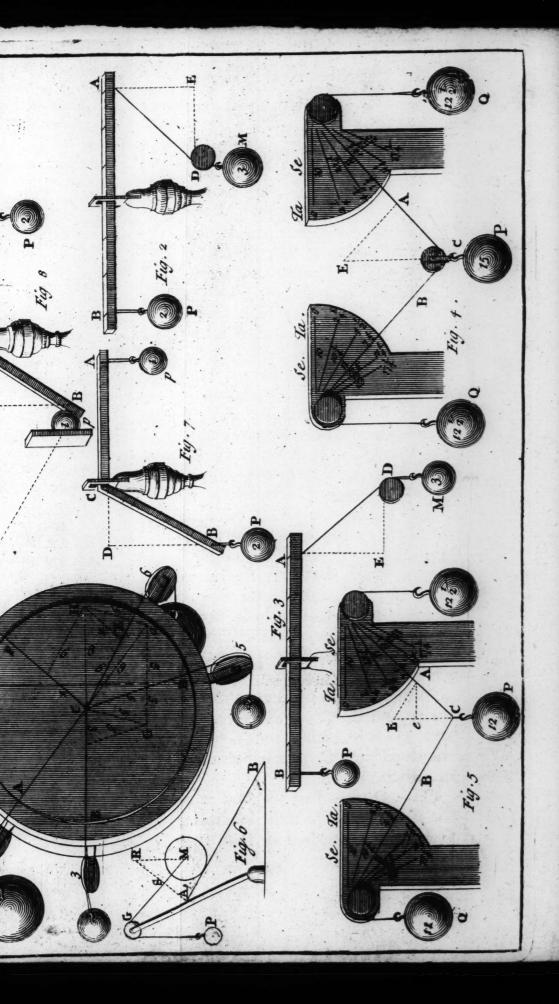
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Ball, or a bigger Machine than what is here mentioned, be made use of; for the less the Bodies are, and the swifter their Motion, the more in Proportion is the Motion retarded by the Air's Resistance; as shall be shewn in its Place.

When the Ball P is let fall from E, running down the Curve E A, it acquires fuch a Degree of Velocity, as appears to be always the same in several Trials; and with that Velocity and hori-

zontal Direction, it continues its Motion.

Experiment.] Having joined together the three Parts of the Machine, as in Fig. 4. let go the Ball P from E, and it will strike the Point F. Take away the least Part C, and let the Ball come down as before, and it will strike G. Lastly, take away the Part B, and the Ball, descending as before, will strike against H.

If you stick on a Piece of soft Clay upon H and G, the Point of the Stroke will be exactly mark'd; this will not do so well in the Point F, because of the greater Obliquity of the Motion there; but, by repeating the Experiment, the Point F will be well enough determined by Sight

only.

The Proposition of Numb. 134. may be experi-211 mentally confirmed by this Machine; for, as we have already said, the Ball running down E A will

strike the Point H.

Coming down E A, it acquires a Celerity which it could have acquired in falling in E D; * with *150 that Celerity it is horizontally projected from the Point A, and it moves that Length b H equably according to that Direction, whilst by its Fall it goes thro' A b equal to E D; but b H is double the Length A b or E D.

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212 What has been faid of the Curve, described by a Body projected horizontally, may also be appli-

ed to any Projection.

Let the Body be projected in the Direction A E, (Plate XV. Fig. 5.) and let A B, B C, C D, D E, be equal; the Body will go through the Curve A F G H I, fo that B F, C G, D H, E I, will be to one another, as 1, 4, 9, and 16; in which Case the Curve is also called a Parabola.

DEFINITION.

213 Let A I be drawn horizontal, and the Curve above-mentioned will cut it in I; A I is call'd the Amplitude of the Projection.

The Motions of Bodies projected with the fame Celerity, but different Directions, may be

compared together.

Let AL be the Height to which a Body, thrown up with a determinate Degree of Celerity, may rife: Let the Body with the fame Celerity be thrown along AB, cutting in B the Semicircle described on the Diameter AL; let AB express that Celerity, and MB be parallel to the Horizon. The Motion in AB may be resolved into two others: * the first along MB a horizon-

*192 into two others; * the first along MB a horizontal, and the second along A M a vertical Line; and it is only by that second Impression that the Body ascends: The Height therefore, to which the Body ascends in that Case, is to the Height to which it would ascend with the Celerity AB, as

*138 the Square of AM to the Square of AB; * that is, as AM to AL; but this is the Height to which the Body ascends with the Celerity of the Projection; therefore also AM is the greatest Height to which the Body comes in that Projection. In the Time of the Ascent in AM, the Body might

y

by an uniform Motion, with the same Celerity with which it moves in AM, in a horizontal Motion go thro' twice the Length of the Line MB; and as the Time of the Fall is equal to the Time of the Ascent, * the Amplitude AB is 136 four Times the Length of the same Line MB. Now this Demonstration will serve, whatever the Inclination of the Direction of AB is. Whence we deduce,

1. That the Amplitude is the greatest, with the 214 same Celerity, when the Angle of the Projection is a Half Right Angle. For then the Line m b, being a Radius of the Semicircle, is the greatest of all.

2. Except this Case, there are always two Inclinations, that give the same Amplitude; for if thro' B, Bb be drawn parallel to AL, cutting the Semicircle at b, and mb parallel to the Horizon; this Line will be equal to MB; therefore the Amplitude of the Projection, in the Direction Ab, will also be AI. In the second Part of the following Book, all this will be confirm'd by Experiments.

If the Celerity be changed, and the Body pro-215 jected in the same Direction, the Amplitude is changed, in the same Ratio as the Diameter A L; that is, the Amplitudes, the Direction remaining the same, are as the Heights to which Bodies, with the same Celerities, being thrown up, may ascend; and therefore they are as the Squares of

the Celerities.

C H A P. XXV.

Of Central Forces.

Body in Motion continues its Motion in a right Line, * and does not recede from it, unless a new Impulse acts upon it; after such an Impulse the Motion is compound, and so from the two there arises a third Motion in a Right Line also. * If therefore a Body is moved in a Curve, it receives a new Impulse every Moment; for a Curve cannot be reduced to Right Lines, unless you conceive it divided into Parts infinitely small. We have an Example of that Motion in the Projection of heavy Bodies; * and another in all Motions round a Point as a Center.

Center, be projected in a Line that does not go thro' that Center, it will describe a Curve; and, in all the Points of it, it endeavours to recede from that Curve, according to the Direction of a Curvature; that is, of a Tangent to the Curve; so that if the Force driving towards the Center should immediately cease to act, the Body would continue its Motion in a Right Line along the Tangent.

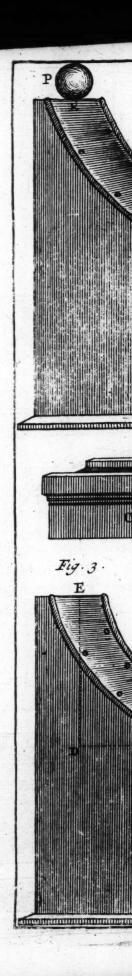
A Stone whirl'd round in a Sling describes a Curve, because the Sling does every Moment, as it were, draw it back towards the Hand; but, if you let the Stone go, it will fly out in the Tan-

gent of the Curve.

DEFINITION I.

The Force with which a Body in the Case abovementioned endeavours to fly from the Center, such as the Force by which the Sling in Motion is stretch'd, is call'd a Centrisugal Force.





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DEFINITION II.

But the Force, by which a Body is drawn or im-219 pell'd towards that Center, is call'd a Centripetal Force.

DEFINITION III.

These Forces are by a common Name call'd 220 Central Forces.

In all Cases, the centrifugal and centripetal For-221 ces are equal to one another; for they act in con-

trary Directions, and deltroy one another.

The whirl'd Sling is equally stretch'd both Ways, * and the Stone endeavours to recede from *1.26 the Hand with as much Force as it is drawn towards it.

Central Forces are of great Use in Natural Philosophy; for all the Planets move in Orbits, and most of them, if not all, turn upon their Axes.

I shall chuse out the chief Propositions relating to these Forces, and confirm them by Experiments; but first we must describe the Machines with which these Experiments are performed.

Plate XVI. Fig. 1, and 2.] A is a round Board 222 or Table of 2 Feet and a half Diameter; whose vertical Section is seen in Fig. 2. in which a a represents the Section of the Table itself, and g b the Section of its turn'd Foot, which is joined perpendicularly to its Center; this Foot or Supporter of it consists of two Pieces separated at D, which are fix'd together by four small Irons, whose Ends are rivetted to Rings of the same Metal.

The upper Part of the Foot has a Groove round it at cc; and has a cylindric Hole thro' it at fg of three Quarters of an Inch Bore.

The

The Frame of the whole Machine, represented at C, is very folid; and one Side receives the Foot of the Table A, which passes freely thro' an Hole in the upper Part of the Frame C; to which is firmly join'd the wooden Collar F of Fig. 3. which fits in the faid upper Part of the Frame.

The Table with its Foot bears upon the cross Piece E D, which has a Plate of Iron to receive the Brass Center b. This transverse Piece is fix'd but just above the Feet of the Frame, that, when the Table-Foot is let down upon it, the Groove c c may be but just above the wooden Collar; to the Top of which are screwed down two Iron Plates RR (Fig. 3.) by four Screws, fuch as In this Polition the Table will very freely move horizontally about its Center; and, that it may move the more eafily, there is slipped on upon the Foot close to the Table, (where it is not round, but fix or eight fquare) a small Wheel or Pulley, whose Section you see in bb, and which is joined to the Table by means of the Screws el, el. There must be three other such Wheels whose Circumferences, taking them at the Bottom of their Grooves, are to one another as one, two, three; the least of all the Wheels is of about 5 Inches Diameter.

Another Table B, made just like the first, is to be whirl'd about round its Center in the opposite Part of the Frame C. Tho' there is a small Difference between them; for in this the lower Part of the Foot has an Hole thro' it as well as the upper, (see i b Fig. 4.) yet it is turn'd freely, having fix'd to its Bottom a Brass Plate with a Hole in it to receive the little Pipe of another Plate M, whose vertical Section is seen at L, and which is fixed to E D, the other cross Piece of the Frame, at the Place m. This cross Piece must the ! fron Foo is m and whi the

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must be bored thro' to answer to the Hole of the Plate, in such Manner that a Thread may go from the Top of the Table quite thro' the whole Foot and the Piece E D. Such a Wheel as bb is made fast to the Table immediately under it, and is in Bigness just equal to the least of those which are made to take off and on, belonging to the Table A.

The two Tables A and B may be whirl'd, very swiftly, either separately, or both together, by Help of the great vertical Wheel Q: For performing of which, you must make use of the Machine of Fig. 5. which is a wooden Plane or strong slat Board, to which is perpendicularly six'd a Parallelopiped, in whose upper Surface are vertically six'd the two Pullies vv, at the Ends, and sideways at one End there is another Pulley as t, which is horizontal. The Surface, when the Machine is applied to the Frame, is in the same Plane with the small Wheels of the Tables.

If B alone is to be whirl'd, the Piece of Fig. 5. is to be fix'd to the Frame C, by Help of two Screws going thro' fuch Holes as x in the lower Part of the Piece, which must be so fixed, in respect to the little Wheel of the Table, as is represented in Fig. 6. where b represents that little Wheel: The Rope goes round the great Wheel Q, and from its lower Part goes from d towards v, goes round the Wheel b, and against the Pulley t, towards c, and so comes back to the upper Part of the Wheel Q.

The feventh Figure represents the Position of the Machine or Piece of Fig. 5. when both Tables are to be whirl'd round at once. A Sight of the Figure shews the Way of the Rope, which from v goes down to d, and so to the lower Part

of the great Wheel.

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Besides this, in several Experiments you must make use of long Boxes or Troughs IF, IF, which are laid upon the Tables, and fix'd to them with Screws; the Center of every one of these Boxes lies just over the Center of the Table where there is a Hole equal to the Hole g,f, (Fig. 2.) and exactly answering to it, in which Hole of the Box is thrust a wooden Cylinder N, Fig. 2.) as may be seen at G: thro' the Middle of this Cylinder goes a little Glass Tube of about a Quarter of an Inch Bore, whose Ends are thicken'd at the Flame of a Lamp, so as to make the Hole something less and smooth; that a Thread or small String may run up and down thro' it, without any sensible Friction.

One of the Troughs holds a Ball, tied to a Thread which goes thro' the above-mentioned Tube, and is also fastened by a Screw to the Weight O, (Fig. 7.) which lies in D the Separation of the Foot. This Weight is laid upon the lower Half of the Foot, from whence it is raised up, as the Ball recedes from the Center of the

Trough.

This Weight is a round Plate of Lead, and of about 2 Inches Diameter; it has a Brass Cylinder fix'd to its Center, whose upper Part, in order to receive the String, is cleft into two Parts, which are drawn together by means of a Screw: this Plate of Lead with its Cylinder weighs half a Pound; and there must be two such Weights.

There are several other Weights, some of half, some of a Quarter of a Pound, represented by P, (Fig. 7.) which are to be laid upon the said Weight O; that one may at Pleasure vary the Weight to

be raifed by the Ball.

When a Body, laid upon a Plane, does in the same Time, and about the same Center, revolve with that Plane,

Plane, and so describe a Circle; if the centripetal Force, by which the Body is every Moment drawn or impelled towards the Center, should cease to act, and the Plane should continue to move with the same Celerity; the Body will begin to recede from the Center (in Respect of the Plane) in a Line which passes thro' the Center.

Experiment 1.] Take a Ball which is tied to a Thread, the other End of the Thread being faftened to the Center of one of the Tubes A or B, and lay it on the Table, which must be whirl'd fingly so long, till the Ball is carried round with it; here the Ball is at rest, in respect of the Table, and in that Situation it is retained only by the String fastened to the Center; therefore it suffers no Impression in that Plane, except that by which the String is stretched, that is, whose Direction passes thro' the Center of the round Table; and so, if it be left to itself, it cannot the first Moment move in any other Direction in that Plane.

When a Body moves about a Center, if in its 224 Motion it comes nearer to the Center, its Motion is accelerated; but on the Contrary retarded, if it recedes from the Center.

Experiment 2.] Let the Trough F I, through whose Center the Cylinder G, with its Glass Tube, is fixed into the Center of the Table B, be fastened to the said Table.

Let the Ball L, tied to a Thread, be laid in the Trough, and the Thread put thro' the Tube above-mentioned, as also thro' the whole Foot of the Table, and the cross Piece at Bottom that sustains the Foot, and then with your Hand hold the End of the Thread.

Let the Table be turned round, and you will observe, that, during that Motion, the Ball will apply itself to one Side of the Trough, and is carried round so as to move with the same Velocity as the Trough. Let the Thread be pull'd, so as to bring the Ball nearer the Center, and it will immediately strike the opposite Side of the Trough, because it moves faster than the Trough. If you bring your Hand nearer to the Foot of the Table, so as to give more String, the Ball recedes from the Center, and strikes the first Side of the Trough, as moving more slowly than the Trough.

This Acceleration when a Body approaches nearer to the Center, and Retardation when it recedes from it, is determined by Geometricians: If a Body, for Example, which is driven towards the Center C (Plate XVI. Fig. 11.) be moved in the Curve A E, it will move faster at E and slower at A: Draw the Lines A C, B C, and E C, D C, so that the Areas ABC and D E C may be equal to one another, the Parts A B and D E of the Curve are described in equal

225 Times by the Body; and therefore, a Body that is retained in a Curve, by a Force tending towards a Center, is faid to describe round that Center

Areas proportionable to the Times.

namely, That a Body which is moved in any Curve in a Plane, and describes about any Point Areas proportionable to the Times, is turned out of the right Line, and urged by a Force tending to that Point.

27 The greater the Quantity of Matter in any Body is, the greater is its centrifugal Force; which arises

from a greater Quantity of Motion.

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come towards it; and they be so disposed, that by their Weight the heavy Fluid comes to the Center; upon moving the Whole about that Center, the light Fluid will come towards the Center, and the heavy one fly from the Center.

If a Solid be included with a Liquid in a determinate Space, the same may be said, as was said of the two Liquids: If it be lighter than the Liquid, it will come towards the Center; if heavier, it will recede from it. All which arises from the great Centrifugal Force in the heavier

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Experiment 3. Plate XVI. Fig. 8.] Take four Glass Tubes of about one Inch Diameter each, and a Foot long, and having hermetically sealed them, let them be firmly tied to an inclined Plane. In the first, you must have Quicksilver and Water; in the second, Oil of Tartar per deliquium, and Spirit of Wine; and the third, Water with a Leaden Bullet; and lastly, in the fourth, Water with a Piece of Cork; and all of them must be about

This inclined Plane must be fastened to the whirling Table A or B (Plate XVI. Fig. 1.) so that the lower Part of the Plane may come almost to the Center of the Table, by means of two Screws, one of which goes thro' α (Fig. 8.) Let the Table be whirled round, and immediately the lower Part of the Tubes will remain empty, and the heavier Bodies will go to that Part of the Tube which is farthest from the Center; the Cork descends and strikes to the lower Part of the Water, whilst the Leaden Eullet goes to the Top of the Tube.

Central Forces not only differ on account of 229 the Quantity of Matter, but the Distance does also cause a Change, and likewise the Celerity with which the Body is moved round: There is nothing

nothing else that can make any Difference in these Forces: And these are all the Things to be considered, when we compare them together.

DEFINITION IV.

Body going round a Center performs one whole Revolution; that is, if it describes a Curve that returns into itself, the Time elapsed between its Departure from and Return to a Point: If the Curve does not return into itself, instead of a Point we must take a Line passing thro' its Center.

The Periodical Time depends upon the Celerity of the Body; and therefore, in comparing central Forces, it must be taken for the Velocity.

When the Periodical Times are equal, and the Distances from the Center are also equal; the central Forces are as the Quantities of Matter in the revolving Bodies.

Experiment 4. Plate XVI. Fig. 1.] Of the three Wheels or Pullies bb, mentioned in the Description of the Machines, apply the least to the Table A; so that if the two Tables A and B be whirled at the same Time by the Motion of the Wheel Q, they may run round in equal Times; to each of them fix the long Troughs I F, I F; and the Cylinders G G, that contain Glass Tubes, must be thrust thro the Center Holes of the Troughs quite into the Feet of the Tables.

Put a Ball L of half a Pound into the Trough of the Table B, and a Ball L of one Pound in the Trough of the Table A: Threads tied to the Balls go thro' the little Tubes GG, and are fastened to Weights placed in the Separations of Hollows of the Feet of the Tables, in such Manner, that the Distances of the Balls from the Center, when the Threads are stretched and the Weights not raised,

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raised may be equal; now if the Weight in the Separation or Hollow of the Foot of A be one Pound, that in the Separation of B must be half a Pound; or if this last should be one Pound, the other must be two Pounds.

Let the Wheel Q be turn'd round faster and faster, till by the centrifugal Force of the Balls the Weights above-mentioned be raised, and both Weights will be listed up precisely at the same Time; therefore Weights, that are as the Bodies, will, cateris paribus, be overcome by the centrifugal Force.

When the Quantities of Matter in the revolving 232 Bodies are equal, and the Periodical Times also equal, the Forces are as the Distances from the Center.

Experiment 5. Plate XVI. Fig. 1.] This Experiment is made in the same Manner as the foregoing; instead of a Ball of half a Pound, put in the Trough of the Table B a Ball equal to the other that is of one Pound. Let the Distances from the Center be taken in any Proportion; if the Weights join'd to the Balls in the same Proportion, and the Wheel Q be moved faster and faster, you will see the two Weights rise exactly at the same Time. As for Example, if the Distance of the Ball upon A be of 12 Inches, and the Weight join'd to it of 1 Pound and a half; and the Distance of the other Ball of 8 Inches, and the Weight join'd to it of 1 Pound, the Experiment will succeed.

When the periodical Times are equal, but the Di- 233 ftances and the Quantities of Matter in the revolving Bodies differ, the central Forces are in a Ratio compounded of the Quantities of Matter and the Diffances; which follows from the two last Propositions. To determine that compound Ratio, the Quantity of Matter in each Body must be multi-

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plied by its Distance from the Center, and the Products will be to each other in the Ratio afore-faid.

Experiment 6.] If in the last Experiment the Ball upon B be changed, and you place a Ball of half a Pound at 8 Inches from the Center, and you also change the Weight join'd to it, and half a Pound be used instead of a Pound; the Experiment will also then succeed, and the Weights will begin to rise at the same Time. If you multiply the half Pound Ball by its Distance of 8 Inches, the Product is 4, and multiplying the 1 Pound Ball by 12 Inches, its Distance from the Center, the Product is 12, which Products are to one another as 1 to 3; that is, as the Weight of half a Pound to that of 1 Pound and a half, which are in this Experiment both listed up at the same Moment.

The Differences of central Forces arising from the different Distances from the Center, and the different Quantities of Matter, may compensate 234 one another; for supposing the Quantities of Matter in the revolving Bodies to be in an inverse Ratio of the Distances from the Center, the Central Forces will be equal; as much as one Force is greater in respect of the Quantity of Matter, so

greater Distance.

Experiment 7.] Let a Ball of half a Pound be placed at the Distance of 14 Inches, and a Ball of one Pound at the Distance of 7 Inches; every thing else being as in the foregoing Experiment; if the Weights in the Foot or Spindle of each Table be alike, they will rise at the same Moment.

much does the other exceed it by reason of its

235 There is a Case of this Proposition, when two Bodies join'd by a Thread revolve about their common Center the

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Center of Gravity. For the Distances from that Center are in an inverse Ratio of the Weights of the Bodies, * and therefore the central Forces are equal. By the Force by which one Body endeavours to recede from the Center, the other is drawn towards it; and by reason of the Equality of the Forces, they retain one another, and continue their Motion; if they revolve about any other Point, they do not continue their Motion, and the Body, whose centrifugal Force overpowers, recedes from the Center, and carries the other Body along with

Experiment 6. Plate XVI. Fig. 10. Let two unequal Bodies P and Q be join'd by a Thread, in which you must mark the Point C, which is the common Center of Gravity of those Bodies, when the Thread is stretch'd.

In this Experiment you must use but one Table, and fix upon it a long Trough that reaches beyond the Diameter of the Table both Ways, and whose middle Point is over the Center of the Table. In this Trough you must place the Bodies above-mention'd, and the Thread that joins them being stretch'd, the Point C must be put in the Middle of the Trough. When the Table is whirl'd round, the Bodies are carried round with it, and remain at rest in it. If the Point C be removed from the Middle of the Box, upon whirling the Table, both Bodies will be carried to that End of the Box which the Point C was placed nearest to.

The Difference of the central Forces is also determined from the Difference of the periodical Time.

When the Quantities of Matter in the Bodies 236 whirl'd round, and the Distances from the Center are equal, the central Forces are in an inverse Ratio of the

the Squares of the periodical Times: that is, directly as the Squares of the Revolutions made in the same Time.

Experiment 9. Plate XVI. Fig. 1.] To the Table A apply a Wheel or Pulley, such as bb, (Fig. 2.) whose Circumference is double the Circumference of the Wheel which is fix'd to the Table B; so that when the two Tables are whirl'd both together, B shall go round twice for A once; that is, the periodical Time of that shall be double the

periodical Time of this.

In each Trough I L, I L, lay a Ball of one Pound at equal Distances from the Center. The Ball laid on the Table B must be tied to two Pounds in the Foot, and the other Ball upon A is join'd by its Thread to half a Pound in the Foot. Upon whirling the Tables, both Weights will rise at the same Time: Which Weights are here as 1 to 4, the periodical Times being as 2 to 1, whose Squares are reciprocally as 1 to 4.

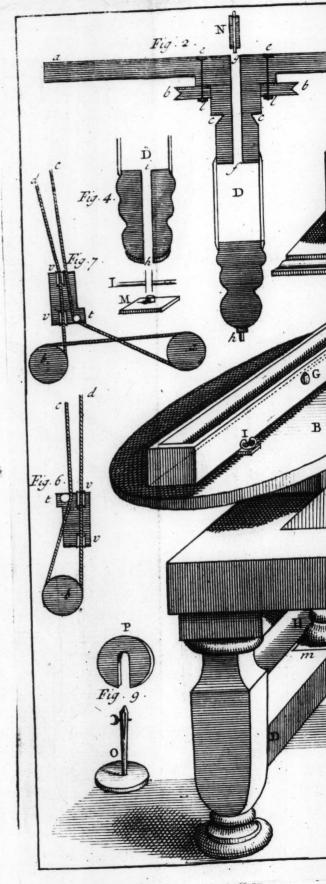
237 However the central Forces differ from one another, they may, according to what has been faid, be compared to one another; for they are always in a Ratio compounded of the Ratio of the Quanti-

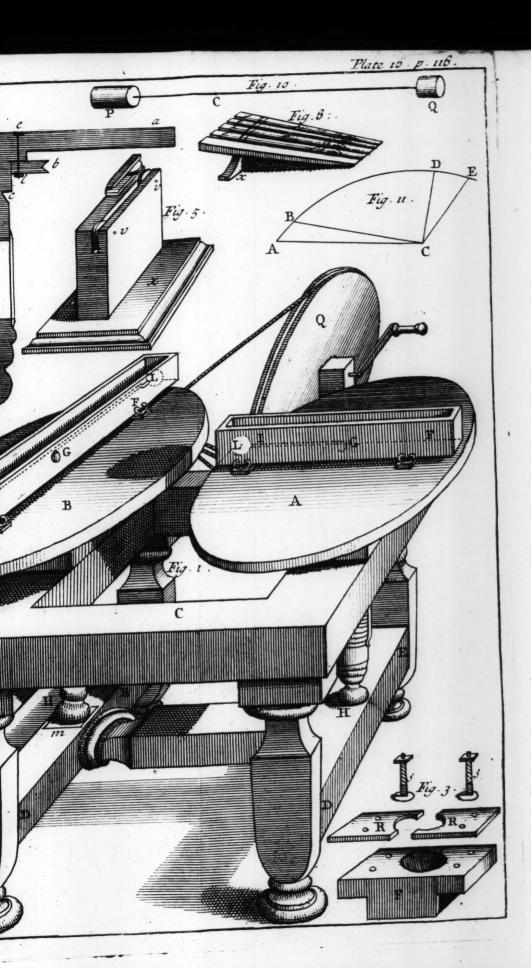
* 231 ties of Matter in the revolving Bodies, * and the * 232 Ratio of the Distances from the Center, * and also

* 236 Times. * If you multiply the Quantity of Matter in each Body by its Distance from the Center, and divide the Product by the Square of the periodical Time, the Quotients of the Division will be to one another in the said compound Ratio, that is, as the central Forces.

Experiment 10.] Every thing being prepared as in the former Experiment, fet a Ball of half a Pound, at the Distance of 8 Inches from the Center

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Center of the Table B, and let it by the Thread be joined to one Pound in the Foot; let another Ball of two Pound be placed at the Distance of 12 Inches from the Center of the Table A, and joined with a Weight of 3 Quarters of a Pound; whirl the Tables, and the Weights will be raised

just at the same Time.

Here the Bodies are as ½ to 1; the Distances as 8 to 12; the Squares of the periodical Times as 1 to 4; multiplying one Half by 8, and dividing the Product by 1, the Quotient of the Division is 4; multiplying 1 by 12, and dividing the Product by 4, the Quotient is 3. Therefore the central Forces are to one another as 4 to 3, which Ratio also the Weights in the Feet have to one another.

When the Quantities of Matter are equal, the 238 Distances themselves must be divided by the Squares of the periodical Times, to determine the Proporti-

on of the central Forces.

In that Case, if the Squares of the periodical 239 Times be to one another as the Cubes of the Distances, the Quotients of the Divisions, as well as the central Forces, will be in an inverse Ratio of the Squares of the Distances.

Experiment 11.] Let the periodical Times of A and B be as 1 to 2, in the fame Manner as in the two last Experiments. Take two equal Balls, and let the Distance from the Center on B be 10 Inches, and the other Ball's Distance from the Center be of 16 Inches: To the Thread of the first, fasten one Pound and a Quarter, and to the Thread of the other, fasten Half a Pound in the Hollow of the Foot of A; whirling the Tables, the Weights will rise the same Moment.

In that Experiment the central Forces are as 5 to 2, which you also find by Calculation. ***238

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This Ratio differs very little from the inverse Ratio of the Squares of the Distances, which are to one another as 200 to 512; the Cubes of the Distances are also almost as the Squares of the periodical Times: These Squares are as 1 to 4, and those Cubes as 125 to 512, which Ratios do not much differ. If you take other Numbers, these Ratios will be exactly the same, and the Experiment will succeed in the same Manner; but it is not easy in the Experiment to vary the periodical Times or the Weights in what Ratio you please.

When the Force, by which a Body is carried towards a Point, is not every where the same, but is either increased or diminished in Proportion to the Distance from the Center, several Curves will thence arise in a certain Proportion.

If the Force decreases in an inverse Ratio of the Squares of the Distances from that Point, the Body will describe an Ellipsis, which is an oval Curve, in which there are two Points called the Foci, and the Point towards which the Force is directed falls into one of them: So that in every Revolution the Body once approaches to, and once recedes from it. The Circle also belongs to that Sort of Curves, and so in that Case the Body may also describe a Circle: The Body may also (by supposing a greater Celerity in it) describe the two remaining Conic Sections, viz. the Parabola, or Hyperbola, Curves, which do not return into themselves.

On the contrary, if the Force increases with the Distance, and that in a Ratio of the Distance itself, the Body will again describe an Ellipse; but the Point, to which the Force is directed, is the Center of the Ellipse, and the Body in each Revolution will twice approach to, and again, twice recede from that Point. In this Case

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Case also a Body may move in a Circle, for the Reason above-mentioned.

Experiment 12.] Hang up a leaden Ball with a long Thread; if the Ball be drawn back from its Point of Rest, it is always carried towards it by its Gravity, and from equal Sides with equal Force, if the Distance be equal. The Ball in its Motion describes an Arc of a Circle, which Way soever it falls when you let it go: If those Arcs are not very great, they coincide with a Cycloid, and the Force, with which the Ball in any Point is carried towards the lowest Point, is as its Distance from that Point; * therefore here the Force increases * 156 in the Ratio of the Distance.

Let the Ball be pull'd back from the lowest Point, and projected obliquely; then it will describe an oval Curve about that Point, which (when the Ball does not run out to a great Distance) will hardly differ at all from an Ellipse, because of the Proportion of the Forces, and because in that Case the Ball does sensibly move in the same Place.

The Center of the Ellipse is the Point in which the Ball is at rest when it is not projected; and in every Revolution the Ball does twice approach to, and twice recede from it. If the Ball hangs over a Table so as almost to touch it when it is at rest, and the Point, over which it is, be mark'd upon the Table, the Experiment will become more sensible if you draw an Oval upon the Table with Chalk, by sollowing the Body with your Hand.

If the Proportion (mentioned Numb. 241, and 243, 242.) of the Forces by which a Point is driven towards a Center, be a little changed, the Body will no longer describe an Ellipse; but such a Curve as may be reduced to an Ellipse, by sup-

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posing the Plane in which the Body moves agitated by some Motion, which therefore will make the Ellipsis moveable.

Experiment 13.] Every Thing being as in the former Experiment, let the Ball be so thrown that it may run out to a greater Distance; and then it will describe a Curve which may be referr'd to the moveable Oval: it will indeed twice in every Revolution come towards the Center, and twice recede from it; but the Place of the Points in which it is least, or most distant, is changed every Revolution, and these Points are always carried the same Way, their Motion conspiring with the Motion of the Ball.

CHAP. XXVI.

Of the Laws of Elasticity.

E have already shewn what Elasticity is, and whence it arises; * and what is its Effect in the Congress of Bodies, whether they strike one another directly or obliquely; what remains is to examine the Laws of Elasticity itself, which we shall do from Phænomena.

All Bodies, in which we observe Elasticity, consist of small Threads or Filaments, or at least may be conceived as consisting of such Threads; and it may be supposed that those Threads laid together make up the Body; therefore that we may examine Elasticity in the Case which is the least complex, we must consider Strings of musical Instruments, and such as are of Metal; for Catgut-Strings have a spiral Twist, and cannot be consider d in the same Manner as those Fibres of which Bodies are form'd.

244 The Elasticity of Fibres consists in this, that they can be extended, and taking away the Force by which they

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they are lengthen'd, they will return to the Length

which they had at first.

Fibres have no Elasticity, unless they are extend-245 ed with a certain Force; as it appears in Strings that have their Ends fix'd without being stretch'd; for if you remove them a little from their Position, they do not return to it: but what the Degree of Tension is, which gives Beginning to Elasticity, is not yet determined by Experiments.

When a Fibre is extended with too much Force, 246 it loses its Elasticity; and this Degree of Tension is also unknown; this we know, that the Degree of Tension in Fibres, which constitutes Elastici-

ty, is confined to certain Limits.

Hence appears the Difference of Bodies that 247 are elastic, and such as are not so; why a Body loses its Elasticity, and how a Body destitute of Elasticity acquires that Property. A Plate of Metal, by repeated Blows of a Hammer, becomes elastic, and, being heated, does again lose that Virtue.

Between the Limits of Tension, that terminate Elasticity, there is a different Force required for different Degrees of Tension, in order to stretch Chords to certain Lengths: What this Proportion is, must be determined by Experiments, which must be made with Chords of Metal, as was said before. But as these Wires are scarce sensibly lengthen'd, the Proportions of the Lengthening cannot be directly measured; therefore they must be measured by another Method.

Let A B (Plate XVII. Fig. 1.) be a small Wire stretch'd horizontally with a certain Force, whose Ends are fix'd at A and B: Let it be bent by a Weight hanging in the Middle of it, so that it may come to the Position ACB.

DEFINITION.

248 The Line C c drawn from the middle Point of a String or Chord after its Inflexion, to the middle Point of the same when it was in its natural State, is call'd the Sagitta (Arrow) of the Chord.

Let ce be an Arc of a Circle described about the Center B, with the Radius B c. Half the Chord or Wire by the Inflexion was stretch'd the Length Ce, which Quantity has a certain Relation

to the Sagitta Cc.

The Weight also, by which the String is stretch'd, has a certain Relation to the Force with which the Fibre is lengthen'd, that is drawn along BC: and so in several Experiments by comparing the Sagitta Cc, and the Weights with which the Chords are inslected, the Proportions of the Lengthenings are determined; as will be shewn in the following Experiments.

Board, about 3 Foot long, and 1 Foot high.

See Plate XVII. Fig. 2.

The Rulers of Wood mn, mn, are fix'd to the Board like a Moulding, and carry two Prisms H, H, made like a Wedge, which slide along upon the Rulers, and are fix'd any where upon them by means of Screws, which hold them behind the Board, their Shanks being moved backwards and forwards, by means of a Slit in the Board.

Between A and B there are equal Divisions reckon'd from the Middle on either Side, in order to determine the Places where to fix the

Prifins.

At O there is a Groove, to hold the Pulley T in the Side of the Board; which Pulley is reprefented in Plate XIII. Fig. 8.

The Wire, with which the Experiments are made, is fix'd at one End of the Ruler m n, and

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at the other End goes over the Pulley T, the Weight P stretching it, and the Prisms, H, H, sustaining it in Points, which are equally distant from the Middle of the Machine.

There is a Brass Plate de let into the Middle of the Board, and mark'd with very small Divisions, along which moves another Brass Plate or Index fg, which hangs upon the Wire, having a Hole thro' which it runs: This Index has a Scale hanging from it, which, together with the Index fg, weighs just an Ounce. The Length of the Wire is determined in each Experiment by the Distance of the Edge of the Prisms H, H; for in the small Instexions made by hanging on Weights in C, concerning which alone Experiments are made, the String is not moved upon the Prisms, nor is the Weight P raised ap, but only the Part A B is extended by these Instections.

In the Inflections of the String, the Sagittæ are measured by the Divisions on the Plate ed; for the End g of the Index gc does always descend equally with the Point C in every Inflection.

Experiment 1.] Let P be a two Pound Weight, 250 and let the Wire be inflected at C with the Weight of an Ounce, that is, with the Weight of the Scale and Index fg; and observe the Division of the Plate ed, to which the End g of the Index fg descends. Change the Weight P to 4 Pounds, and also double the Weight by which the String is inflected, that g may descend to the same Division, and this Weight will be two Ounces: Three Ounces will give the same Inflexions, when the Weight P is of six Pounds.

From this Experiment it follows, that the 251 Weight, by which a Fibre is increased a certain Length by its stretching, is in the different Degree of Tension, as the Tension itself; if, for Example, there be three

three Fibres of the fame Kind, Length, and Thickness, whose Tensions are as 1, 2, and 3; any Weights in the same Proportion will equally stretch those Fibres.

The least Lengthenings of the same Fibres are to 252 one another nearly as the Forces by which the Fibres are lengthened. As for Example, let a Fibre be stretched with the Weight of 100 Ounces, if it be separately lengthen'd with the Weights of I Ounce, 2 Ounces, and 3 Ounces, the Lengthenings will be nearly as 1, 2, and 3; that is, each Ounce superadded does equally lengthen the Fibre: For the Tensions by the Weights of 100, 101, and 102 Ounces, by which the Fibre is stretch'd in each Case, when an Ounce is superadded, do not fenfibly differ from each other.

The Property of Fibres may be applied to their Inflexion, and is of great Use. Let the Wire A B (Plate XVII. Fig. 3.) be so inflected, as to acquire the Positions AcB, AcB, and ACB, yet so that in the greatest Inflexion the Sagitta may not be i Inch long, supposing the Wire 2 Feet and a Half; In those Cases the Lengthenings of the String are very small, therefore they are in the Ratio of the Forces that

252 produce them, * and they ferve to express them; let cD express the Force by which a String is stretch'd when it is not inflected, and with the Center B describe the Circle Dd; the Lines dc, dc, dC, which are longer than cD by the Quantity by which the Fibre was lengthened in every Case, express the whole Forces, by which the Fibre is stretched in every Case. But here the Arc Dd is hardly of one Degree, and D is always far enough distant from the Point c, wherefore Dd may be looked upon as a Right Line parallel to c C, and the Lines cd, cd, Cd have the same Ratio to the Lines & B, & B, CB. ThereA, b CA flecte doub fore Strin ni |be the C

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fore the Point C is always drawn towards B c and A, by Forces proportionable to the Line C B or C A; and the Force by which the Wire is inflected, whose Direction is along c C, is as the double Sagitta, * or as the Sagitta itself. There-* 203 fore in all the least Inflexions of a Chord, Musical 253 String or Wire, the Sagitta is increased and diminished in the same Ratio as the Force with which the Chord is inflected.

Experiment 2. Plate XVII. Fig. 2.] Let the Wire AB, stretched by any Weight, be inflected by the Weight of 1, 2, and 3 Ounces; the Descents of the Point g, that is, the Sagittæ themselves are

to one another as 1, 2, and 3.

In Chords of the same Kend, Thickness, and 254 which are equally stretched, but of different Lengths; the Lengthenings, which are produced by superadding equal Weights, are to one another as the Lengths of the Chords. This is plain, because the Chord is equally stretched in all its Parts; therefore the Lengthening of a whole Chord is double the Lengthening of half of it, or of a Chord of half

the Length.

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As to the Inflexion of those Chords, let AB, ab, (Plate XVII. Fig. 4) be Chords of the same Kind and Thickness, but of different Length, equally stretched, and so inflected, that ACB shall be the Position of the first, and adb that of the last; and let the Triangles BCc, and bDd be similar: cB is to Db, that is, the Lengths of the Chords are as CB to db; therefore the Chords are lengthened in Proportion to their first Length, and consequently they are drawn by equal Force in the Directions bd, ad, BC, AC: ** 254 But by the Likeness of the Triangles above-men-255 tioned, the Forces also acting along cC and Dd are equal to one another *, and the Sagittæ cC, * 203 Dd;

D d, are as the Lengths of the Chords; which does therefore, cæteris paribus, obtain in unequal and inflected Chords.

Experiment 3. Plate XVII. Fig. 2.] Let the Chord A B be stretched by any Weight, having fixed the Prisms H, H, at the sixth Division on each Side: Now let it be inslected with any Weight, so that the Sagitta may be equal to six Divisions of the Plate e d. Let the Prisms be brought to and fixed at the fourth Division on each Side, and the Sagitta will be equal to four Divisions of the Plate; and so on for any Position of the Prisms.

One may compare together Fibres of the fame Kind, but different Thickness; they may be looked upon as made up of feveral very fine Fibres of the same Thickness, whose Number in the abovementioned Fibres must be taken in a Ratio of the Solidity of those Fibres, that is, as the Squares of the Diameters, or as the Weight of the Fibres when their Lengths are equal. Therefore these Fibres will be equally stretched by Forces that are in the same Ratio of the Squares of the Diameters; which Ratio also is required between the Forces by which the Chords are inflected, that the Sagittæ may be equal in the given Fibres. But by diminishing the Force by which the Fibre is stretched in the same Ratio as the Force by * 250 which it is inflected, the Sagitta is not changed *

256 Therefore, if the Forces by which the Fibres are firetched be equal, and they are inflected by equal Forces, even in that Case also the Sagittæ will be equal, however different the Thickness be.

Experiment 4. Plate XVII. Fig. 2.] Take any Chords of the fame Kind, and unequal Thickness;

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ckfs; ness; and let them be separately applied to the Machine, leaving the Prisms HH in the same Place; if they be stretched by the same Weight P, and also be inslected by the same Weight L, the Sagittæ will be equal.

Let the Chord AB (Plate XVII. Fig. 1.) ftretch- 257 ed any bow, be so inflected as to acquire the Figure ACB, then left to itself, and by its Elasticity it will return to its first Figure, and in that Case the Motion of the Point C is accelerated; for when the Chord is let go from the Position ACB, the Point C is moved with the Force that is able to retain it in that Position. This Motion is not destroyed, but there is superadded to it, in all the Points of the Sagitta, the Force by which the Point C might be retained in them. The Celerity is the greatest of all at c, and by that Celerity the Point C is carried farther, and then returning, it will perform several Vibrations, in which the Point C runs out but short Spaces; for which Cause the Force, by which the Point C is acted upon in all Distances from c, is as the Distance * in each Point. Therefore the Motion agrees * 253 with the Motion of a Body vibrating in a Cyclold, and how unequal soever the Vibrations are, they are performed in the same Time.*

If there be two equal and similar Chords, but 258 unequally stretched, unequal Forces are required to inflect them equally; therefore the Vibrations are performed in unequal Times. One may compare their Motions with the Motions of the Pendulums which vibrate in Cycloids *, and descri- * 257 bing similar Cycloids by different Forces; which Forces are inversly as the Squares of the Times of the Vibrations. * In Chords therefore likewise the * 165 Squares of the Times of the Vibrations are to one another inversly, as the Forces by which they are equally

equally inflected; which are as the Weights by

* 250 which the Chords are stretched. *

but of different Lengths, their Motion must be compared with that of Pendulums by another Method; for as the Times of the Vibrations are to be consider'd, the Celerities also, with which the Chords are moved, must also be considered: And in the Chords ACB, adb (Plate XVII. Fig. 4.) whose Sagittæ are equal, and in which the Points C and d may be considered as describing similar Cycloids, the Celerities, with which those Points are moved in correspondent Points, are to each other in an inverse Ratio of the Squares of the Times of the Vibrations. * In Pendulums and equal Chords.

* 165 Vibrations. * In Pendulums and equal Chords, the Forces are taken for the Celerities; because in

77. 63 those Cases they are in the same Ratio. *

Let the Chords A C, a b, be divided into very fmall Parts, but each into an equal Number of Parts; the Ways to be run thro' by correspondent Parts, supposing the Sagittæ equal, will be equal, and thefe fmall Parts will perform fimilar Vibrations; but the Particles of Matter in the correspondent Particles are as the whole Chords: That therefore their Celerities may be determined in correspondent Points, the Forces with which the Chords are inflected, when the Sagittæ are equal, must be divided by the Quantity of Matter in the Chords, as it follows from Numb. .64. It is therefore plain, that those Celerities are to one another directly as the Weights by which the Chords are inflected, and inverfly as the Quantities of Matter in those Chords, that is, inversly as their Lengths: But those Weights are also in an inverse Ratio of the 255 Lengths of the Chords; * therefore the Celeri-

Lengths, that is, inversly as the Squares of the

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Length; and then, as was faid before, the Squares of the Times of the Vibrations will also be in that inverse Ratio. The Lengths therefore of the Chords

will be as the Times of the Vibrations.

One may, in the same Manner, compare the 265 Times of the Vibrations of Chords of different Thickness, supposing the Chords equal, and stretched with equal Weights; the Quantities of Matter are as the Squares of the Diameters; therefore to determine the Celerities of the correspondent Points, the Weights, by which the Chords are inflected, are to be divided by those Squares, when the Sagittæ are equal; * the Celerities therefore are * 256 inversly as the Squares of the Diameters, and therefore the Diameters are as the Times of the Vibrations.

Any Chords of the same Kind being given, the 261 Durations of the Vibrations may be compared together; for they are in a Ratio compounded of the inverse Ratio of the square Roots of the Weights, by which the Chords are stretched,* of the Ratio * 158 of the Lengths of the Chords,* and the Ratio of * 259 the Diameters.* If you multiply the Diameters * 260 by the Lengths, and divide the Product by the square Root of the Weight that stretches the Chord, and go thro' the same Operation for several Chords; the Quotients of the Division will be to one another as the Times of the Vibrations.

Elastic Plates may be considered as a Conge-262 ries, or Bundle of Chords; when the Plate is inflected, some Fibres are lengthened, and there are unequal Lengthenings in several Points of the Plate; now the Curve, which is formed by the inflected Plate, may be discovered from what has been said concerning Chords.

By comparing together the Inflexions of the 263 fame Plate, they are proportional to the Forces by

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which the Plate is bent. Let AB (Plate XVII. Fig. 5.) be an elastic Plate or Spring, whose End A is fixed, and let it be inflected by two Forces,

264 so as to be brought into the Position ab and ab; if the one be doubled, the other, bb and bB, will be equal; and therefore in the Vibrations the Motion of the Spring is accelerated in the same 253 Manner as the Motion of a Chord *, and the Mo-

tion of a Pendulum in a Cycloid *; and the Vibrations of this Plate are performed in the same

Time.

Experiment 5. Plate XVII. Fig. 6. The Spring A is made up of feveral elastic Plates, and put into the Box B, and there moves on each Side; between the Rulers c d, c d, two Strings are fixed to the upper Part of the Spring, and run thro' the Holes e, e, in the Bottom of the Box. If you hang half a Pound upon the Threads, it will descend half an Inch; add another half Pound, and it will descend half an Inch more; and so on, till the Spring can be compressed no farther.

Each small Plate is bent in Proportion to the Weight; and the Motion of the Weight, on account of all the Inflexions together, follows the same Proportion. The Experiment is made with several Plates joined together; because in various Inflexions the Direction of the Action of the Weight on the Plates is not sensibly

changed.

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265 What has been said of the Inflexion of Plates may be applied to the curve Plate or Spring A C B (Plate XVII. Fig. 7.) If it be pressed by two Weights, so as to acquire the Position acb, aeb, and the Weights are to each other as I to * 263 2, the Distances cc and cC will be equal *:

Therefore the bending in of the Spring, or Spaces gone

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gone thro' by the Point C, are as the Weights with which the Plate is pressed. Which may also be applied to the bending in of several Plates joined together.

The Ball ACB (Plate XVII. Fig. 8.) being 266 made of an elastic Substance, may be considered as consisting of several Plates; and the Introcessions (or Yieldings inward) of the Point C will be proportionable to the Forces with which the

Body is compressed.

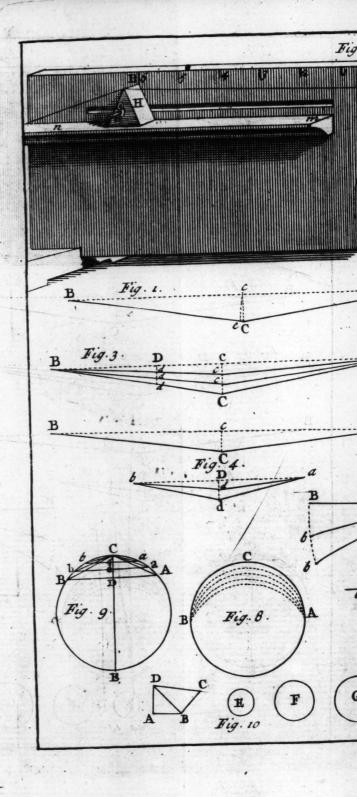
Let the Point C of the Ball ACBE (Plate XVII. Fig. 9.) strike several times against any Plane, and let that Point go inwards to d, d, and D; the Strokes will be to each other as the Lines Cd, Cd, and CD. At the first Stroke the Part abc becomes flat, the second Stroke acb is flattened, and the third ACB: As here we always consider the least Arcs, the Arcs (that is, the Diameters of the plane Surfaces made by the Strokes,) are to one another fenfibly as the Chords Ca, Ca, and CA; therefore the Surfaces are as the Squares of those Chords; in which Ratio also, from the Nature of the Circle, are the Lines Cd, Cd, and CD, which are to each other as the Strokes. Therefore in elastic Spheres, the 268 Planes made by the Strokes follow the Proportion of the Strokes.

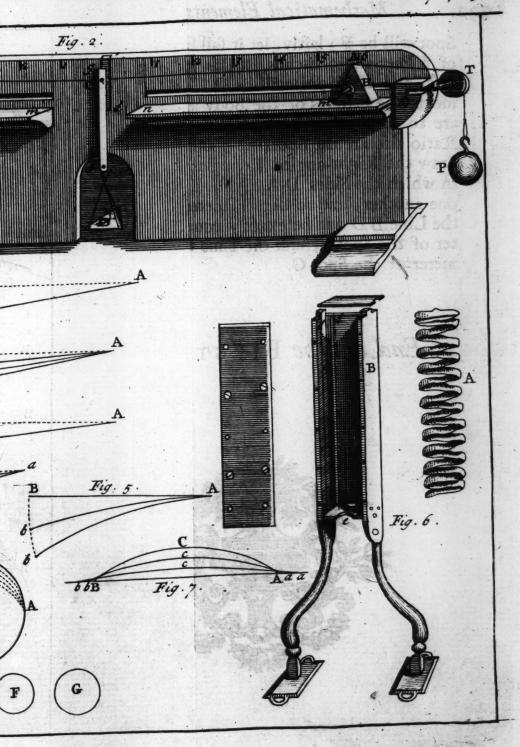
Experiment 6.] Take a flat Piece of blue Marble made fast in a horizontal Position, and a little wet, so as to make the Colour the more intense; if you let an Ivory Ball fall upon this Plane, that Part of the Ball, which by being made flat applies itself to the Stone, leaves a very round Spot in the Surface of it; Let the Ball fall from the Height of 9 Inches, and the Spot be E: then let it fall from the Height of 3 Feet which is the Quadruple of the other, and the Spot will be F; lastly, let it fall from the Height of 6 Feet and 9 Inches, which is nine times the first, and the Spot will be G. In that Experiment, the Strokes of the Body against the Stone are to each other as 1, 2, and 3 *: In which are to each other as 1, 2, and 3 *: In which are the Spots E, F and G; for if you draw the Right-angled Triangles DAB, DBC, in which the Sides DA, AB, BC, are equal to one another, and to the Diameter of the Spot E, the Line BD will be exactly equal to the Diameter of the Spot F, and the Line CD to the Diameter of the Spot G.

End of the FIRST BOOK.



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ELEMENTS

OF

Natural Philosophy,

CONFIRMED BY

EXPERIMENTS.

BOOK II.

PART I. Of the Gravity, Pressure, and Resistance of FLUIDS.

CHAP. I.

Of the Gravity of the Parts of Fluids, and its Effect in the Fluids themselves.



FLUID is a Body whose Parts yield to any Force impressed, and by yielding are very easily moved one amongst another. * Whence it * 30 follows, that Fluidity arises from 269

this, That the Parts do not strongly cohere, and that the Motion is not hinder'd by any Inequality in the Surface of the Parts, as it happens in Pow-ders.

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But the Particles, of which Fluids consist, are of the same Nature with the Particles of other Bodies, and have the same Properties; for Liquids are often converted into Solids, when there is a more strong Cohesion of them, as in Ice. On the contrary, melted Metals give us an Instance

of a Solid changed into a Fluid.

they consist of heavy Particles, and have their Gravity proportionable to their Quantity of Matter, in any Position of the Parts. If in the Liquid itself that Gravity be not sensible, it is owing to this, that the lower Parts sustain the upper, and hinder them from descending: But it does not follow from thence, that the Gravity is taken away; because a Liquid contained in a Vessel will press down the End of a Balance, which carries the Vessel, in Proportion to its Quantity. The sollowing Experiment will also shew, that the Gravity is preserved in any Part of the Liquid.

riments relating to the Gravity of Fluids, we use a very exact Pair of Scales, differing from common Scales only in this, that each Scale has a Hook VV under it, (Plate XVIII. Fig. 1.) for suspending such Bodies as are to be immersed in Liquids.

The Balance itself hangs by a Line which goes round two Pullies TT, and is fastened to a Weight P, (Plate XVIII. Fig. 1.) that, by moving the Weight, the Balance may be conveniently raised and depressed, and suspended at any Height.

Experiment 1. Immerse in Water the Phial D close shut, and hanging by a Horse-hair, and balance it with the Weight in the opposite Scale; then, without taking the Phial out of the Water, open it, and let it be filled with Water, and you will

will find, that the Water in the Phial will bring down the End of the Balance, altho' it has no Communication with the external Water: If you restore the Aquilibrium, by putting more Weight into the opposite Scale, the Phial will remain fuspended in any Part of the Water.

From this Gravity it follows, that the Surface 272 of a Fluid contained in a Vessel, to keep it from flowing out, if it be not pressed from above; or if it be equally pressed (for that makes no Alteration) will become plain, or flat, and parallel to the Horizon. For, as the Particles yield to any Force impressed, they will be moved by Gravity, 'till at last none of them can descend any lower.

The lower Parts fustain the upper, and are pref- 273 fed by them; and this Pressure is in Proportion to the incumbent Matter, that is, to the Height of the Liquid above the Particle that is pressed; but, as the upper Surface of the Liquid is parallel to the Horizon,* all the Points of any Surface, which * 272 you may conceive within the Liquid parallel to the Horizon, are equally press'd.

If therefore in a Part of such a Surface there 274 is a lesser Pressure than in the other Parts, the Liquid, which yields to any Impression there, will be mov'd, that is, will ascend, 'till the Pressure

becomes equal.

Experiment 2. Plate XVIII. Fig. 2.] Take a Glass Tube C open at both Ends, and stopping one End with your Finger, immerfe the other in Water; when the Tube is full of Air, the Water will rife in it but to a very small Height: If you take away your Finger, that the Air that is compressed may go out, the imaginary Surface (as Mr. Boyle used to call it) that you conceive in the Water, just at the Bottom of the Tube, and parallel to the Horizon, is less pressed just against the

the Hole of the Tube, fo that the Water will rise up into the Tube till it comes up to the same Height with the external Water.

The Pressure upon the lower Parts, which arises from the Gravity of the superincumbent Liquid, exerts itself every Way, and every Way equally.

Which follows from the Nature of a Liquid, for its Parts yield to any Impression, and are easily moved; therefore no Drop will remain in its Place, if, whilst it is pressed by a superincumbent Liquid, it is not equally pressed on every Side: But it cannot be moved on account of the neighbouring Drops, which are pressed in the same Manner, and with the fame Force, by the fuperincumbent Liquid; and therefore the first or lowest Drop is at rest, and equally pressed on all Sides, that is, in all Directions.

Experiment 3. Plate XVIII. Fig. 2.] Let the Glass Tubes A, B, D, be immersed in Water, in the fame Manner as in the last Experiment; and, upon taking away the Finger, the Water will rife in all the Tubes to the same Height as in the Tube C: In C the Pressure is directed upwards, in B downwards, in A sidewise, and in D obliquely; yet the Pressure is equal in each. If you pour in a greater Quantity of Liquid into the Veffel, it will also rife equally in each Tube.

Hence it follows, that all the Particles of Liquids are pressed equally on all Sides, and therefore are at rest; and that they do not continually move among themselves, as several have supposed.

In Tubes that have a Communication, whether equal or unequal, whether streight or oblique, a Fluid rises to the same Height; that is, all the upper Surfaces are in the fame horizontal Plane; which is eafily deduced from what has been faid.

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le of the Tube, to that the Plate XVIII. Fig. 3.] Let A be a Vessel, and B a vertical Tube, and D an inclined Tube; they must communicate by Means of the Tube C, E: Let there be a Liquid poured into them, and let f g b be a Surface parallel to the Horizon. If the Heights f i and g l be unequal, the Water will ascend where that Difference is least. * For the * 274 fame Reason, unless the Pressures at g and b be equal, the Water will not be at rest; but they are equal when l and n are in the fame horizontal Plane: For fince the Pressure arises from the Gravity of the Parts, which tends towards the Center of the Earth, the Height of the pressing Liquid must be measured according to that Direction, that is, it will be b m; but the Obliquity of the Column bn causes no Change, because at the same Depth the Pressure every Way is equal. *

Experiment 4. Plate XVIII. Fig. 4.] Pour 278 Water into the Machine represented by Fig. 3. and after any Agitation it will not rest, unless all the Surfaces be in the same horizontal Plane. The Glass Vessel A is joined to the Glass Tubes B and D, by Help of the Brass Tube C E.

All Liquids are not equally heavy, that is, have not the same Quantity of Matter in the same Space; but what has been said will agree to every

Liquid by itself.

When Liquids of different Gravities are con-279 tained in the same Vessel, the heaviest lies at the lowest Place, and is pressed by the lighter, and that in Proportion to the Height of the lighter.

Experiment 5. Plate XVIII. Fig. 5.] Take Water tinged with some Colour, and pour it into the Glass Vessel A to the Height of bc; immerge into it the Glass Tube dE; the Water will

Oil of Turpentine, which is a Liquid lighter than Water, and immediately the Water will rife in the Tube; and so much the higher as the Oil is poured in, to a greater Height: Yet the Water in the Tube does not rise to the same Height as the Oil in the Vessel; because, since Water is heavier, there is not required the same Height of Water as there would be required of Oil to produce the same Pressure.

If you have a Mind to try this Experiment with Mercury and Water, you will find a greater Difference in their Heights, by reason of their

greater Difference of Gravity.

Experiment 6. Plate XVIII. Fig. 6.] Let the End of a Tube be immersed in Water, and pour Oil into it. The Water in the Tube is depress'd as far as d; yet the Height of the Oil de is greater than the Height of the Water in the Vessel. If the Tube be immersed deeper, the Water will run into it in greater Quantity; if you raise it up, the Water will again go out at a, and the Water in the Tube de sollow it, if it be raised to such a Height, that the Pressure of the Oil may overcome the Pressure of the Water in the lower Part of the Tube.

CHAP. II.

Of the Actions of Liquids against the Bottoms and Sides of the Vessels that contain them.

THE Bottom and Sides of a Vessel, which contain a Liquid, are pressed by the Parts of the Liquid which immediately touch them; and because Re-action is equal to Action,* those Parts all sustain an equal Pressure. But, as the Pression of Liquids

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Liquids is equal every Way, the Bottom and Sides are press'd as much as the neighbouring Parts of the Liquids; therefore this Action increases, in Proportion to the Height of the Liquid,* * 275 and is every Way equal at the same Depth, depending altogether upon the Height, and not at all upon the Quantity of the Liquid. Therefore, when the Height of the Liquid and Bigness of the Bottom remain the fame, the Action upon the Bottom is always equal, however the Shape of the Body be changed. In every Cafe the Preffure, fustained by the Bottom, is equal to the Weight of a Column of Water, whose Base is from the Bottom itself, and the Height of the vertical Distance of the upper Surface of the Water from the Bottom itself.

Plate XVIII. Fig. 7 and 8.] Take the hollow 281 Cylinder A, open at both Ends, and finely polished within, whose Diameter and Height also are about three Inches and an half; the Ring E is fastened to it by a Screw, so as it may be sustain-

ed by a Trevet.

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of ds Let the Cylinder have a moveable brass Bottom F, with which the brass Ring G, having a Screw in the Inside, is joined: This Ring retains and fixes a Leather Ring, broader than the Bottom, all round by half an Inch; this Leather covers the external Surface of the brass Ring when the Bottom is thrust into the Cylinder, and it hinders the Water from going out when it is moved up and down. This Leather must be soaked in Oil, and after a few Days it must be taken out and soaked as long in Water; after which Preparation the Leather must be well anointed with Oil and Water, and moved several times up and down the Cylinder, and left in it in that Condition two or three Days. When you are going to use the Machine

chine, you must anoint the Leather again with Oil and Water, then the Bottom will move easily, and hold Water. The Leather must be neither too thick nor too thin, which must be left to the

Judgment of the Workman.

The Bottom has in its Middle a small Brass Cylinder b i sastened to it, by which the Motion of the Bottom is directed; for this Cylinder goes thro' the Hole m in the Plate b, which is laid upon the larger Cylinder A, and let into it by a Cut in the Edge. In the upper Surface of the Cylinder b i there is a Cavity which contains a Screw, by which the Bottom is joined to the Brass Wire n p, which is carried through the Tube D, that the Bottom may be sastened to the Brachium of a Balance by the Help of this Wire.

Let the Cylinder A have the Cover C laid upon it; and, to hinder the Water from running out, the Mouth of the Cylinder must be cover'd with a Leather Ring, which is strongly pressed by the Screw which joins the Leather Cover to the Cylinder. To the Cover and Cylinder itself may be added a Handle, that the Cylinder may the more easily be shut and open'd. The Cover has a Hole in the Middle, and the hollow Cylinder 1, which has a Screw on the Outside, is fasten'd to it, that the Tube d may be joined to the Machine with a Leather upon the Screw, to hinder the Water from coming out.

Experiment 1. Plate XIX. Fig. 1.] Having joined together all the Parts of the Machine in the Manner just mentioned, hang upon one End of the Beam of a Balance the Brass Wire which is fixed to the moveable Bottom, so that the Beam may be exactly horizontal when the Bottom is two Inches distant from the Cover; then

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put such a Weight in the opposite Scale as will make an *Aquilibrium* with the Weight of the Bottom only. Let the Tube be one Foot long; and, the Beam of the Balance being placed horizontal, pour Water into the Tube D, so that it may rise up to its upper End; another Weight of 4. Pounds, being put into the upper Scale, will make an *Aquilibrium* with the Water; and, if you diminish or increase this Weight, the Bottom will move upwards or downwards. But you must observe, that, in altering the Weight, you must put in, or take out a pretty considerable Weight; for Example, half a Pound, because of the Friction of the Bottom.

The Diameter of the Bottom is almost 3: Inches, and the Height of the Top of the Water, in this Experiment, is 14 Inches; the Weight of a Pillar of Water of that Height, whose Base is equal to the Bottom, is 4: Pounds; and just so much does the Water press against the Bottom; tho' there be but a small Quantity of Water in the Machine.

Since only the Motion of the Bottom is to be observed, the Machine is to be fix'd down, lest it should be wholly raised; which is done by laying such Weights upon it as are represented by PP, Plate XX. Fig. 1.

Experiment 2. Plate XIX. Fig. 2.] Having taken away the Cover and the Tube, join the Cylinder A to the Vessel DE, which has at the Bottom a Ring with a Screw. Into this Machine pour Water upon the Bottom as high as in the foregoing Experiment; the rest of the Experiment is made in the same Manner as the former, and the Success is the same; for the Pressure is not changed, tho' you alter the Figure of the Vessel

Vessel and the Quantity of the Water, provided you keep the Water to the same Height.

Experiment 3. Plate XIX. Fig. 3. Hang the Cylindrick Vessel A to the End of a Balance. which Vessel must be fill'd in part by a wooden Cylinder De, which Cylinder is fixed any how to the Piece of Wood BC, and neither touches the Sides nor the Bottom of the aforefaid Veffel: if you pour Water into this Vessel to any Height, and make an Aquilibrium by putting Weights in the opposite Scale, that Weight will be the Weight of the whole Water which would be contained in the Vessel, the Cylinder being taken away, supposing it filled to the same Height as in the Experiment. And fo a finall Quantity of Water, whose upper Surface is raised, so as the Pressure against the Bottom be increased, will fustain a great Weight.

It will visibly appear, that the lateral is equal to the vertical Pressure, making use of the follow-

ing Machine.

282 Plate XIX. Fig. 4. The Vessel DB is a Parallelopiped of Wood about a Foot and a Half high; in the Side towards the Bottom there is a Hole in which there is a Brafs Ring containing a Screw, that the Cylinder A, mentioned in the first and second Experiments, may be screwed to it. Here you must take away the Trevet which fustained the Cylinder in those Experiments, and was fixed to the lower Ring by Screws. Now the Motion of the Bottom, in the Cylinder is horizontal. Two cross Pieces of Wood are joined to the Sides of this Machine, one of which is feen in GH; along them the Ruler CC is moved horizontally, which is wider in the Middle towards F, that by its Motion the Bottom of the Cylinder may be thrust inwards, which the

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the Ruler presses a little below the Center. At CC Ropes, as CE, are fasten'd to this Ruler, which are stretch'd along the Pieces as GH, and going over Pullies at the Extremities of the said Pieces, as T, have Weights joined to them, as P.

Experiment 4.] Pour Water into the Vessel BD, so that the Surface of the Water may be higher by 14 Inches than the Ruler GC; let the Weights, as P, be of 2 Pounds and a Quarter each; so that both taken together shall amount to 4 Pounds and a Half, the Pressure of the Water will sustain that Weight, and the Bottom in that Case will be moved with the same Ease towards either Part.

The following Experiment proves that the Force, with which Water presses upwards, is equal to that with which it presses downwards and sidewise.

to the vertical Preflute, making ale Experiment 5. Plate XX. Fig. 1.] In the Middle of the upper Surface of the Block or Foot B there is a Cylinder of about 2 Inches Diameter, on which you must put the moveable Bottom of the Cylinder A, so often mentioned; so that, the Bottom remaining fix'd, the Cylinder may be moved. The Cylinder must have its Cover on, and to it the Tube D, 3 Foot and a Half long, must be fastened; pour in Water, by which, the Bottom remaining fix'd, the Machine will be raifed; put the Weights PPP, which altogether weigh 9 Pounds, upon the Cover, and they, with the Weight of the whole Machine, will be fultained by the Water in the Tube; but the Weight of the Machine is more than 3 Pounds and a Half.

The Force, which acts against the Cover, is equal to the Weight of a Pillar of Water, whose

whose Base is the Cover, excepting the Hole to which the Tube is fix'd, and whose Height is the Height of the Water-Tube above the inward Surface of the Cover; which agrees with this Experiment.

If you apply the same Tube to a greater Machine, the Action against the Cover will increase in the same Ratio as the Cover; so that a prodigious Weight may be sustained, and even raised by a small Quantity of Water.

AB, AB, of 15 Inches Diameter, and join them together with a Piece of Leather, so that they may make a Cylindrick Vessel something like a Pair of Bellows, so that it may contain Water.

There is a Hole *l* in the upper Board, to which is fix'd a brass Cylinder that has a Screw, whereby the Tube D is fix'd to it, which is as long as the Tube used in the former Experi-

ment.

Experiment 6.] Pour Water into this Bellows thro' the Tube, and the Water in the Tube will fustain the Weights P, P, P, P, P, P, all which together weigh more than 250 Pounds. These Weights will even be raised by continuing to pour Water into the Tube.

Though these are Paradoxes, they follow from the Nature of Liquidity; every Drop, which is at rest, endeavours to recede every Way with 275 equal Force; * if therefore it be press'd on one Side, it endeavours to recede that Way with the same Force, because Action and Re-action are equal, and with that very Force itself will press every Way. In the first Experiment, the Water which touches the Bottom, and corresponds with the

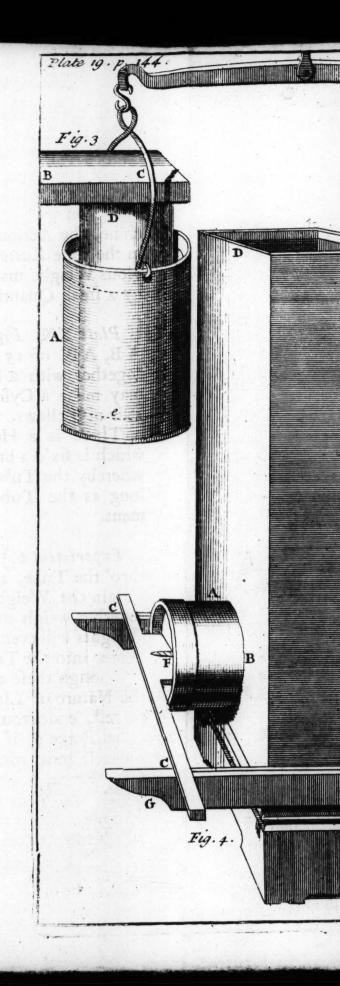
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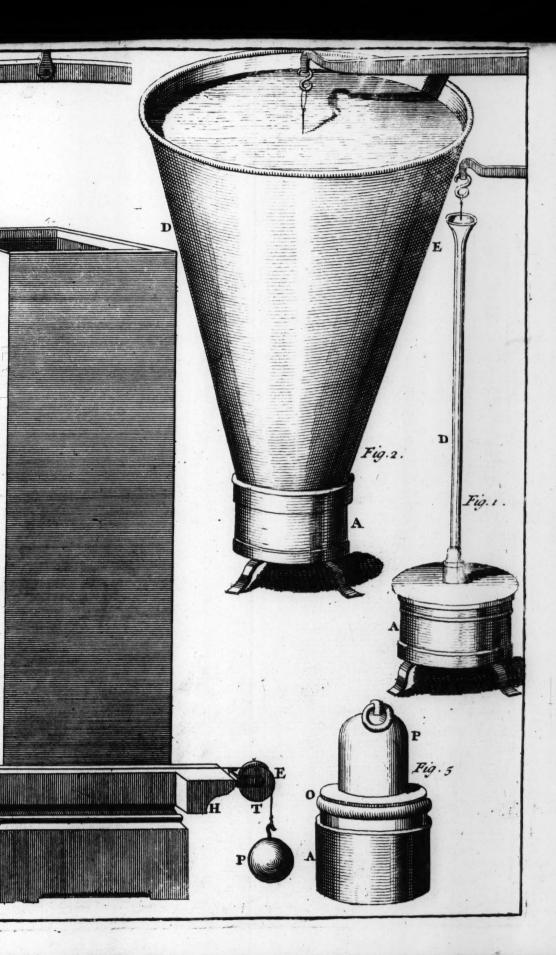
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Water contain'd in the Tube, and reaching quite to the Bottom, and presses the Bottom with such a Force, that it acts with the same Force upon the Water next to it; and since that Water cannot flow out against the Bottom, the Water next to that is also press'd with the same Force. The same may be said of the Water next to that; and so in all Parts of the Bottom there is a Pressure equal to that which lies under the Water in the Tube; and therefore the Bottom in this Case is as much press'd as if a Pillar of Water, of the same Height as the Water in the Tube, and of a Base equal to the Bottom, should lie upon it.

The fifth and fixth Experiments are illustrated

by the same Reasoning.

In the fecond Experiment, suppose that the Cylinder A should be continued, so as to reach up to the Surface of the Water; by this Means the external Water would be separated from the Water contain'd in this Cylinder, and then no Water but this interior Water would press upon the Bottom, and the Bottom would fustain it all. The Water in the Cylinder presses against the Sides of the Cylinder, and the external Water presses upon the external Surface of the Cylinder, and the outward Surface is press'd exactly in the fame Manner as the inward, and the Pressures against opposite Points are precisely equal; so that if the Surface was taken away, these Pressures would destroy one another; therefore it is no Matter, whether there be fuch a Surface or not, fo that taking it away (that is, taking away the Continuation of the Cylinder) the Action against the Bottom is no Way alter'd.

The third Experiment is also illustrated by what has been said; for the Weight placed in the Balance is not only sustain'd by the Water

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in the Vessel, but also by the Action of the inferior Surface in the Cylinder De against the Water.

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Tho' all that has been faid depends upon the Gravity of Liquids, their Actions must be distinguish'd from their Gravity, which last is always proportionable to the Quantity of Mat-

CHAP. III.

Of Solids immersed in Liquids.

WE have often faid, that the different Gravity of Bodies, whether Solids or Liquids, arises from this, that they contain a greater or less Quantity of Matter in an equal Space.

DEFINITION I.

284 The Quantity of Matter in a Body being confider'd in relation to its Bulk, that is, in relation to the Space posses'd by it, is call'd the Density of the Body.

A Body is faid to have double, or triple, &c. the Density of another Body, when, supposing their Bulks equal, it contains a double, or triple, &c. Quantity of Matter.

DEFINITION II.

285 A Body is said to be Homogeneous, when it is every where of the same Density.

DEFINITION III.

286 Heterogeneous, when the Density is unequal in different Parts of the Body.

DEFINITION IV.

287 The Gravity of a Body, considered with relation to its Bulk, is called the specifick Gravity of a Body.

The

The specifick Gravity is said to be double, when under the same Bulk the Weight is double.

Therefore the specifick Gravities and Densities 288 of Bodies, in homogeneous Bodies, are in the same Ratio; and they are to one another as the Weights of equal Bodies, in respect to their Bulk.

If homogeneous Bodies are of the same Weight, 289 their Bulks will be so much less as their Densities are greater, and under the same Weight the Bulk is diminished in the same Ratio in which the Density is increased; therefore in that Case the Eulks are inversly as the Densities.

When a Solid is immersed in a Liquid, it is press'd by the Liquid on all Sides, and that Pressure increases in Proportion to the Height of the Liquid above the Solid; as it follows from what has been said in the foregoing Chapter; and which may also be proved by a direct Experiment.

ther Bag S to the End of a Glass Tube B m, and fill it with Mercury; you may also make use of a Bladder; let this Bag be immersed in Water, but so, that the End B of the Tube may be above the Water; by the Pressure of the Water against the Surface of the Bag, the Mercury in the Tube will rise to m; and the Ascent of the Mercury follows the Proportion of the Height of the Water above the Bag.

When a Body is immersed in a Liquid to a great Depth, the Pressure against the upper Part differs very little from the Pressure against the under Part; whence Bodies very deeply immersed, are, as it were, equally press'd on all Sides; which Pressure may be sustained by soft Bodies, without any Change of Figure, and by very brittle Bodies without their breeking.

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ly. he Experiment 2. Plate XIX. Fig. 5.] Take a Fiece of foft Wax of an irregular Figure, with an Egg, and inclose it in a Bladder full of Water, and the Bladder being exactly shut must be put into a brass Box A; let it be covered with a wooden Cover O, so that it may be sustained by the Bladder, lay on a Weight P of 70 or 80 Pounds, and the Egg will not be broken, nor the Figure of the Way any Way sharged

Figure of the Wax any Way changed.

immersed in a Liquid in any Depth, will descend.
The inferior Part of the Body presses the Surface of a Liquid which it touches, and this Pressure is equal to the Weight of a Column made up of the Body itself and the superincumbent Liquid, and with this Force the Body is carried downwards. The Weight of a like Column, but which consists wholly of a Liquid, is the Force by which

* 290 the Body is press'd upwards by the Liquid.* But 275 when the Solid is supposed specifically lighter than the Liquid, this Force is less than that, and

therefore is overcome by it.

293 It is proved by the same Reasoning, That a Solid specifically lighter than a Liquid, and immersed into it, must ascend to the highest Surface of

the Liquid.

But suppose a Solid of the same specifick Gravity with the Liquid, it will neither ascend nor descend, but remain suspended in the Liquid at any Height, and the Liquid will sustain the whole Body; in which Case, by reason of the Equality of the specifick Gravities, the Liquid sustains a Weight equal to the Weight of the Quantity of the Liquid, which would fill the Space taken up by the Body. But a Liquid acts in the same Manner upon all equal Solids immersed to the same Depth, and will sustain

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Quar the restor fustain them equally; therefore they all lose Part of their Gravity.

DEFINITION V.

A Weight, which keeps a Body immersed in a Li-295

quid, is called its respective Gravity.

And this respective Gravity is the Excess of the 296 specifick Gravity of a Solid above the specifick Gravity of a Liquid; for since a Solid immersed 297 in a Liquid loses that Part of its Weight which is sustained by the Liquid, it loses the Weight of the Quantity of the Liquid, which could fill the Space taken up by the Body.

Experiment 3. Plate XXI. Fig. 1. Hang the hollow Brass Cylinder E to the Balance above-mentioned; * hang the solid Cylinder C of the same * 271 Metal by a Horse-hair to a Hook six'd to the Bottom, which, if it be put into the other Cylinder E, will exactly fill it; so that E, when it is full of Water, will contain such a Quantity of Water as will fill the Place taken up by C; put a Weight in the opposite Scale to make an Æquilibrium; let the Balance descend, that the Cylinder C may be immersed into the Water contained in the Vessel D; by that Means the Æquilibrium is destroyed, because C is partly sustained by the Water; but is restored, if E be fill'd with Water.

Hence it follows, that all equal Solids, but of 298 different specifick Gravity, when they are immersed into the same Liquid, they lose equal Parts of their Weight. The last mentioned Experiment will succeed in the same Manner with a Cylinder of any other Metal, and by pouring in the same Quantity of Water, that is, so much as will fill the Vessel E, the Æquilibrium will always be restored.

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qual will tain that however the Densities of equal Bodies differ among themselves, if they be immersed in the same Liquids, the Weight which they lose is in the Ratio of their Bulks, for the Spaces which they take up in a Liquid are in the same Ratio.

Therefore Bodies of the same Weight, but of different Densities, lose an equal Part of their Weight, when they are immersed in the same Liquid, because of the Inequality of their Bulks.

Experiment 4. Plate XX. Fig. 4.] Let two Pieces of Metal of the same Weight, the one of Gold, and the other of Lead, g, g, be suspended with the Hook VV of the Balance above-mentioned with Horse heir * and you will have an Figure

* 271 with Horse-hair, * and you will have an Æquilibrium; let the Balance descend, and the Bodies g, g, be immerged in the Water contained in the Vessel F F, and the Æquilibrium will be destroyed. When a Solid, specifically heavier than a Liquid, is suspended in a Liquid, the Liquid acts on every Side against that Solid, in Propor-

* 290 tion to its Weight, * and the Solid re-acts equally against it; therefore those Actions are the same as if the Space taken up by the Solid were fill'd

with the Liquid; therefore it is no Matter, in respect of the Gravity of the Liquid, whether a Solid, specifically heavier than the Liquid, be suffered in it, or a Quantity of the Liquid be poured in, which takes up a Space equal to the Solid.

Experiment 5. Plate XXI. Fig. 2.] Take the Vessel A containing Water, hang it to one End of the Balance, immerge into it the Brass Cylinder C, which is sustained by a Horse-hair, lest it should touch the Bottom of the Vessel, putting a Weight into the opposite Scale, and you will have an Æquilibrium; take the Cylinder Court

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d of the Water, the Æquilibrium will be destroyed: and it will be restored again by pouring in Water as much as can be contained in the hollow Cylinder E, which will be exactly filled by the fol-

lowing Cylinder C.

By comparing together the Numb. 297 and 301 300, as also the third and fifth Experiments, which confirm them, it appears, that a Liquid acquires the Weight which the immersed Solid loses. The Force of Gravity is always proportionable to the Quantity of Matter, and is not changed by the Immersion of a Solid into a Liquid; wherefore the Sum of the Weight of the Solid, and of the Liquid, do not differ before and after the Immersion.

Experiment 6. Plate XX. Fig. 5.] Hang the Solid C to the Balance, and make an Æquilibrium, by putting into the opposite Scale B the Weights P and p, of which p is equal to the Weight which the Body C loses in Water. Take the Vessel E, which contains Water, and is suspended to the Balance EF, and, putting a Weight into the opposite Scale, make an Æquilibrium here also; let the Balance descend with the Body C, that it may be immersed in the Water contain'd in D, by this Means you will destroy the Æquilibrium in both Balances, which will be restored by taking out of the Scale B the Weight p, and putting it into the Scale of the Brachium F.

A Body specifically heavier than a Liquid, and 302 which descends in it, is carried downwards with a greater Force than it is pressed upwards, as has been explained before*; the Difference of which * 292 Forces is the respective Gravity of the Body.

The first Force in part consists of the Weight of the Liquid incumbent over the Body, and the Body may be immersed to such a Depth, that

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that Weight shall be equal to the above-mentioned specifick Gravity: If in that Case you take away

303 the superincumbent Liquid, the Body will be sustained by the Pressure of the Liquid under it. If the Body immersed to a greater Depth, and the Liquid be also hindered from passing upon the upper Surface of the Body (because the Pressure, by which a Body is pushed up, increases as the

290 Depth to which it is immersed)* the Body then will be carried upwards with greater Force than downwards by Gravity; wherefore, if it could

move freely, it would afcend.

Experiment 7. Plate XXI. Fig. 3.] To the Cylinder C, which is open at both Ends, apply at Bottom the Plate of Lead F, a Quarter of an Inch thick; if it fits so exactly to the Cylinder as to let no Water slip by, and the Plate be held up by a Thread sastened to the Hook V in the Center of the Plate, until it be immersed with the Cylinders to the Depth of about 3 Inches, the Lead will be sustained by the Water, as appears by letting go the Thread. If you immerge it to a greater Depth, it will stick closer to the Cylinder; but if to a less, it will fall off.

If this Experiment was made with a Plate of Gold, it ought to be immerfed to a greater Depth; for the specifick Gravity of Gold is to the specifick Gravity of Water as 19 to 1; and therefore its respective Gravity is to that of Wa-

Water equal in respective Gravity to the Plate of Gold, that Pillar must be above 18 times its Height; and therefore the Height of the Water, above the upper Surface of the Plate of Gold, must be at least equal to as many times its Thickness.

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Experiment 8. Plate XXI. Fig. 3.] Take a Cylinder A with a moveable Bottom, that has also a Cover with the Tube D joined to it, as was before described; * immerge it in Water, and when * 381 it comes to be a Foot under Water, the Bottom will rise, altho' it weighs a Pound and a Quarter, and has P a Pound Weight screwed to it at Bottom.

If the same Solid be immersed into Liquids 304 of different Density, it will lose different Parts of its Weight; * And therefore, when two Bodies * 297 of the same Density and Weight are immersed in Liquors of different Density, they will lose their

Æquilibrium.

Experiment 8. Plate XXI. Fig. 4.] Take two flat Pieces gg, of the same Metal and equal, and hang them upon the Hooks V V of the Scales A and B; then by the Descent of the Balance immerge them in the Liquids contained in the Vessels FF, the one in Water, the other in Oil of Turpentine, and the Æquilibrium will be destroyed, the Piece which was immersed in Oil becoming lighter.

A Solid lighter than a Liquid, and immersed in 305 it, ascends and remains at the upper Part of the Liquid, * so as to be immersed only in Part; but * 293 the greater is its specifick Gravity, the more it descends, and the Body will not be at rest till the immersed Part takes up such a Space in the Liquid, that the Bulk of the Liquid, which would fill that Space, shall weigh as much as the whole Body. For in another Case the Solid does not act with the same Force against the neighbouring Parts of the Liquid, as the Liquid would act, if it should take up the Place of the Body; therefore in this Case alone the Liquid and the Body can be at rest. * * 2

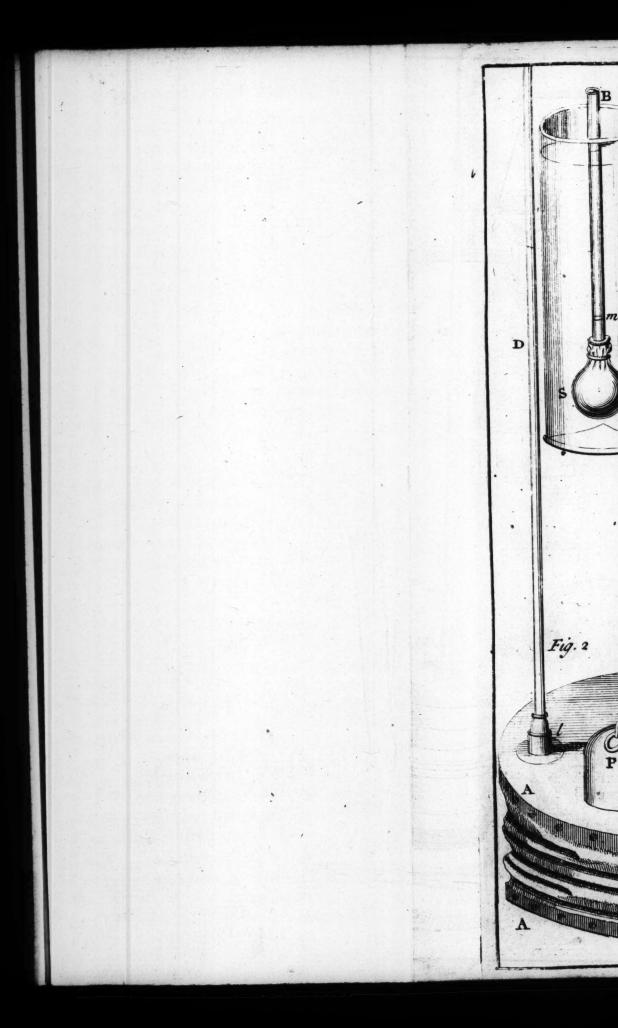
It follows from this Proposition, that the immersed Parts of the Bodies, swimming on the Surface of the same Liquor, are to one another as the Weights of the Bodies. Therefore if, by superadding a Weight, the Gravity of the Body is changed, the immersed Part is increased in the same Proportion, and the Parts, which descend into the Liquid by laying on of different Weights, are to one another as those Weights.

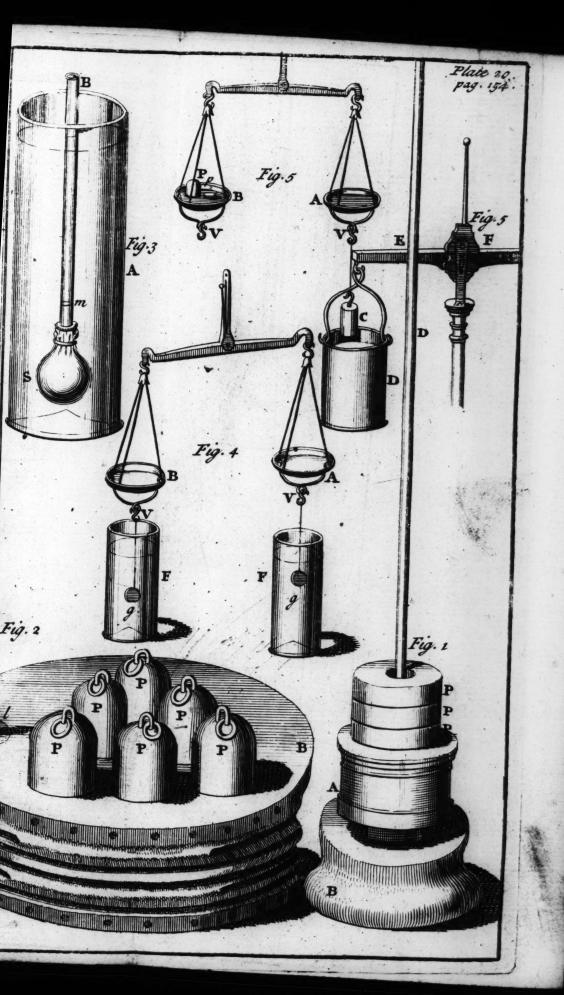
Experiment 10. Plate XXII. Fig. 1.] Take a Vessel A containing Water in it; let C be a hollow Cylinder of any Metal; lay upon it the Weight p, that it may descend into the Water with its Part bd; adding the Weight of one Pound, measure how far it will descend; then adding another equal Weight, you will find that it will descend equally every Time.

In Numb. 302 and 303, confirmed by the Experiments 7 and 8, it appeared how a Body, specifically heavier than a Liquid, may be made to swim; by the same Method a Body, specifically lighter than a Liquid, may be retained at the Bottom: In that Case the Pressure of the super-incumbent Water is taken off; but here you must take off the Pressure of the inferior Water whereby the Body is pushed upwards.

Experiment 11. Plate XXII. Fig. 2.] Upon the Foot D, which is fixed at the Bottom of the Vessel A, there is a Brass Plate b c exactly flat and polished; there is another Brass Plate b c, like the former, fastened to a large Piece of Cork E, so that together with the Cork it shall make up a Body specifically lighter than Water: Lay this Plate upon the other, so that they may sit, and keep the Cork down with a Stick while you pour in Water; leaving the Cork, it will not ascend until, by moving it out of its Place, the

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the Plates are separated, so that the Water may exert its Pressure against the Plate joined with the Cork, and push it upwards together with the Cork.

CHAP. IV.

Of the Manner of comparing the Densities of Liquids.

Ince the Density of Bodies is in Proportion 309 to their Gravity, by comparing the Weights of equal Bodies we discover their Densities. * If * 288 therefore any Vessel be exactly filled with a Liquid, and that Liquid be weighed; and if you make the same Experiment with other Liquids, their Weights will be as their Densities. But, as this Method is liable to several Difficulties in Practice, I shall not spend any Time in explaining it here.

When the Pressures of two Liquids are equal, 310 the Quantities of Matter, in Columns that have equal Bases, do not differ; * wherefore the Bulks, * 273 that is, the Heights of the Columns, are inversty as the Densities; * whence may be deduced the * 289

Method of comparing them together.

Experiment 1. Plate XXII. Fig. 3.] Pour Mercury into a curve Tube A, so as to fill the lower Part of the Tube from b to c; pour in Water in one Leg from b to e; in the other Leg pour in Oil of Turpentine, till both the Surfaces of the Mercury bc be in the same horizontal Line, and the Height of the Oil be cd: These Heights will be as 87 to 100, which is the inverse Ratio that the Density of the Water has to the Density of Oil of Turpentine; and therefore these Densities are to each other as 100 to 87.

The Mercury is poured in, lest the Liquids should be mix'd in the Bottom of the Tube.

The Densities of Liquids are also compared together, by immerging a Solid into them; for if a

ther, be immersed successively into different Liquids, the immersed Parts will be inversely as the Densities of the Liquids; for, because the same Solid is made use of, the Portions of the different Liquids, which in every Case would fill the Space taken up by the immersed Part, are of the same

* 505 Weight; * therefore the Bulks of those Portions, that is, the immersed Parts themselves, are in-

* 289 versely as the Densities. *

Plate XXII. Fig. 4.] Take the Glass A, which is a hollow Ball that has a Tube divided into equal Parts; at the Bottom of the great Ball there is: a small one, Part of which is fill'd with Mercury, or very fmall Shot, whose Weight ferves to make the Tube descend vertically in Liquids, and stand in that Position: Care must be taken not to have too much Weight in the little Ball, for the whole Glass must be lighter than the Liquids to be compared together. The Hydrometer, (for fo it is call'd) descends to different Depths in different Liquids; and those Densities, as we have already faid, are inverfely as the Parts immerfed, which therefore are to be compared together. Tie a Thread to the Hydrometer, and weigh it together with the Thread; the Weight (if it be like mine) will be 573 Grains; if put into Water, it will descend to b; therefore a Bulk of Water, equal to the immersed Part of the Hydrometer, weighs * 305 573 Grains, * and may be express'd by that Number. Fasten the Thread above-mention'd to the

ber. Fasten the Thread above-mention'd to the Hook V of the Scale A of the Balance represented in *Plate* XVIII. Fig. 1. the Hydrometer

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remains immersed; put 20 Grains in the Scale B, and let the Weight P be moved gently to raife the Balance (by which the Tube will be drawn a little Way out of the Water) 'till there be an Æquilibrium, and the Surface of the Water then will be given with the Point d; the Water fustains the Weight of the whole Machine, except 20 Grains, that is, it fustains 553 Grains; and the Weight of the same Bulk of Water, which is now immersed, weighs just so many Grains, and is expressed by that Number; wherefore one may call the Bulk of the Parts db of the Tube 20; if the Space db be divided into 10 equal Parts, and you continue the Divisions upwards beyond b, and downwards below d, each Division may be called 2; and by observing the Division to which the Instrument descends in a Liquid, you will have the Bulk of the immersed Part; so, if the whole Tube stands out above the Water, the immersed Bulk will be 549; if it rises to the upper Divisions, the immersed Bulk will be 579; and the Densities of the Liquids, in which this happens, will be inversly as those Numbers, that is, as 579 to 549, and only the intermediate Densities may be compar'd by this Instrument; if the Ball was less in Proportion to the Tube, it would ferve for comparing together Liquids whose Densities differ more than this. When feveral Liquids are compared together, the Numbers which express the Bulk of the immersed Parts are the Denominators of Fractions, which have I for their Numerator; and thefe Fractions express the Ratio of the Densities; for they are to one another inversly as the Denominators.

Experiment 2.] Let the Densities of Waters, containing different Quantities of Salts, be to be com-

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compared, the Hydrometer descends in the one to the Division a; if it be immersed in another, it only descends to the Division c, their Densities will be to one another as 300 to 505, as may be eafily deduced from what has been faid.

This Method is also liable to several Difficulties besides this, that it is difficult to compare together Liquors very different in Denfity by the

fame Hydrometer.

313 The best Method of all is, to make use of a Solid heavier than the Liquids. When the same Body is immersed in different Liquids, the Weights, which it loses in the Liquids, are to each other as

*297 288 *271

the Densities of those Liquids.* Here you must use a hydrostatical Balance, * and besides a solid Piece of Glass, as C, which may hang to one of the Scales by a Horse-hair, Plate XXI. Fig. 5 and 6, you must have a Weight, as P, which æquiponderates with the Glass C, when it is immersed in Water, as is represented in Fig. 4. The Difference between the Weight P, and the Weight of the Glass C, when it is taken out of the Water, is the Weight which the Body has loft, when weigh'd in Water: This must be obferved, that it may ferve in all the Experiments; in our Balance it weighs 722 Grains. Suspend the Fody in any other Liquid, unless it be of the fame Density as Water, the Æquilibrium will not be preserved: Let it be restored by putting Grain Weights in either of the Scales; if they be put into the Balance A, add them to the above-mentioned Difference of 722 Grains if the Weights be put into B, substract them from that Number; and by that Means in each of those Cases, as it appears, the Weight lost by a Body is determined, that is, the Weight which expresses the Denfity of the Liquid.

Experi-

Experiment 3.] Let the Weight C, which hangs from the Scale A, be immerfed in Oil of Turpentine, whilst the Weight P hangs from the Scale B; put 94 Grains in the Scale B, and you will have an Æquilibrium. Then immerge the same Weight in Milk, that the Balance may return to an Æquilibrium, a Weight of 22 Grains must be put in the Scale A. Substracting the first Number from 722, and adding the second to it, you will have 628 and 744, expressing the Densities of the above-mentioned Liquids, whilst 722 shews the Density of the Water itself.

CHAP. V.

Of the Hydrostatical Comparison of Solids:

I N all homogeneous and equal Bodies, the Densities are as the Weights;* in unequal *288 Bodies of the same Weight, the Densities are inversely as the Bulks*; if therefore both the Bulks *289 and the Weights differ, the Ratio of the Densities is compounded of the direct Ratio of the Weights, and the inverse Ratio of the Bulks; and therefore, dividing the Weights by the Bulks, 315 you have the Densities, that is, you will have Numbers that are to each other as those Densities.

The Weight of all Bodies may be compared by 316 Means of the Balance; the Bulks are found by immerging Bodies in the same Liquid; for the Weights, which they lose, are as the Bulks.*

Plate XXI. Fig. 7.] Here also the hydrostati-317 cal Balance is to be used,* as likewise the Glass *271 Vessel D, in which the Bodies to be compared are to be placed; you must also have such a Weight as is represented by P in Fig. 6. that is equal to the Weight

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Weight of D; and lastly, the Weight p (Fig. 8.) equal to the Weight which the Glass D loses,

when it hangs in the Water.

With a Horse-hair you must fasten the Glass D in the Place of the Body C (Fig. 4.) in the Scale A, and hanging the Weight P in the Scale B, you will have an Æquilibrium. The Body, whose Denfity is required, is placed in the Glass D (as we have faid before) and weighed, the Vessel and Body being immerfed in Water; putting the Weight p into the Scale B, the Æquilibrium is restored in respect to the Glass D; you must add as much Weight besides as is required to make an Æquilibrium, and that will be the Weight loft by the Body weighed; by this Weight therefore you must divide the Weight of the Body itself,

315 to have the Denfity.*

Experiment 1.] A Piece of Gold, weighing 137 Grains, lost in Water 7 4 Grains. A Piece of Silver, weighing 248 Grains, lost in Water 24 Grains. Therefore their Densities are as 18 16 to 10; that is nearly as 11 to 6. By fastening a Body whose Density is required, and is heavier than a Liquid, to a Body lighter than the Liquid, the Density is also discover'd.

Plate XXII. Fig. 5.] Take the Machine A, like the Machine describ'd in the preceding Chap-312 ter,* and let it have fix'd to its Bottom the Ring DE, and to its Top the Ring FG; then the Ball will, by its own Weight, be in part immerg'd This Machine cannot be apply'd to in Water. Use, unless you know by some other Method, how much of its Weight any Body loses in Water; therefore we lay down as known, that 109 Grains of Lead weigh in Water but 100 Grains; therefore lay just as many Grains upon the Ring

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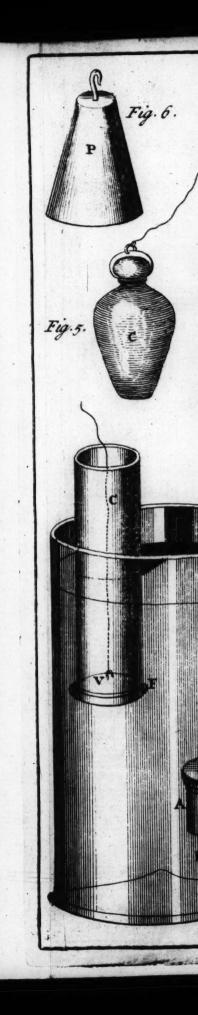
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D E as will make the Machine, when immerg'd in Water, descend to a; lay what Number of Grains you please upon the Ring FG; for Example, Eight, and the Machine descends to c; the Space a c must be divided into Eight Parts, and the Divisions must be continued upwards and downwards; if you make a the hundredth Division, c will be the hundred and eighth Division, and the lowest of all in this Figure will be the 97th. Tis plain, that if the Proposition of Num. 307 be compar'd with the aforefaid Preparation, the Division, to which the Machine descends in Water, shews the Weight of the Grains which press down the Machine; therefore laying a Body upon the Ring D E, its Weight in Water will be determin'd; by fubstracting this Weight from its Weight out of the Water, you will have the Weight loft in the Water; by which if the Weight out of the Water be divided, the Density is discover'd, as has been faid in the Beginning of this Chapter.

Experiment 2.] Lay a Piece of Brass, weighing, for Example, 100 Grains, on the Ring D E by which the Ball of the Machine is not immerg'd; lay any Weight, for Example, of 17 Grains, on the Ring F G, and the Machine descends to b, that is, to the 105th Division; which proves, that the Machine is press'd down by so many Grains; from this Number of Grains fubfract the 17 last mentioned, the remaining 88 are the Weight of the Piece Brass in Water, which therefore loses 12 Grains. If again, the Weight 100 Grains be divided by the 12 Grains, you have 8; expressing the Density of the Brass. the Densities of any other Bodies may be found after the fame Manner.

This Method has feveral Difficulties. The

foregoing is the best of all.

CHAP. M

CHAP. VI.

Of the Resistance of Fluids.

A LL Bodies moved in Fluids suffer a Resistance, which arises from two Causes. The first is the Cohesion of the Parts of the Liquid. A Body in its Motion, separating the Parts of a Liquid, must overcome the Force with which those Parts cohere, and thereby its Motion is retarded.

ter, that belongs to all Bodies, which is the Reafon, that a certain Force is required to remove the Particles from their Places, in order to let the Body pass. The Body acts upon the Parts to remove them, and they diminish its Motion by Re-action.

The Retardation from the first Cause, that is, the Cohesion of Parts, is always the same in the same Space, the same Body remaining, be the Velocity of the Body what it will. The same Cohesion is to be overcome in every Case; therefore this Resistance increases as the Space run through, in which Ratio the Velocity also in-

*53 creases; * therefore it is as the Velocity itself.
321 The Resistance arising from the Inertia, or Inactivity of Matter, when the same Body moves through different Liquids with the same Velocities, follows the Proportion of the Matter to be removed in the same Time, which is as the Density of the Liquid.

when the same Body moves thro' the same Liquid with different Velocities, this Resistance increases, in Proportion to the Number of Particles struck in an equal Time, which Number is as the Space run through in that Time, that is, as the Velocity. But this Resistance does farther increase, in Proportion to the Force with which the Body runs against every Part; which Force is also as

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the Velocity of the Body. And therefore, if the Velocity is triple, the Resistance is triple from a triple Number of Parts to be removed out of their Places. It is also triple from a Blow three times stronger against every Particle; therefore the whole Resistance is ninefold, that is, as the

Square of the Velocity.

A Body therefore moved in a Liquid is refifted 323 partly in a Ratio of the Velocity, and partly in a duplicate Ratio of it. The Resistance from the Cobesion of Parts in Liquids, except glutinous ones, is not very sensible in respect of the other Resistance; which as it encreases in a Ratio of the Square of the Velocities, * but the first in a Ratio of the * 222 Velocity itself: * By how much the Velocity in- 220 creases, by so much more do these Resistances differ amongst themselves; wherefore, in swifter 324 Motions the Resistance alone is to be considered, which is as the Square of the Velocity.

I shall not now treat of tenacious or glutinous Liquids, nor of slow Motions, in which the Resistance, arising from the Cohesion of the Parts,

must be considered.

If a Liquid be included in a Vessel of a prismati- 225 cal Figure, and there be moved along in it with equal Velocity, and a Direction parallel to the Sides of the Prism, two Bodies, the one spherical and the other cylindric, so that the Diameter of the Base of this last be equal to the Diameter of the Sphere, and the Cylinder be moved in the Direction of its Axis, these Bodies will suffer the same Resistance. To demonstrate this, suppose the Bodies at rest, and that the Liquid moves in the Vessel, with the same Velocity that the Bodies had; by this the relative Motion of the Bodies and the Liquid is not changed, therefore the Actions of the Rodies on the Liquid, and of the Liquid on the Bodies, are not changed. The Retardation which the Liquor M 2

fuffers in passing by the Body, arises only from this, That in that Place it is reduced to a narrower Space, but the Capacity of the Vessel is equally diminished by each Body; therefore each Body produces an equal Retardation. And because Action and Re-action are equal to one another, the Liquids acts equally upon each Body; wherefore also each Body is equally retarded, when the Bodies are moved, and the Liquid is at rest.

Vessel be supposed much bigger; and it will do in an infinite Liquid compressed; therefore it may be referred to Bodies deeply immersed. Here we speak of a continuous Liquid, and whose Parts cannot be reduced into a lesser Space by Pressure; otherwise there will be an Accumulation before the Body, and a Relaxation behind;

and so much the more, the more blunt the Body 327 is; which also causes a greater Irregularity in the Motion of the Liquid, and a greater Retardation

in the Motion of the Body.

When a Body is moved in any Liquid along the Surface, the Liquid is raised before the Body, and depressed behind; and these Elevations and Depressions are greater, the more blunt the Body is, and by that Means it is more retarded; for there is also a greater Irregularity in the Motion of the

Retardation of the Body, This is also true, if the Body be not immersed deep; yet in that Case the Irregularity of the Motion of the Liquid is the chief Cause of the Retardation.

Therefore, to take away these Irregularities, we must consider Bodies as deeply immersed, and give Rules relating to them; by which the Retardations in several Cases may be compared together. We suppose the Bodies spherical, tho' the De-

monstrations will serve for all similar Bodies moved in the same Manner.

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differ Dens Here you must observe, that the Resistance is to 329 be distinguished from the Retardation; the Resistance produces the Retardation. When we speak of the same Body, the one may be taken for the other, because they are in the same Proportion; but, supposing the Bodies different, the same Resistance often generates different Retardations. From the 330 Resistance arises a Motion contrary to the Motion of the Body; the Retardation is the Celerity, and the Resistance itself is the Quantity of Motion.

Let the Bodies be equal, but of different Densi-331 ties, and moved thro' the same Liquid with equal Velocity, the Liquid acts in the same Manner upon both; therefore they suffer the same Resistance, but different Retardations; and they are to one another as the Celerities, which may be generated by the same Forces in the Bodies proposed; * that is, they are inversly as the Quantities * 330 of Matter in those Bodies, * or inversly as the * 60

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Now, supposing Bodies of the same Density, but 331 unequal, moved equally fast thro' the same Fluid, the Resistances increase according to their Superficies, that is, as the Squares of their Diameters; the Quantities are increased in Proportion to the Cubes of the Diameters; the Resistances are the Quantities of Motion, the Retardations are the Celerities arising from them; * dividing the * 330 Quantities of Motion by the Quantities of Matter, you will have the Celerities; * therefore the Retardations are directly as the Squares of the Diameters, and inversely as the Cubes of the Diameters, that is, inversely, as the Diameters them-selves.

If the Bodies are equal, move equally swift, 332 and are of the same Density, but are moved thro' different Liquids, their Retardations are as the * 339 Densities of those Liquids.*

M 2 When 322

334 When Bodies, equally dense and equal, are carried thro' the same Liquid with different Velocities, the * 324 Retardations are as the Squares of the Velocities. *

From what has been faid, the Retardations of any Motions may be compared together, for they

* 334 are first, as the Squares of the Velocities; * secondly, as the Densities of the Liquids thro' which * 333 the Bodies are moved; thirdly, inversly as the Di-

* 332 ameters of those Bodies; lastly, inversly as the

* 331 Densities of the Bodies themselves. *

The Numbers in the Ratio, compounded of those Ratio's, express the Proportion of the Retardations. Multiplying the Square of the Velocity by the Density of the Liquid, and dividing the Product by the Product of the Diameter of the Body multiplied into its Density, and working thus for several Motions, the Quotients of the Divisions will still have the same compound Ratio to one another.

These Retardations may also be compared together, by comparing the Resistance with the 336 Gravity. It is demonstrated; that the Resistance of a Cylinder, which moves in the Direction of its Axis, (to which the Resistance of a Sphere of the same

Diameter is equal, *) is equal to the Weight of a Cylinder made of that Liquid, thro' which the Body is moved, having its Base equal to the Body's Base, and its Height equal to half the Height, from which a Body falling in Vacuo may acquire the Velocity with which the said Cylinder is moved thro' the Liquid. From the given Celerity of the Body moved, the Height of the Liquid Cylinder is found, as also the Weight of it from the known specifick Gravity of the Liquid and Diameter of the Body. Let a Ball, for Example, of 3 Inches Diameter be moved in Water, with that Celerity with which it would go thro' 16 Foot in a Second: From what has been faid of falling Bodies

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Bodies and Pendulums,* as also by Experiments made on Pendulums, it has been found that this is the Celerity which a Body acquires in falling from a Height of 4 Foot; therefore the Weight of a Cylinder of Water, of 3 Inches Diameter, and 2 Foot high, that is, a Weight of about 6 Pounds and 3 Ounces, is equal to the Resistance of the aforesaid Ball.

Let the Resistance so discovered be divided by the Weight of the Body, which determines its Quantity of Matter, and you will have the Retardation.* By which Rule the Proportion of the several Retardations is discovered, * and found to be the same as is given by the foregoing Rule.

Having considered the Retardations of direct Motions, we pass on to the Motion of Pendulums.

The Arc described by a Pendulum oscillating in Vacuo, with a Celerity that it has acquired by descending, is equal to the Arc which is described by the Descent; * the same does not happen in a Liquid, and there is a greater Difference between those Arcs, the greater the Resistance is; that is, if you speak of the same Liquid and Pendulum, the greater the Arc is which is described in the Descent.

Let the Resistance of the Liquid be in Proportion to the Velocity, and two Pendulums, entirely alike, oscillating in a Cycloid, perform unequal Vibrations, and begin to fall the same Moment; they begin to move by Forces that are as the Arcs to be described; if those Impressions alone, which are made the sirst Moment, be considered, after a given Time, the Celerities will be in the same Ratio as in the Beginning; for the Retardations, which are as the Velocities themselves, and change their Proportions, for the Ratio between Quantities is not changed by the Addition and Substraction of the Quantities in the same Ratio. Therefore M 4

in equal Times, however the Celerities of Bodies are changed in their Motion by the Refistance, Spaces which are gone thro' are as the

*53 Forces in the Beginning; * that is, as the Arcs to be described by the Descent; therefore after any Time the Bodies are in the correspondent Points of those Arcs. But in these Points the Forces are

156 generated in the same Ratio as in the Beginning,
and the Proportion of the Celerities, which is not
varied by the Resistance, suffers no Change from
the Gravity. In the Ascent, Gravity retards the
Motion of the Body, but in correspondent Points
its Actions are in the same Ratio as in Descents.
And therefore every where in correspondent Points
the Celerities are in the same Ratio. But as in
the same Moments the Bodies are in these correspondent Points, it follows that the Motion of
both is destroyed in the same Moment, that is,
they finish their Vibrations in the same Time. The
Spaces, run thro' in the Time of one Vibration,
are as the Forces by which they are run thro';

340 that is, the Arcs of the whole Vibrations are as the Arcs described by the Descent, whose Double are the Arcs to be described in Vacao. The De-

341 feets of the Arcs to be described in Liquids, from the Arcs to be described in Vacuo, are the Differences of Quantities in the same Ratio, and are as

the Arcs described by the Descent.

Since there is the same Proportion between those different Arcs, it follows, that the Celerities, in the correspondent Points of the Arcs described, are every where as the Arcs described by the Descent; for these correspondent Points are also the correspondent Points of the Arcs to be described in Vacuo, in which we have demonstrated that this Proportion holds.

Now let the Resistance increase in the duplicate
Ratio of the Velocity, and let the Pendulum perform
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unequal Vibration, the greatest will last the longest, because the Resistance increases more than in the

Cafe Numb. 239.

Yet the Celerities, Supposing the Arcs not very 344 unequal in the correspondent Points of the Arcs described, are every where nearly in the same Ratio, and indeed in the Ratio of the Arcs described by the Descent. If the Resistance was in the Ratio of the Celerity, this Proportion would obtain; * but now it is disturb'd by reason of 342 a greater Resistance in a greater Vibration, by which the Motion in this is more diminish-But it is more accelerated by two Causes, 1st, this greater Vibration lasts longer,* and the *343 Body stays longer in a certain Space, than in the correspondent Space in a less Vibration, and is accelerated during a longer Time. 2dly, the Defect of the Arc described here, from an Arc to be described in Vacuo, is greater in Proportion, in a greater Vibration, because in this the Refistance differs more from the Resistance in a less Vibration, than in Numb. 241. therefore the correspondent Points, keeping the same Proportion, are more distant from the lowest Point in the greater than in the lesser Arc, as long as the Body descends in it: therefore in Proportion it has a great er Acceleration, because the Force, which acts continually on the Body, is as its Distance from the lower Point; * therefore there is a Compensation, *156 and the Proportion above-mentioned is restored. In the Ascent of the Body, the Duration of the Retardation concurs with the Resistance to disturb that Proportion; but now the correspondent Points are less distant from the lowest Point in the greater Arc (the fame Proportion continuing) than in the leffer, and the Gravity in Proportion produces a less Retardation;

therefore now (the Proportion continuing) the Difference of the Distance of the correspondent Points from the lowest Point is increased, so that

a Compensation is given from this alone.

The Refistances which are as the Squares of the Celerities, and therefore every where in correspondent Points, as the Squares of the Arcs described by the Descent, in which Ratio also the *329 Retardations are; * but, as each of them keep the fame Proportion in corresponding Points, the Sums of them all will be in the same Proportion; that is, the whole Retardations, which are the Defects of the Arcs described in the Liquid from the Arcs to be described in Vacuo; or, what is the same, the Differences between the Arcs described in the Descent and the next Ascent. Therefore these Differences, if the Vibrations are not very unequal, are nearly as the Squares of the Arcs described by the Descent. Which is also confirmed by Experiments in greater Vibrations; for in these the Proportion of Refistance, which we treat of here, ob-

324 tains.

346

Fill the wooden Vessel ABFCD, (Plate XXII. Fig. 6.) 3 Foot long, I Foot wide, and I Foot high, with Water; hang up the Pendulum V p by a Hook V hanging over the Middle of the Veffel; this Pendulum is made of an Iron Wire 7 or 8 Foot long, and a Leaden Ball p of the Diameter of an Inch and a Half; when the Pendulum is at rest, the Ball is distant 3 Inches from the Bottom of the Vessel. At P there is a greater Ball of Lead, of 3 Inches Diameter, joined to the Iron Wire, that the Ball P may be the less retarded in Water.

A-cross the Top of the Vessel, upon the Brim of it, may be moved a Board about 5 Inches high, to which must be applied the divided Brass Rulers E G, E G, and the Indices M, M, for meafuring

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aris of t rate measuring the Angles described by the Pendulum in the Descent, or Ascent, by the Method given Numb. 170. Page 70.

Experiment.] Let the Rulers E G, E G, be so disposed, that the Ends G, G, may be overagainst the Pendulum when it is at rest, and in such Manner that between their Ends there may be a Distance equal to the Diameter of the Wire to which the Bodies Pp are fixed. Let one Index be applied to the 16th Division of the Ruler, and another to the 14th Division of the other Ruler; let the Pendulum sall from that Division, and it will rise almost to this. If, instead of these Divisions, you take 20 and 16 \(\frac{7}{2}\), the Experiment will succeed in the same Manner, as also when you apply the Indices to the Divisions 24 and 19 \(\frac{1}{2}\). Take care that the Water be perfectly at rest.

In this Experiment the Arcs described in the Descent are to one another as 4, 5, and 6, whose Squares are 26, 35, 26; the Difference of those Arcs, from the Arcs described in the Ascent, are 2, 3 \frac{1}{8}, 4 \frac{1}{2} which Numbers are to one another as the aforesaid Squares, as appears by multiply-

ing them by 8.

A Body freely descending in a Liquid is accele-347 rated, by the respective Gravity of the Body which continually acts upon it; yet not equally as in a Vacuum,* the Resistance of the Liquid occasions * 129 a Retardation, that is, a Diminution of Acceleration, which Diminution increases with the Velocity of the Body. For there is a certain Velocity 348 which is the greatest that a Body can acquire by falling; for if its Velocity be such, that the Resistance arising from it becomes equal to the respective Weight of the Body, its Motion can be no longer accelerated; for the Motion which is continually generated

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nerated by the respective Gravity, will be destroyed by the Resistance, and the Body forced to go on equably: The Body continually comes nearer and nearer to this greatest Celerity, but can never attain to it.

When the Densities of a Liquid and a Body are given, you have the respective Weight of the Body; and, by the knowing the Diameter of the Body, you may find out from what a Height Body, falling in Vacuo, can acquire such a Velocity, that the Resistance in a Liquid shall be e-

that greatest Velocity above-mention'd.

If the Body be a Sphere, it is known, that a Sphere is equal to a Cylinder of the same Diameter, whose Height is two third Parts of that Di-

Ratio in which Height is to be increased in the Ratio in which the respective Weight of the Body exceeds the Weight of the Liquid, in order to have the Height of the Cylinder of the Liquid, whose Weight is equal to the respective Weight of the Body; but, if you double this Height, you will have a Height, from which a Body, falling in Vacuo, acquires such a Velocity as generates a Re-

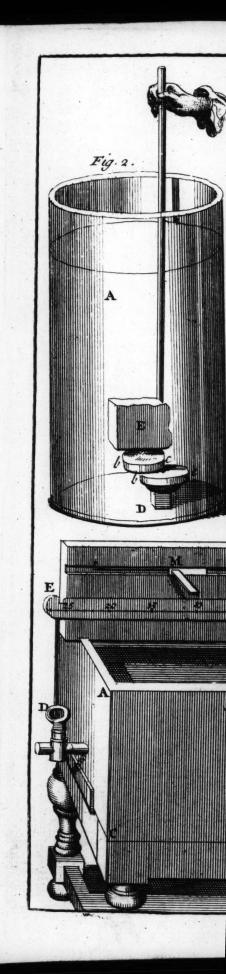
* 336 fistance equal to this respective Weight, * and which therefore is the greatest Velocity which a Body can

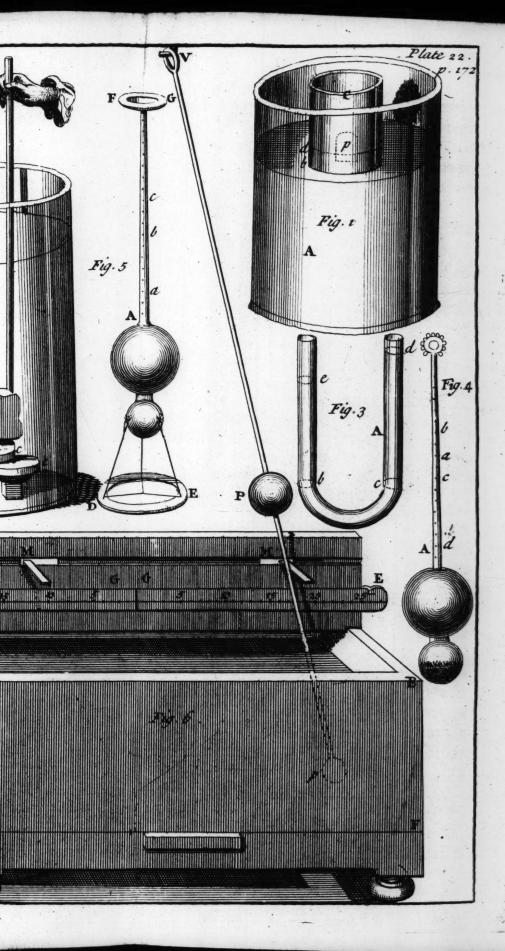
* 348 acquire, falling in a Liquid from an infinite Height.*
349 Lead is eleven times heavier than Water, wherefore its respective Weight is to the Weight of
Water as 10 to 1; therefore a leaden Ball, as it
appears from what has been said, cannot acquire
a greater Velocity, falling in Water, than it would
acquire in falling in Vacuo, from an Height of
13 ½ of its Diameters.

by the Action of the Liquid, is moved exactly by the fame Laws as a heavier Body falling in the Liquid.

Where-ever you place the Body, it is fustained by

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the Liquid, and carried up with a Force equal to the Difference of the Weight of the Quantity of the Liquid, of the fame Bulk as the Body, from the Weight of the Body, as appears by comparing Numb. 293. with Numb. 292. therefore you have the Force that continually acts equably upon the Body, by which, not only the Action of the Gravity of the Body is destroyed, fo that it is not to be considered in this Case, but by which also the Body is carried upwards by a Motion equably accelerated, in the same Manner as a Body, heavier than a Liquid, descends by its respective Gravity; but the Equability of the Acceleration is destroyed in the same Manner by the Refistance, in the Ascent of a Body lighter than the Liquid, as it is destroyed in the Descent of a Body heavier than the Liquid.

When a Body, specifically heavier than a Liquid, 352 is thrown up in it, it is retarded upon a double Account, on Account of the Gravity of the Body, and on Account of the Resistance of the Liquid; therefore a Body rises to a less Height than 353 it would rise in Vacuo with the same Celerity. But the Defects of the Height in a Liquid, from the Heights to which a Body would rise in Vacuo with the same Celerities, have greater Proportion to each other than the Heights themselves, and, in less Heights, the Defects are nearly as the

Squares of the Heights in Vacuo.

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PART II. Of the Motion of Fluids.

CHAP. VII.

Of the Celerity of a Fluid arising from the Pressure of the Superincumbent Fluid.

A N inferior Fluid is pressed by a superior, and that equally every Way; * because Action is equal to Re-action, it endeavours to recede every Way with equal Force; therefore if you take off the Pressure on one Side, the Liquid will 354 move towards that Side; and which Way soever the Pressure be taken away, it will move with the same Gelerity; which will be confirm'd by the Experiments to be mention'd in the following Chapter.

At the same Depth the Celerity is also every where the same, by reason of the Equality of the Pressure. * but when the Depth is changed, the

272 Celerity is also changed.

Yet the Velocity does not follow the same Proportion as the Depth; tho' the Pressure, from which the Velocity arises, does increase in the

* 273 fame Ratio as the Depth. * The Quantity of Motion, which is produced in the Liquid, is the Effect of the whole Pressure; and this Quantity

* 59 increases as the Pressure, * but the Ratio of the Quantity of Motion is compounded of the Ratio of the Velocity and the Quantity of the Matter

* 64 moved. * Here the Matter moved is the Water, which goes out of the Hole, whose Quantity, the Time remaining the same, increases with the

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Celerity; it will be double, if the Celerity be doubled, in which Case the Quantity of Motion 355 is quadruple; that is, increased as the Square of the Celerity, which obtains in any Celerity; therefore that Square increases as the Pressure; that is, is the Height of the Liquid above the Hole from which the Water spouts.

Plate XXIV. Fig. 1.] Fill with Water the Pa-356 rallelopiped A B, which is 15 Inches long, and as wide, and 2 Foot high; it must be so placed that its Bottom may be raised about 8 Inches above the horizontal Bottom of a hollow Trough C D, whose Length is almost 4 Foot, and Breadth a Foot and a half, and Depth 5 or 6 Inches.

At E, near the Bottom of the Vessel AB, there is fix'd a Brass Tube horizontally, above half an Inch in Bore; the fore Part of it is shut by a Plate, in the Middle of which there is a Hole, whose Diameter is equal to in Inch: that Hole is shut with a Cover that screws on upon the fore

Part of the Tube.

The Celerities, with which the Water flows out from E, when you have open'd the Hole, are compared together by Help of this Machine. Let it move, for Example, in the Line EL, and at L let it come to the Bottom of the Vessel CD; this Motion may be refolved into two Motions; the one horizontal along E I, in the Direction that the Water has in going out of the Hole, and tho other vertical along IL; the first is equable, and the Water, with the Celerity with which it goes out, runs thro' the Space EI, in the fame Time that in falling it runs thro' I L; * * 209 whatever the Celerity be, I L is not changed, because E I and the Bottom of the Vessel are horizontal, therefore the Time is not changed, in which feveral fuch Lines as E I may be run thro',

thro', and therefore they are as the Celerities with which the Water goes out: * if you measure the Distance to which the Water spouts, you will have the Line E I.

Experiment 1.] Let there be Water in the Veffel AB, up to the Height of five Inches, above the Hole at E; let the Distance be measured to which the Water spouts; if more Water be poured in to the Height of twenty Inches, it will spout to a double Distance. The Squares of the Distances are here as the Height of the Water, in which Ratio also are the Squares of the Celerities.

as that which a Body, falling from a Height equalto the Depth, would acquire; for the Velocity of a Liquid increases, when the Depth of the Hole below the Surface of the Liquid increases, in the same Ratio as the Celerity of the falling Body increases, when the Space gone thro'by the Fall in-

*355 creases *; and in the Beginning these Velocities
131 are equal; for in a Liquid the upper Parts, as

well as in a Body at the Beginning of the Fall,

endeavour to descend by Gravity only.

Experiment 2. Plate XXIV. Fig. 1.] This is performed with the same Machine as was used in the former Experiment; the Vessel AB is silled with Water, and a Tube with a Hole like the Tube E is placed at F, so that the Height of the upper Surface of the Water, above the Bottom of the Vessel CD, is divided by that Hole into two equal Parts; the Water from that Hole will spout to M, so that the horizontal Distance from the Point M to the Hole will be double the Height of the Hole, above the Bottom of the Vessel CD; therefore the Water, by an equable

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would yet it fever: quid the (Parts differ which necef Colu ment which lowin yield. every retard dimir loft al Colu Liqui Sides

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equable Motion, and with the Celerity, with which it goes out, runs thro' double the Space of that Height, in the Time in which a Body can fall from F to the Bottom of the Vessel C D, and therefore it moves with the Celerity which a Body can acquire in falling from that Height*; *134 but this Height is equal to the Height of the Surface of the Water above the Hole.

CHAP. VIII.

Of Spouting Liquids.

Liquid, spouting vertically out of a Hole, a- 358 rifes up with that Celerity, with which it would come up to the upper Surface of the Liquid, yet it never comes up to that Height *; and that for *357 feveral Caufes. 1. The Celerity, by which the Liquid ascends, is diminished every Moment, and the Column of the spouting Liquid consists of Parts, which are moved to different Heights by different Celerities; all the Parts of a Column, which is every where of the same Thickness, are necessarily moved by the same Celerity; the said Column every where will be broader every Moment, as the Celerity of the Liquid is diminish'd; which arises from the Impulse of the Liquid following, and which from the Nature of a Liquid yields to every Impression, and is easily mov'd every Way, by that Impression the Motion is retarded every where. 2. This Motion is also diminished by the Liquid, because, when it hath lost all its Motion, it hangs in the upper Part of the Column, and is fustained for a Moment by the Liquid that follows, before it flows off on the Sides, which retards the Liquid that follows it, and that Retardation is communicated to the 3. By the Friction against the whole Column. Sides

Sides of the Hole, the Celerity of the Liquid is diminished; which Friction is increased, when the Liquid is brought through Pipes and Cocks. 4. Lastly, the Air's Resistance stops the Motion of Liquids.

The first Cause above-mentioned of the Re-

tardation cannot be corrected.

The fecond is corrected by fomewhat inclining the Direction of the Liquid, as is felf-evident; 359 and this is the Reason why a Liquid rises bigber, if its Direction be a little inclined, than if it spouts vertically.

Experiment 1. Plate XXIV. Fig. 1.] To the 356 Machine above-described, * by Help of a Screw at N, join the Curve Tube NO, from which the Water, thro' a small Hole, spouts up vertically by turning the Tube a little, which is easily done by reason of the Screw at N, the Direction of the spouting Water will be inclined, and it will afcend higher. But by this Inclination the Beauty of a Jet is destroyed.

As to the third Cause of the Retardation, 'tis to be observed, that there is a greater Friction, in Proportion, in fmall Holes, than in great ones; the Celerity being increased, the Friction also

360 is thereby increased; and therefore the Holes and to be increased according to the Heights of the spout-

ing Water.

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The Ends of the Pipes, from which the Water spouts, have commonly the Figure of a truncar the Moted Cone, as is represented at P, (Plate XXIV. among Fig. 3.) in which End the Water suffers a great Part; deal of Friction, and is moved irregularly, and been fa fronts up with that Irregularity. This may be and if from the famouth, and polished Plate, fixed to it, which has a Hole Square in it; for then the Water spouts bigher, and because ing from

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the ned, it rifes with a Motion intirely regular, it is perfeetly transparent.

Experiment 2. Plate XXIV. Fig. 3.] Take the Tube above-mentioned P, as also the Cylinder O, shut up at one End with a bored Plate; let those be screw'd on, one after another, to the End O of the Tube NO (Fig. 1.) the Water remaining at the same Height in the Vessel A B, let it spout from the Tube P, and the Cylinder Q, and the Experiments will fully confirm what we have faid.

The Pipes, which bring the Water from a Reser-362 voir, must be very wide, in Proportion to the spouting Hole, that the Water may move flowly in these Pipes, and have no fenfible Friction.

For the same Reason the Water-way, or Pas- 363

is fage, of the Cocks must be very large.

Experiment 3. Plate XXIV. Fig. 1.] To the ina- Vessel A B, at the same Height as the Tube F, fix the Cock H, the Pipe of the Cock must be hut up in the same Manner as the Tube F, and ion, bor'd with a Hole of the same Size; the Waterway of this Cock is a Quarter of an Inch. The also Water, which goes thro' this Cock, is brought thro' a narrower Space than that which moves cout thro' the Tube F; therefore this last is more transparent, and spouts to a greater Distance.

ater The Resistance of the Air has a sensible Effect upon 364 ncarthe Motion of Liquids; (for itself may be reckon'd IV. amongst Liquids, as will be said in the Second great Part;) therefore we may here apply what has and been faid of the Ascent of any Body in a Liquid; y be and in small Heights, the Defects of the Heights sharp from the Heights in Vacuo are in the Ratio of the Hole Squares of those Heights *; that is, abstract-*353 and ing from the other Causes of Retardation, they

N 2

are in the Ratio of the Square of the Height of the Liquid above the Hole. Besides this Resistance there is also another, not to be over-look'd, which is the Action of the Air against the spouting Liquid. It incloses the whole Column of the spouting Liquid, and resists that Part of is Motion, whereby it spreads itself sidewise, as it becomes wider, and there is requir'd a greater Force of the Liquid that comes after, than if this Refistance was taken away; therefore the Air refifts by its lateral Pressure. The Resistance from the Stroke of the Liquid against the Air increases with the impingent Surface, that is, if the Celerities remain the same, increases with the Hole; in which Ratio, also, the Quantity of the Matter moved increases, and upon this Account 'tis no Matter, of what Bigness the Hole is.

The lateral Pressure follows the Proportion of the Surface of the Column; the Matter mov'd, which, (the Celerity being the same) is in the same

*62 Ratio as the Quantity of Motion, * follows the

Proportion of the whole Column, that is, of the Square of its Surface; and therefore, if the Hole be increased, the Quantity of Motion increases faster than the Cause retarding it; and for that

365 Reason in the greatest Heights of spouting Liquids, that the lateral Pressure (which exerts a greater Action when it acts the longer) may be the better overcome, greater Holes are requir'd; which we have also shew'd before to be requir'd in the

*360 same Case from another Cause: * where, as well as here, we supposed the greater Holes only necessary for the greatest Heights, tho the Demonstrations prove that these Holes, which are very necessary in the greatest Heights, are in general to be preferred to others.

Great Holes also hinder the Motion; for then there is a greater Surface which is press'd

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upon by the highest Part of the Liquid, which has lost all its Motion, and hangs on a longer Time, before it runs off down the Sides. From these two contrary Effects joined together, in all 366 Heights there is a certain Measure of the Hole, thro' which the Liquid will rise to the greatest Height possible. Yet one cannot gives Rules to determine the Diameter of the Hole, because the Bigness of the Pipes of Conduct and their Inslexions require it different, so that there may be a Variation to

Infinity.

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In respect to the greatest Heights, 'tis to be 367 observed, that the Bigness of the Hole, and also the Height to which the Liquid can ascend, have their Limits, which they cannot exceed. Not only the Liquid which is directly against the Hole runs out, but, that there may be a constant Supply, the neighbouring Liquid, continually comes towards the Hole with an oblique Motion, and in going out it spouts with a compound Motion, and the Motion of the Liquid, spouting vertically, is disturbed; the greater the Hole is, the greater is the Disturbance arising from that Cause, and in spouting Waters the Holes should never exceed an Inch and a Quarter. When the Celerity of the Liquid is too great, it strikes against the Air with fo much Force, that it is dispersed into Drops; in which Case, by diminishing the Celerity, the Height to which the Liquor spouts will be increased, and there is a Height which is the greatest to which a Liquor can ascend, which Height in spouting Water scarce exceeds 100 Feet.

Liquids, which spout obliquely, are not retarded 368 from so many Causes, nor so much, as those that spout vertically. The second Cause of Retardation, abovementioned, * has no Place here, and the Effect of * 358 the first is less. As for the rest, one may apply here what has been said of Solids oblique pro-

N 3 jected

quite to the End of the Chapter. And a Liquid may be confidered as an innumerable Quantity of Solids, following one another, and running the same Way. In the Motion of the Liquid, the Way gone thro' may be perceived by our Senses, and what has been said of Solids, obliquely projected, may be reduced to Experiments by the Help of Liquids; for doing which we must make use of Quicksilver, because of the great Specifick Gravity of this Liquid in respect of others: But these Experiments are to be made by a particular Machine contrived as follows.

A, B, C, D, E, F, H, is four Foot and an half broad, eight or ten Inches long, and fix or feven Inches high; the Bottom is made of a Board hollowed in half an Inch, to contain the Mercury the better.

In the End H, of the Side E, F, H, you have a Board H I fix Inches wide, and two Foot high, which has in it a Slit o t. By this means you may fix to any Height upon the Board the wooden Paralellopiped s, which has a Screw

fixed in its hinder Part.

The fecond Figure represents this Parallelopiped at S: there is fastened to it a cylindric Vessel of Box Wood, which has a Groove round it to receive two Brass Plates, one of which may be seen at fe; their Ends are joined together by the Screw G, so as to make the Box Vessel immoveable, till it is loosened by unscrewing g, which will allow it to move about its Axis.

In the Bottom of this Vessel there is a cylindric Cavity ab, a Quarter of an Inch Diameter; this communicates with a like Cavity bc, which terminates in the Middle of the greater Cavity cd, whose

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d, se whose Diameter is above half an Inch, that it may receive the truncated Cone of Box H, which is joined to the Cylinder I L, Fig. 3.

The truncated Cone H exactly fills the Cavity c d, and is held fast in it by Help of the Screw R, that goes thro' the Brass Plate QO, but so that this truncated Cone may turn upon its Axis.

In this Cone, as well as in the Cylinder I L, there is a Cavity bil, of the fame Diameter as the Cavity bc, and answering to it. This Cylinder I L has a Glass Tube N cemented to it.

The Tube is a Foot and a half long, one End of which is feen at NM (Fig. 5.) which is cemented also to the Box Cylinder LI, which is hollowed at lib, with a round Hole in the Form of a Gnomon, or the Carpenter's Square; at bc the Cavity is greater, to receive the truncated Cone CD, that exactly fills it, and is moveable about its Axis by the Help of the Handle EA.

The Cavity b i answers to the Cavity de, which communicates with fg; this Part of the Box has driven upon it an Iron Ferril BQ, in which is drilled a very small Hole g, which, when the Parts of the Machine are joined together, communicates with the Cavity of the Box P

(Fig. 2.)

To prevent the Tube from breaking the Ends L. L. of the Box Cylinders (Fig. 3. and 5.) together with the Tube, are joined close to a streight and stiff Piece of Wood m n (Fig. 1.) whose lower End m has an Iron Plate fixed to it (as may be seen in Fig. 6.) whose End LPB Q is bent in the Figure of a double Gnomon; when the End L. (Fig. 5.) of the Box Cylinder is applied to the End of the Piece M N I of Fig. 5. it fits to I of Fig. 6. and the Screw Q, applied to 0, presses the Cylinder

N 4

B D

BD of Fig. 5. and joins it firmly to the Cylinder L 1.

All the Parts of the Machine may be feen joined together at Fig. 1. Quickfilver, being poured into the Vessel p, spouts out of the Hole g, Fig. 5. When the Mercury is at the same Height in the Box, and you don't vary the Inclination of the Piece n m, the Mercury spouts with the fame Celerity in any Direction; but the Inclination of the Direction may be varied by moving the Handle e a (E A, in Fig. 5.) the Angle that the Direction, in which the Mercury goes out of the Hole, makes with the Horizon, may be meafured by Help of the Quadrant q, along which the Index f b is moveable, which by its Weight is always kept in a vertical Position. This Quadrant may be seen in Fig. 7. with its Index FH, it has 2 Rings behind, to receive the Handle EA, Fig. 5. When this Handle is vertical, the Index hangs against the 45th Degree, and the Direction of the Motion of the Mercury, which spouts out then, makes a half right Angle with the Horizon.

In Fig. 1. the Jets of Mercury in their feveral Directions are represented: They become the more visible by Help of a wooden Plane G painted black, along which the Mercury in its Motion does almost slide: Upon this Plane must be drawn the Ways which a Body (according to what is faid in Numb. 212) runs thro', when it moves with the same Celerity according to Directions which make different Angles with the Horizon. Also the Semicircle A L of Plate XV. Fig. 5. must be drawn upon this Plane, tho' it

could not be represented in this Figure.

There are feveral other fuch Planes, in which the same Things are drawn, but so as to reprefent the Ways of Projectiles, &c. according to different Celerities.

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This Plane stands upright near the Middle of the Trough, and bears against the Side E F H, so as to move backwards and forwards according to the Length of the Trough.

The Celerity of the spouting Mercury, is varied, as you change the Inclination of the Piece n m; and, by lowering the Vessel p, the Hole, throwhich the Mercury spouts, is set to the Direction of the Linear transfer of the Linear

on of the Lines drawn on the Plane.

The Mercury will stop its spouting, when the Cavity a b (Fig. 2.) is stopp'd with the Pin D E of Fig. 4.

Experiment 4. Plate XXIII. Fig. 1.] The Parts 371 of this Machine being join'd and fix'd together, as in the Manner above describ'd, incline the Piece n m, till the Height to which the Mercury is to fpout, when it ascends to a Direction almost vertical, is nearly equal to the Diameter of the Semicircle describ'd on the Plane G. Let the Vesfel P be fix'd at fuch a Height, and the Plane G be so plac'd, that the Axis of the Circumvolution of the Cylinder B D (Fig. 5.) shall answer to the lowest Point of the Semicircle above-mention'd. Which Way foever the Inclination of the Direction of the Jet (that is, of the Projection) be, its Amplitude will always be the Quadruple of the Line BM in the Semicircle ABL (Plate XV. Fig. 5.) There is indeed a small Difference, which chiefly arifes from the Resistance of the Air, and must be observed in the following Experiments.

the foregoing Experiment, if the Mercury spouts in two Directions, and the Inclination of one of them exceeds a half Right-Angle, as much as the other is under it, the Mercury will cut the Horizontal Line which is drawn from the lower Point,

Point of the Semicircle on the Plane G, just in the same Place in both Cases.

- before, if the Way for any Direction of Motion be drawn on the Plane, and the Index fb agrees with that Division of the Quadrant which denotes that Inclination, the Mercury in its Motion will follow the Line drawn to represent its Way. If you draw the Ways for several Angles, by the Motion of the Handle ae, you will bring the Mercury to spout in Jets that go along these very Lines.
- 374 Experiment 7.] Let there be another Plane as G, in which all the Lines above-mentioned are drawn for another Celerity of the Mercurial Jet, and the Experiments will fucceed in the fame Manner.

By the same Method, as we do by a Semicircle determine the Distance to which Bodies obliquely projected will fall, one may find the Distance to which the Liquor coming out of the Side of a Vessel spouts, when the Vessel is set upon a Horizontal Plane; which Distance is disterent according to the different Height of the Hole, the upper Surface of the Liquid remaining the same.

375 Plate XXIV. Fig. 4.] Let A B be the Height of a Vessel fill'd with a Liquid; suppose this Height cut into two equal Parts at C, with the Center C and Distance E A describe a Semicircle; let there be a Hole at E; lastly, draw E D perpendicular to A B, and terminated in the Circumserence of the Semicircle at D. Let the Liquid spout from E to F in the Horizontal Plane, and the Distance B F will be double the Perpendicular E D. Which

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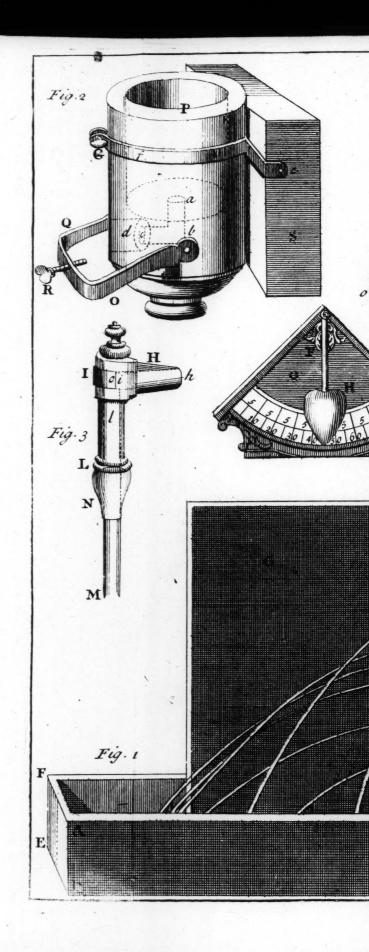
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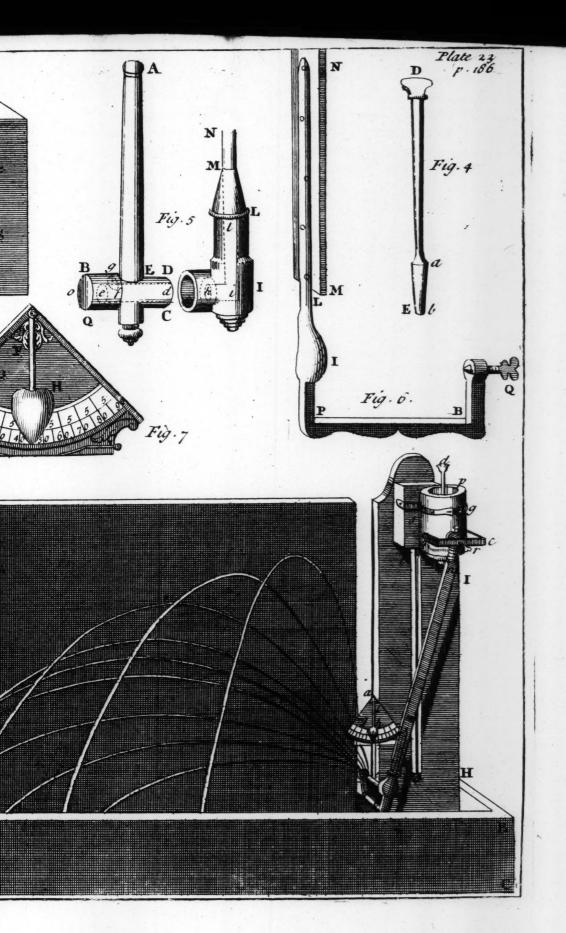
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Which will be demonstrated, if we consider, that the Liquid, with an equable Motion with the Celerity that it has coming out of the Hole, wou'd (in the Time that a Body can fall from E

to B) run thro' the Space B F*.

In all Motion, the Time remaining the fame, the Space gone thro' is as the Celerity *; the *53 Celerity remaining the fame, it is as the Time; Therefore if you change the Time and the Celerity, the Space gone thro' will be in a Ratio compounded of the Celerity and the Time; and multiplying the Time by it, you will have the Space gone thro'; that is, if you apply this Operation to different Motions, you will have fuch Quantities as will express the Proportion of the Spaces gone thro'. If you compute the Squares of the Celerities and the Time, you will have the Proportion of the Squares of the Spaces gone thro'. A E here expresses the Square of the Celerity; * EB the Square of the Time; * there- *355 fore the Product of those Lines expresses the *131 Square of the Space gone thro' E F. But that Product is the Square of the Line E D, which therefore, changing the Hole, increases and diminishes in the same Ratio as the Distance BF. Suppose the Hole in the Center C; BG, the Distance to which the Liquor spouts, is equal to BA, * and it is double the Perpendicular, which *357 from C may be drawn to A B in the Semicircle; 134. which therefore obtains in all Holes, and E D will be the Half of B F.

Hence it follows, that a Liquid, spouting from 376 a Hole in the Center C, will go to the greatest Distance possible.

Experiment 8. Plate XXIV. Fig. 1.] Here we must make use of the Machine, described in the foregoing Chapter*. Let the Water spout from *356 the

the Hole F, as in Experiment 2. Chap. VII. let it fpout at the same Time from E, and also from G, where there is a Tube like those which are made fast at F and E; the Hole G is less than F, but the Hole E is farther distant from the Surface of the Water, the Water comes from neither of them to the Distance to which it comes, when spouting from F.

Plate XXIV. Fig. 4.] From what has been faid, it follows, That the Water spouts to the same Distance from the Holes E e equally distant from the Center C, because in that Case the Perpendiculars ED and Ed are equal.

377 Experiment 9. Plate XXIV. Fig. 1.] From F let there be drawn a horizontal Line which goes through H; if H G and H E are equal, the Water will go from each Hole G and E to L.

CHAP. 1X.

Of a Liquid flowing out of Vessels, and the Irregularities in that Motion.

The Quantity of a Liquid, which in a given flows from a given Hole, increases in Proportion to the Velocity of the Liquid going out; this depends upon the Height of the Liquid above the Hole, and 'tis no Matter to what Part the Motion of the Liquid is directed;

*354 * therefore the Squares of the Quantities flowing out are in the Ratio of the Heights of the Liquid

*355 above the Holes *.

In the Time in which a Body falling freely goes through the Height of the Liquid above the Hole, a Column of the Liquid flows out equal in Length to twice that Height; * the Hole itself is the Base of the Column, and is given

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given; if the Height of the Liquid above the Hole is known, the whole Column is known; the Time also is easily determined by Experiments of Pendulums, * but having found what *157 Quantity flows out in a known Time, one may know what Quantity will flow out in a

given Time.

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Here you must observe, that the Resistance of the Air, and the Friction of the Liquid against the Sides of the Hole, hinders the Motion of the Liquid, and that the Rule above-mentioned does not exactly obtain, and that there always slow out a less Quantity than what there is determined by it. Yet making Experiments with Water, it is plain, that the Quantities, which slow from the same Hole in equal Times, sensibly keep the Proportion of the Squares of the Heights of the Water above the Hole, in Heights not exceeding fifty Foot.

In Vessels which are not supplied by the slowing in of the Liquid, the Celerity of the Liquid flowing out is continually changed, to which Regard must be had, when you compare together the Times in which different Vessels are

emptied.

Here we consider cylindric Vessels; and what is here said may be applied to any Vessels that are of the same Bigness, from Top to Bottom; we suppose the Liquid to slow out from a Hole in the Bottom.

The Times in which cylindric Vessels of the same 37 9
Diameter and Height are emptied, the Liquid slowing
from unequal Holes, are to each other inversely as

those Holes.

If we suppose that these Vessels are divided into very small equal Parts, by Planes parallel to their Base; and that the Divisions of each Vessel don't differ from one another, when we consider the

the smallest Parts, one may conceive that the Celerity is not changed in the Evacuation of one The Quantity of a Liquid which flows from a Hole, if the Celerity is not changed, increases with the Hole and with the Time; that is, in a Ratio compounded of the Time and of The correspondent Parts in the Vesthe Hole. fels are emptied with equal Celerities, and the aforesaid compounded Ratio obtains here: the fame Parts also, that is, the Quantities of the Liquid which flow out, are equal; wherefore the Difference of the Times is recompenced by the Difference of the Holes; that is, the Times are in the same, but inverse Ratio, as the Holes. Now as this happens in all the correspondent Parts, it must also be referred to the Times of the whole Evacuations of the Vessels.

When the Vessels are cylindric, unequal, and equally high, they are emptied thro' equal Holes, in Times that are to one another as the Bases of the Cylinders.

Let the Vessels again be supposed to be divided into very small Parts, and equal in Number in each Vessel; the Liquid of the correspondent Parts slows thro' equal Holes, and with equal Celerity: therefore the Quantities that slow out are as the Times; and consequently the correspondent Parts themselves are in that Ratio of the Times, which are as the Bases of the Cylinders: But the Times of the whole Evacuations are as the Times in which the correspondent Parts are evacuated.

Bases are equal, but their Heights, for Example, as 1 to 4, and let them be evacuated thro' equal Holes: Let these also be conceived to be divided into very small Parts, by Planes parallel to the Base; and let the Number in those Parts be equal in each Vessel; those Parts will be to one another

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as the Vessels, that is, as I to 4. We can consider every Part as evacuated by an equable Motion, because the Parts are very small; the Celerities in the correspondent Parts are every where, as I to 2, * because the Heights of those Parts above *355 the Bases are as the Heights of the Vessels, which are as the Squares of those Numbers. Whence it follows, that the Times, in which correspondent Parts are evacuated, are to one another, as I to 2; because in twice the Time with a double Celerity, a quadruple Quantity is evacuated. But as the Times are in the fame Ratio for each correspondent Part, the Times in which the whole Vessels are evacuated are also, as I to If the Vessels are, as I to 9, the Times will be, by a like Demonstration, as 1 to 3; and generally the Times are as the Celerities in which correspondent Parts are evacuated, the Squares of whose Celerities are as the Heights of the Vesfels, * in which Ratio also are the Squares of the *355 Times.

Experiment 1. Plate XXIV. Fig. 2.] Let there be three thin cylindric Vessels of Metal A, C, B, having equal Diameters, and whose Heights are, as 1, 3, and 4; let each of them have a Lip in the Top to let the Water run out, when it comes to a certain Height, which Lip must be reckoned the Top of the Vessel; in the Bottoms of the Vessels A and B, which are, as 1 and 4, let there be equal Holes, and let them be filled with Water; let the Holes be opened in the same Moment; if the Water running out of B be received in the Vessel C, it will be filled in the same Time that A is evacuated. C contains three Quarters of the Vessel B; the Quarter which is lest will also be evacuated in the same Time as the Vessel A,

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which is evident to Sense; therefore A is emptied twice, whilst B is emptied once.

The Times, in which any cylindric Vessels are evacuated, are in a Ratio compounded of the Bases,*

of the inverse Ratio of the Holes, * and of the square *579

*381 Roots of the Heights. *

The cylindrick Vessel may be so divided, that the 883 Parts intercepted between the Divisions shall be emptied in equal Times, which will happen, if the Distances of the Divisions from the Base be as the Squares of the natural Numbers; for the Times of the Evacuations of the Vessels, whose Heights are

381 in that Proportion, are as the natural Numbers, and the Differences of the Times are equal.

The Time, in which a cylindric Vessel is empti-

ed, is as the Celerity with which the Liquid be-*381 gins to run out; * therefore the Celerity, while the Liquid descends in the Vessel, is diminished

in the same Ratio as the Time of the Evacuation of the Liquid remaining in the Vessel, and the

Motion of a Liquid, running out of a cylindric Veffel,

is equally retarded in equal Times.

385 Ifthro' equal Holes a Liquid runs out of a Cylinder, and out of another Vessel of the same Height, (and in which the Liquid is always supplied so as to be kept at the [ameHeight] in the Time in which the Cylinder is emptied, there runs out twice as much Water from the other Vessel as from the Cylinder. For, because of the equal Height of the Vessels, the Celerities in the Beginning are equal; the Celerity of the Liquid, which comes out of the Vessel that is always kept full, is equable; the Celerity of the Liquid, which runs out of the Cylinder, is equably retard-

*384 ed. * Therefore, whilst the Cylinder is emptying, there will flow twice as much Water out of this Vessel as out of the Cylinder: For if two Bodies are driven with the same Celerity, and the first

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goes with an equable Motion and the fecond with a Motion equally retarded, and they move till they have lost all that Motion, the first in that Time will run double the Space of the fecond; * here the Liquor that runs out may be *135 look'd upon as the Space gone thro', because the *136 Holes are equal.

Besides the Irregularities from Frittion, and the 386 Resistance of the Air, there are several others arifing from the Cobesion of Parts, even in Liquors that are not glutinous. I shall here only speak of Water. We observe in Relation to it, that, tho' it be driven by the same Force in any Direction, * *354 the Height of the Water above the Hole remaining the fame, yet it will descend the more swiftly in a vertical Direction; the Water, in falling, is continually accelerated in its Motion, it coheres with the following, and accelerates that, and increases the Velocity of the Water flowing out of the Veffel.

Plate XXIV. Fig. 2. For this Reason the Mo-387 tion out of a Vessel, that has a Tube fix'd to its under Side, is also accelerated. Let E be such a Vessel equal and fimilar to the Vessel A, and which, together with the Tube, makes up the Height of the Vessel B; let the Tube, have the Holes at both Ends, equal to the Holes at the Bottoms of the Vessels A and B, fill the Water in the Vesfels A, E, and B. In the Beginning of the Motion, the Water flows from the Vessel E and B with equal Celerity, because the Heights of the Water above the Holes, from which the Water goes out, are equal; but the Celerity, in the Vefsel E, is immediately diminished, because there cannot run a greater Quantity of Water out of the Tube than what comes in at the upper Hole of the Tube, into which Hole no more Water

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can run in, than what can flow out at the Vessel A. Since the Parts of the Water cohere, the Water, which runs out, accelerates that which runs into the Tube, and this last retards that which runs out; and so the Quantity of Water, which in a certain Time runs out of the Vessel E, is a mean Quantity between the Quantities of Water that can run out at the same Time from the Vessels A and B.

Experiment 2.] The Vessels AE and B being made of some thin Metal, in the Proportions above-mentioned, fill with Water A and E; having opened the Holes at the same Instant of Time, the Water of the Surface at E will descend faster than that at A: On the contrary, if you make use of the Vessels E and B, it will descend faster in the last than in the first.

Municates with the Vessel, remain as before; and the lower Hole be open'd wider; then a greater Quantity of Water will flow out, and the Water which goes into the Tube will be more accelerated; this Hole may be made sufficiently wider without altering the Length of the Tube, insomuch that a greater Quantity of Water shall flow out from it than from the Vessel B. In that Case thro' the upper Hole of the Tube, at a small Depth below the Surface of the Water, there flows out a greater Quantity of Water, than from an equal Hole four Times the Depth. The same may de done by applying a longer Tube, without widening its lower Hole.

Experiment 3. Plate XXIV. Fig. 2.] Take the Vessel F no Way different from the Vessel E, but in having the lower Hole of its Tube bigger; take also the above-mentioned Vessel B. The Diameters

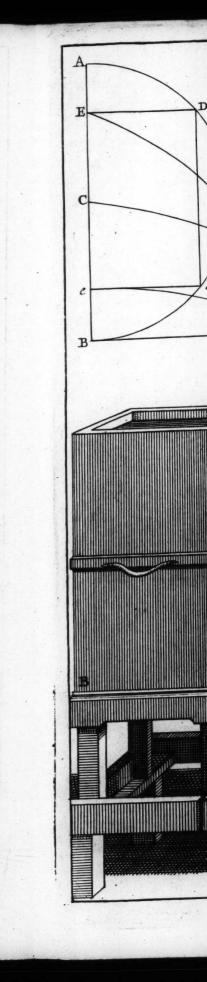
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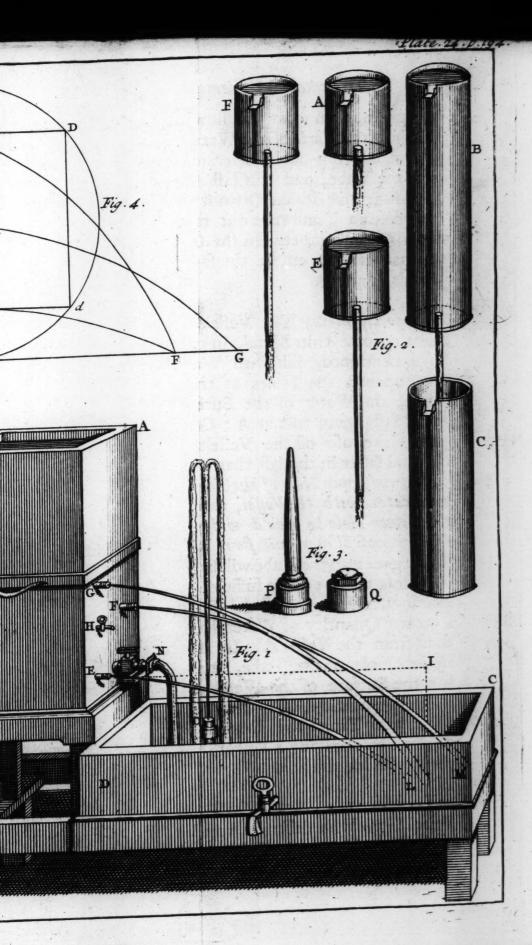
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Diameters of the Hole in the Bottom of this, and of the upper Hole of the Tube which is joined to F are of four Lines (or 4 of an Inch) the lower Hole of this Tube is of five Lines. Let the Vessels be filled with Water; and let the Water begin to run out of both at the same Moment; the Surface of the Water in F will descend faster; than that of B. The Vessel B is about 16 Inches high.

CHAP. X.

Of the Running of Rivers.

DEFINITION I.

THE Water that runs by its own Gravity, in 389 a Channel open above, as A E, is called a River, (Plate XXV. Fig 1.)

DEFINITION II.

A River is said to remain in the same State, 390 or to be in a permanent State, when it flows uniformly, so as to be always at the same Height in the same Place.

DEFINITION III.

A Plane, which cutting a River is perpendicular 391 to the Bottom, as ponq, is called the Section of a River.

When a River is terminated by flat Sides parallel to each other, and perpendicular to the Horizon, and the Bottom also is a Plane either horizontal or inclined, the Section of the River with these three Planes makes Right Angles, and is a Parallelogram.

In every River that is in a permanent State, the 392 same Quantity of Water flows in the same Time thro' every Section. For unless there be in every Place

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as great a Supply of Water, as what runs from it, the River will not remain in the same State. And this Demonstration will not hold good, whatever be the Irregularity of the Bed or Channel, from which, in another Respect, several Changes in the Motion of the River arise; as, for Example, a greater Friction in proportion to the greater Inequality of the Channel.

The Irregularities in the Motion of a River may be infinitely varied, and Rules cannot be given to settle them: Therefore setting aside all Irregularities, we must examine the Course of Rivers; for, unless the Laws of Motion be known in that Case, we have no certain Foundation for

determining any Thing.

Therefore, we suppose the Water to run in a regular Channel, without any sensible Friction, and that the Channel is terminated with plane Sides that are parallel to one another and vertical; and also that the Bottom is a Plane, and inclined to the Horizon.

Let A E be the Channel, into which the Water runs from a greater Receptacle or Head; and let the Water always remain in the fame Height at the Head, so that the River may be in a permanent State. The Water descends along an inclined

* 144 Plane, and is accelerated; * whereby, because the same Quantity of Water slows thro' every * 392 Section, * The Height of the Water, as you re-

cede from the Head of the River, is continually diminished, and the Surface of the Water will

acquire the Figure i q s.

To determine the Velocity of the Water in different Places, let us suppose the Hollow of the Channel A D C B to be shut up with a Plane; if there be a Hole made in the Plane, the Water will spout the faster thro' the Hole, as the Hole is more distant from the Surface of the Water

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Water bi; and the Water will have the fame Celerity that a Body, falling from the Surface of the Water to the Depth of the Hole below it, would acquire; * which arises from the Pressure *357 of the superincumbent Water. There is the same Pressure, that is, the same moving Force, when the Obstacle at AC is taken away; then every Particle of Water enters into the Channel, with the Celerity that a Body would acquire in falling from the Surface of the Water to the Depth of that Particle. This Particle is moved along in an inclined Plane in the Channel, with an accelerated Motion; and that in the same Manner, as if, in falling vertically, it had continued its Motion to the same Depth below the Surface of the Water in the Head of the River.* So, if you *150 draw the horizontal Line it, the Particle at r will have the same Celerity as a Body falling the Length iC, and running down Cr, can acquire; which is the Celerity acquired by the Body in falling down tr. Therefore the Celerity of a Particle may be every where measured, drawing from it a Perpendicular to the horizontal Plane, which is conceived to run along the Surface of the Water in the Head of the River; and the Velocity, which a Body acquires in falling down that Perpendicular, will be the Celerity of the Particle; which is greater, the longer the Perpendicular is. From any Point, as r, draw r s perpendicular to the Bottom of the River, which will measure the Height or Depth of the River. Since r s is inclined to the Horizon, if from the feveral Points of that Line you draw Perpendiculars to it, they will be the shorter, the more distant they are from r, and the shortest of them all will be fv: Therefore the Celerities of the Particles in the Line r s are so much the less, the nearer they are to the Surface of the 0 3

394 River, and the lower Water is moved faster, than the

upper Water.

sos But yet the Celerities of those Waters, as the River runs on, continually approach nearer and nearer to an Equality. For the Squares of those Celerities are as r t to s v, the Difference of which Lines, as you recede from the Head of the River, is con-

which is also continually diminished as the Lines themselves are lengthened. Now as this obtains in the Squares, it will much more obtain in the Celerities themselves, whose Difference therefore

is diminished as they increase.

the Head of the River, so as to become y z, and a greater Quantity of Water flows into the Channel, it will be higher every where in the River, but the Celerity of the Water is no where changed. For this Celerity does not depend upon the Height of the Water in the River, but, as has been demonstrated, from the Distance of the moved Particle from the horizontal Plane of the Surface at the Head continued over the said Particle; which Distance is measured by the Perpendicular rt or s z; but these Lines are not changed by the Afflux of Water, provided that the Water remains at the same Height in the Bason or Head.

397 Let the upper Part of the Channel be stopped up by an Obstacle, as X, which descends a little Way below the Surface of the Water; the whole Water which comes cannot run through, therefore it must rise up: But the Celerity of the Water below this

comes on is continually heaped up, so that at last it must rise so as to slow over the Obstacle or the Banks of the River. But if the Banks be raised and the Obstacle be continued, the Height of the Water would rise above the Line it; but, before

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that, the Celerity of the Water cannot be increased: In which Case the Height of all the Water in the Head will be increased; for as we suppose the River in a permanent State, there must continually be as great a Supply of Water to the Head, as there runs from it down the Channel; but, if less Water runs down, the Height must necessarily be increased in the Head, till the Celerity of the Water slowing under the Obstacle be so much increased, that the same Quantity of Water shall run under the Obstacle, as used to run in the open Channel before.

All these Things, as we have already said, if 308 we abstract from all the Irregularities, are true; and, the less the Irregularities are, the more will the true Motions agree with what we have said: concerning which, before we can make any Judgment, we must be able to compare the Velocities of Water by Experiments, and so determine the Velocities themselves, as to know the Spa-

ces gone thro' in a certain Time.

Plate XXV. Fig. 2.] Let ACB be a Quadrant divided into Degrees, * with a Thread in * 398 the Center, that has at the other End a Ball P hanging, which is heavier than the Water.

Let the Ball hang within the running Water, 399 whilst you hold the Side C A of the Quadrant in a vertical Position; the Ball by the Motion of the Water will be so far sustained, that the Thread P C will make the Angle P C A, with the Side C A, which will serve to determine the Celerity of the Water running against the Ball.

The Ball, being at rest in the Water, is drawn by three Powers; by its Gravity it endeavours to descend vertically; by the Action of the Liquid it is carried in the Direction of the Motion of the Water; and, lastly, it is drawn by the Thread

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along PC. Draw the Triangle E F G, in which E F represents the vertical Line; let F G make with that Line the Angle E F G, equal to the Angle which the Direction of the Motion of the River makes with the vertical Line; lastly, let the Angle G E F be equal to the Angle P C A. The Sides of the Triangle EFG are parallel to the Directions of the three Powers above-mentioned; therefore the Powers are to one another, as those Sides *: If therefore E F expresses the respective Gravity of the Ball, FG will express the Action of the Water on the Ball. If you make feveral Experiments in different Places with the same Ball, you must draw such Triangles, the Side F remaining, (which denotes the respective Gravity of the Ball that never changes) the Sides that are as FG will have the fame Proportion, as the Actions of the Water on the Ball. But these are as the Squares of the Velocities of the Waters in the Places in which the Experiments are made *; for there is no Difference, in respect of the Action of the Water on the Ball, whether the Ball be moyed and the Water at rest, or, on the contrary,

The Action of the Water against the Ball may be compared with the Weight, for it is to the respective Gravity of the Ball, as F G to E F.

the Water be moved and the Ball at rest.

But this Action is equal to the Resistance which a Body fuffers, when it is moved thro' quiescent Water with the same Celerity with which the flowing Water does now strike against the Body which is at rest: By knowing the Weight, which is equal to the Refistance, we know what Space could be run thro' in a given Time, with the Celerity with which the * 336 Body moves; * therefore we shall also here know what Space the Water can go thro' in a known Time, and so likewise what Quantity of Water

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come any . ed w defce acqu by w Water flows in a given 'Time thro' a Place given in the Section of the River.

Here it is to be observed, that the Determination of the Velocity of the Water will not be exactly settled, if the Experiment be made towards the Surface of the Water, because there the Action of the Water upon the Globe is irregular.*

* 328

This Celerity may be determined by immer-401 ging in Water a Body which is but a little lighter than Water, and which, swimming at the Surface, does not float so high above it, as to be affected by the Motion of the Wind; as the specifick Gravities of the Water and the Body scarce differ at all, and this Body may be look'd upon as wholly immersed, it will move with the same Celerity as the Water; and you may, by Help of a Pendulum, measure the Time in which a Body runs thro' a certain Space that was measured before. When the Surface of the Water is agitated by the Wind, the Experiment will not succeed well, because of the Motion of the Waves, which cause an Irregularity in the Motion of the Body.

CHAP. II.

Of the Motion of the Waves.

THE Surface of the stagnant Water is plane, 402 and parallel to the Horizon *; if it be-*272 comes hollow at A (Plate XXV. Fig. 3.) upon any Account whatever, this Cavity is surrounded with the Elevation BB; this raised Water descends by its Gravity, and, with the Celerity acquired in descending, it forms a new Cavity, by which Motions the Water ascends at the Sides

of this Cavity, and fills the Cavity A, whilst there is a new Elevation towards C; and, when this last is depressed, the Water rises anew towards the fame Part; whence there arises a Motion in the Surface of the Water, and a Cavity, which carries an Elevation before it, is moved from A towards C.

DEFINITION I.

403 This Cavity, with the Elevation next to it, is called a Wave.

DEFINITION II.

The Breadth of a Wave is the Space taken up 404 by a Wave in the Surface of the Water, and meafur'd according to the Direction of the Wave's Motion.

The Cavity, as A, is encompass'd every Way with an Elevation, and the Motion above-mention'd expands itself every Way, therefore the

405 Waves are moved circularly.

Plate XXV. Fig 4.] Let A B be an Obstacle, against which the Wave, whose Beginning is at C, does run; we must examine, what Change the Wave fuffers in any Point, as E, when it is come to the Obstacle in that Point. In all Places thro' which the Wave runs, whilst it goes forward its whole Breadth, the Wave is rais'd; then a Cavity is form'd, which is again fill'd up, which Change while the Surface of the Water undergoes, its Particles go and come through a fmall Space. The Direction of this Motion is along C E, and the Celerity may be represented by that Line; let this Motion be conceiv'd to be refolved in two other Motions along G E and DE, whose Celerities are respectively re-192 presented by those Lines *. By the Motion a-

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long DE the Particles do not act against the Obstacle, and after the Stroke continue their Motion in that Direction, with the fame Celerity; and this Motion is here represented by EF, suppofing E F and E D to be equal to one another, by the Motion along G E the Particles strike directly against the Obstacle, and this Motion is destroy'd; * for tho' these Particles are elastick, * 168 yet, as in the Motion of the Waves they run thro' but in a small Space, going backward and forward, they are mov'd fo flowly, that the Figure of the Particles cannot be chang'd by the Blow, and so they are subject to the Laws of Bodies perfectly hard. But there is a Reflexion of the Particles from another Cause; the Water which cannot go forward beyond the Obstacle, and is push'd on by that which follows it, yields that Way where there is the least Resistance, that is, ascends: And this Elevation greater than in other Places is caus'd by the Motion along GE, because 'tis by that Motion alone that the Particles come against the Obstacle. The Water, by its Descent, acquires the same Velocity with which it was raised; and the Particles of Water are repelled from the Obstacle with the same Force in the Direction E G, as that with which they came against the Obstacle. From this Motion and the Motion above-mentioned along EF, arises a Motion along E H, whose Celerity is expressed by the Line E H, which is equal to the Line C E; and by the Reflexion the Celerity of the Wave is not changed, but it returns along EH in the same Manner, as if, taking away the Obstacle, it had moved along E b. If from the Point C, C D be drawn perpendicular to the Obstacle, and then produced, so that Dc shall be equal to CD, the Line HE continued will

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go through c; and, as this Demonstration holds good in all the Points of the Obstacle, it follows

406 that the reflected Wave has the same Figure on that Side of the Obstacle, as it would have had beyond the Line A B, if it had not run against the Obstacle.

- 407 If the Obstacle be inclined to the Horizon, the Water rises and descends upon it, and suffers a Friction, whereby the Reslexion of the Wave is disturbed, and often wholly destroyed. This is the Reason, why very often the Banks of Rivers do not reslect the Waves.
- When there is a Hole, as I, in an Obstacle, as BL, the Part of the Wave, which goes through the Hole, continues its Motion directly, and expands itself towards QQ, and there is a new Wave form'd, which moves in a Semicircle, whose Center is the Hole. For the raised Part of the Wave, which first goes through the Hole, immediately flows down a little at the Sides, and then, by descending, makes a Cavity, which is surrounded with an Elevation on every Part beyond the Hole, which moves every Way in the same Manner, as was said concerning the Generation of the first * 402 Wave. *
- In the same Manner a Wave, to which an Obflacle, as A O, is opposed, continues to move between O N; but expands itself towards R in a Part of a Circle, whose Center is not very far from O.
- Hence we may easily deduce what must be the Motion of a Wave behind an Obstacle, as M N.
- Waves are often produced by the Motion of a tremulous Body, which also expand themselves circularly, tho' the Body goes and comes in a Right Line;
 for the Water, which is raised by the Agitation,
 descending, forms a Cavity, which is every where
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Different Waves do not disturb one another, when 412 they move according to different Directions. The Reason of which Esfect is, that whatever Figure the Surface of the Water has acquired by the Motion of Waves, there may in that be an E-levation and a Depression, as also such a Motion as is required in the Motion of a Wave.

Whoever has attentively considered the Motion of the Waves, will find that all these Things

agree with Experiments.

To determine the Celerity of the Waves, a-413 nother Motion, analogous to their Motion, is to be examined. Let there be a Liquid in the recurve cylindric Tube EH (Plate XXV. F. 5.) and let the Liquid in the Leg EF be higher than in the other Leg by the Distance lE; which Difference is to be divided into equal Parts at The Liquid by its Gravity descends in the Leg EF, whilft it ascends equally in the Leg EH; and fo, when the Surface of the Liquid is come to i, it is at the same Height in both Legs, and that is the only Position in which the Liquid can be at rest: But, by the Celerity acquired by descending, it continues its Motion, and afcends higher in the Tube GH, and in EF it is depressed quite to l, except fo much as it is hindered by the Friction against the Sides of the Tube. The Liquid in the Tube GH, which is higher, also defcends by its Gravity; and fo the Liquid in the Tube rifes and falls, till it has lost all its Motion by the Friction.

The Quantity of the Matter to be moved is the whole Liquid in the Tube; the moving Force is the Weight of the Pillar IE, whose Height is always double the Distance Ei; which Distance therefore increases and diminishes in the same Ratio with the moving Force. But the Distance Ei is the Space to be run through by the Liquid,

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that from the Position EH it may come to the Position of Rest; which Space therefore is always as the Force which continually acts upon the Liquid: But we have demonstrated that it is upon this Account, that all the Vibrations of a Pendulum, oscillating into a Cycloid, are performed in the same Time; and* therefore here also, whatever be the Inequality of the Agitations, the Liquid always goes, or comes, in the same Time.

fcends, or descends, is the Time in which a Pendulum vibrates, whose Length, that is, the Distance between the Center of Oscillation and Suspension, is equal to Half the Length of the Liquid in the Tube, or to Half the Sum of the Lines EF, FG, GH. This Length is to be measured in the Axis of the Tube.

Plate XXV. Fig. 6.] Let fuch a Pendulum vibrate in a Cycloid, in the Manner explained above (Page 62 and 63.) Let the Pendulum BC and the Arc AD be of the fame Length; for the Arc CA is equal to the Arc AD, and the Thread, by which the Pendulum is fuspended, applies to it, when the Body suspended is at A; in that Point the Direction of the Curve is perpendicular to the Horizon, and the Body endeavours to descend with all its Weight along the Curve: But this Weight is to the Force acting upon the Body, when it is at P, as AD, or PC to PD. * Now let the Liquid be in fuch a Position, that i E (Fig.5.) be equal to P, D; the Weight of the whole Matter to be moved, that is, of the whole Liquid, is to the Weight IE (which is the Force acting upon the Liquid in that Polition) as the Length of the Liquid in the Tube to the Line 1E, in which Ratio also the Halves of those Quantities

Quantities are, that is, PC to PD (Fig. 6.) Therefore in the Pendulum the Weight of the Matter to be moved is to the Force acting upon it, at P, as in the Tube, the Weight of the Matter to be moved is to the Force acting upon it in the Position E H. Therefore the pendulous Body and the Liquid, in this Case, are acted upon by equal Forces, and this always obtains where the Spaces to be run through by the Liquid in Agitation, and by a Body in Vibration, are equal; therefore in this Case the Agitation and the Vibration are perform'd in the fame Time, and not only in this Cafe, but always. * *413 But, as the fmall Vibrations in a Circle do not differ from the Vibrations in a Cycloid, the Demonstration will agree with them.

Experiment.] Take a cylindric recurve Tube, as EFGH; let the Length of the Legs be one Foot, and the Bore of the Cylinder half an Inch; pour Mercury into this Tube, and having made a Pendulum, whose Length is equal to Half the Length of the Cylinder of Mercury in the Tube; if the Mercury be agitated in the Tube, it will afcend and descend in the same Time as the Pendulum will go and come.

Plate XXV. Fig. 7. To determine the Celerity of the Waves from what has been faid, we must consider several equal Waves that follow one another immediately, as A, B, C, D, E, F, which move from A towards F, the Wave A runs its Breadth, when the Cavity A is come to C; which cannot be, unless the Water at C ascends to the Height of the Top of the Waves, and again descends to the Depth C; in which Moment the Water is not agitated fensibly below the Line bi; therefore this Motion agrees with the Motion

tion in the Tube above-mentioned, and the Water ascends and descends; that is, the Wave goes through its Breadth, whilst a Pendulum of the Length of half B C performs two Oscillations,

*414 * or whilst a Pendulum of the Length B C D, that is four Times as long as the first, performs one

*158 Vibration *.

Therefore the Celerity of a Wave depends upon the Length of a Line B, C, D, which is greater, according as the Breadth of the Waves is greater, and as the Water descends deeper in the Motion of the Waves.

In the broadest Waves, which do not rise high, 415 such a Line as B C D does not much differ from the Breadth of the Wave, and in that Case a Wave runs through its Breadth, whilst a Pendulum, equal to that Breadth, oscillates once. In every equable Motion, the Space gone through increases with the Time and the Celerity; wherefore multiplying the Time by the Celerity, you have the Space gone thro'; whence it follows, that the Ce-

A16 lerities of the Waves are as the Square Roots of their Breadths: For, as the Times in which they go

*158 through their Breadths are in that Ratio, * the
415 fame Ratio is required in their Celerities, that
the Products of the Times by their Celerities
may be as the Breadth of the Waves, which are

the Spaces gone through.

All these Things must be only looked upon as nearly true, because the Motion of the Waves differs something from the Motion in the Tube; which Error is in part taken off, because the Length of the Pendulum is measured along the inclined Lines B C and C D.

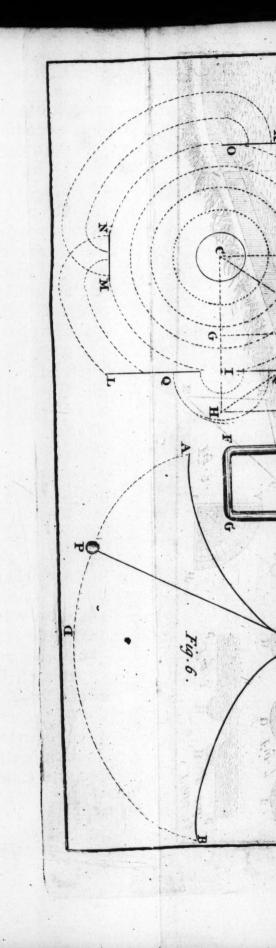
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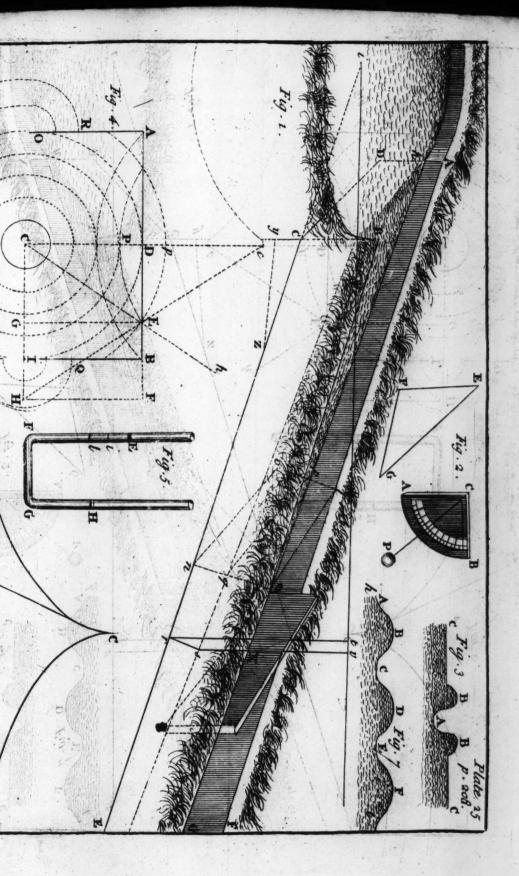
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PART III. Of the Air, as an Elastic Fluid.

CHAP. XII.

That Air has the Properties of Fluids.

W E have often spoken of the Air; and as we live in, and are always encompass'd by it, we must have Regard to its Effect in several Experiments, as we have said in other Parts of this Treatise: but now we shall consider its Properties singly.

The Air is corporeal, heavy, its Parts yield 417 to any Force impress'd, and are very easily moved one amongst another; it presses in Proportion to its Height, and the Pressure every Way is equal: it is plain therefore, that it ought to be reckon'd among & Fluids.

DEFINITION I.

All the Air which the Earth is encompass'd with, 418 considered together, is call'd the Atmosphere of the Earth, or simply, the Atmosphere.

DEFINITION II.

The Height of the Air above the Surface of the 419 Earth is call'd the Height of the Atmosphere.

That the Air is a Body, appears from its exclu-420 ding all other Bodies from the Place where it is. *

That

421 That it yields to any Impression, and has its Parts easily moved, is not doubted by any one.

422 That it is heavy, is proved by its pressing upon the Surface of other Fluids, and sustaining them in Tubes.

Glass Tube AB, about three Foot long, of about a Inch Bore; if you stop up the End A, and let the Tube be filled with Mercury, and let the other End be immers'd in a Vessel full of Mercury, the Mercury will be sustain'd at the Height of about 29 Inches. This is occasion'd by the Pressure of the Air on the Surface of the Mercury in the Vessel, which cannot press equally in every Part of it, unless in the Tube where no Air is, there be a Column of Mercury, which presses equally *274 with outward Air*.

*277 keep the fame perpendicular Height *: If therefore there be two Vessels containing Mercury, in which Tubes in the Manner above-mentioned are immers'd, of which E D is inclined to the Horizon, the Mercury is sustained at the Heights bf and ig, so that f and g are in the same Horizontal Lines; supposing the Surfaces of the Mercury in the Vessels to lie in the same Plane.

Experiment 3. Plate XXVI. Fig. 2.] The fame Pressure of Air sustains the Water of the Glass U, which is immerged in Water and filled with it, and then is pulled out all but the Orifice, which still remains immers'd.

Water would be sustained in the same Manner, tho' the Height should be 32 Foot; for Quicksilve filve lar pred Inc. fure

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filver 14 times heavier than Water, and a Pillar of Water a little more than 32 Foot high presses equally with a Column of Mercury 29 Inches high, which Pressure is equal to the Pres-

fure of the Atmosphere.

That the Pressure of the Air depends upon its 424 Height, may be easily deduced from what has been faid; but it is immediately prov'd by carrying the Tube with the Mercury above-mention'd to a higher Place; for, when you carry this Machine up a Hill, for 100 Foot that you rise perpendicularly, the Mercury descends a Quarter of an Inch.

That Air presses equally every way, appears from 425 this, that the Pressure is sustained by soft Bodies without any Change of Figure, and brittle Bodies without their breaking, tho' this Pressure be equal to the Pressure of a Pillar of Mercury 29 Inches high, or a Height of Water of 32 Foot *; any Body may fee that nothing can pre- *423 ferve these Bodies unchanged, but the equal Presfure on all Parts; but it is plain that the Air does press in that Manner. * If you take away the *291 Air on one Side, the Pressure is sensible on the opposite Side.

Exper. 4. Plate XXVI. Fig. 3.] Hang a Glass Tube to one of the Scales of a Balance AB, which is shut at D, and 3 Foot long; fill this Tube with Mercury, and let the End E be immers'd in the Mercury that is contain'd in the Vessel U. The Mercury by the Air's Pressure is fustain'd at the Height f in the Tube, and the upper Part of the Tube f.D is left void of Air; to make an Æquilibrium, you must put into the opposite Scale a Weight equal to the Weight of the Tube and the Mercury contained in it. Mercury inthe Tube cannot press the Balance; for

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for its Action against the Sides of the Tube is Horizontal; but the Air acts upon the upper Part of the Tube, and the Column that is sustained by the Tube is æquiponderate with the Column of Mercury that is contained in the Tube: If letting the Mercury run out, you suffer the Air to come in, then nothing but the Tube weighs down the Scale; which proves, that the Action against the inferior Surface of the upper Part of the Tube destroys the Action on the exterior Surface, and that the Air presence upwards and downwards with the same Force.

By this Experiment also is confirmed what has

been faid of the Air's Gravity.

CHAP. XIII.

Of the Air's Elasticity, or Spring.

E have shewn, the Air has the Properties of other Liquids; but besides it has another Property, which is, that it can take up a greater or lesser Space, according as it is compress'd with a different Force; and, as soon as that Force is diminished, it expands itself.

426 By reason of the Analogy of this Effect with the Elasticity of Bodies, this Property of the Air is

call'd its Elasticity.

427 That the Air may be compress'd, appears from

*14 an Experiment already mentioned. *

428 That it may be dilated, may appear from the following.

Tube AB close at the End A, and pour Mercury into it, so that there may be some Air lest in the Tube, which, when in the State of the external

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ternal Air, will take up the Space A1; if the End B of the Tube be immerfed into Mercury in a Vessel, the Mercury in the Tube will descend to g, and there remain. The Height ig dissers very much from the Height of the Mercury in the sirst Experiment of the foregoing Chapter, which does not arise from the Weight of the Air in the Tube; for its Weight is too little to produce any sensible Dissernce in the Height of the Mercury: The Expansion of the Air causes this Essect.

From this Experiment we deduce this Rule, 429 that the Air dilates itself in such a Manner, that the Space taken up by it is always inversely as the Force by which it is compress d.

The Force, by which the common or external Air is compress'd, is the Weight of the whole Atmosphere, which is equal to a Pillar of Mercury of the Height bf, Fig. 1. therefore the compressing Force may be express'd by that Height; the Space taken up by the Air in the Tube, when it is compress'd with such a Force, is A1.

But in the last Experiment, the Pressure of the Atmosphere exerts two Effects; it sustains the Pillar of the Mercury ig, and it reduces the Air in the Tube to the Space g A; if the Force, by which the Mercury is sustained at the Height g i, be substracted from the Pressure of the whole Atmosphere, that is, if the Height g i be taken from the Height bf, (Fig. 1.) there remains the Force by which the Air is compressed in the upper Part of the Tube; but this Difference of the Heights of the Mercury bf, and g i, is always to bf, as A l to Ag, that is, their Forces are inversely as the Spaces.

This Rule also obtains in compress'd Air,

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Experiment 2. Plate XXVI. Fig. 5.] Take a curve Tube ABCD, open at A, and shut at D; let the Part BC be filled with Mercury, fo that the Part CD may contain Air of the same State or Tenor as the external Air; therefore, the compressing Force is the Column of Mercury, whose Height is bf, Fig. 1. and by this Height must this Force be express'd, as in the foregoing Experiment; but the Space taken up by the Air is CD. Pour Mercury into the Tube AB, that it may rife up to g, the Air will be reduc'd to the Space eD: Now the compressing Force acts as strongly as a Column of Mercury of the Height fg, and also the Presfure of the external Air upon the Surface g of the Mercury; this Force is express'd by the Sum of the Heights fg in this Figure, and bf, in Fig. 1. This Sum is always to bf (Figure 1.) as CD to cD; and again the Forces are inversely as the Spaces.

The Elasticity of the Air is as its Density; for this last is inversely as the Space taken up by the Air*; therefore, as the Force compress'd the Air*, which is equal to that by which the Air endeavours to expand itself; but this Force is its

Elasticity.

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Hence it follows, that the Air in which we live is reduced to the Density which it has near the Earth, by the Pressure of the superincumbent Air, and that it is more or less compress'd, according to the greater or less Weight of the Atmosphere; for which Reason also the Air is less dense at the Top of a Mountain than a Valley, as being compress'd by a less Weight.

How far this Property of expanding itself is extended, we do not certainly know; and it is very probable that it can be determined by no

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Experiments. Nevertheless, if you compare the following Experiments with the Experiment of the Air compress'd in a Pump *, it will appear *14 that the Air may take up twenty thousand Times more Space in one Case than in the other.

Experiment 3. Plate XXVI. Fig. 6.] Let the Glass AB, about fourteen Inches high, be exactly fill'd with Water; it has a brass Cap fixed to it at the End B, by which it is to be screwed to the Pump that is represented in Plate XXIX. Fig. 6. by drawing out the Piston of the Pump the Water descends into it by its Gravity; and the Place in the upper Part of the Vessel is void both of Air and Water. The Air Bubbles in the Water, which are now compress'd, because the Air does not act upon the Surface of the Water, expand themselves, and rise up to the Surface of the Water; in that Motion the Bubbles are accelerated, fo as not to be feen distinctly near the Surface, upon account of their very fwift Motion; they also grow bigger as they ascend, and if you compare the Diameter of a Bubble at B with its Diameter, when it is come almost up to the Surface of the Water, but so far from it as to be feen distinctly, its Diameter is at least four Times as great as before.

The upper Part of the Glass, as was said before, is entirely void of Air, for the small Quantity of Air, which is continually going out of the Water, is not to be taken notice of here; therefore, the Air-bubbles near B, which is about a Foot below the Surface of the Water, are compress'd only by the superincumbent Water; which Pressure is to the Pressure of the Atmosphere nearly as one to thirty-two;* in which Ratio *423 also is the Space taken up by the Air, when 'tis compress'd by the whole Atmosphere, to the

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*429 ed; * their Diameter in their Ascent, as has been said before, becomes quadruple; that is, the Bubble becomes 64 times bigger than it was; and so the Space taken up by the Air, in this last Case, is to the Space taken up by the Air, when compress'd by the Atmosphere, as 64 times 32 (that is 2048) to 1. The Air compress'd by the Atmosphere is reduced to a Space 10 times less in a forcing Pump; and so the Density of the Air above-mentioned is to the Density of this Air, as 1 to 20480. Extracting the Cube Roots of these Numbers, we shall find that the Distances between the Center of the Particles, in these two Cases, are, as 1 to 27.

Hence we conclude, that the Particles of Air are not of the same Nature with other elastic Bodies, for the single Particles cannot expand themselves every Way into 27 times the Space, and so be increased 2000 times, preserving their Surface free from every Inequality or Angle; for, in every Expansion or Compression, the Parts are easily moved one amongst another; but, as the Air may be dilated much more than in this Experiment, it follows, that the Air consists of Particles and that made

cles which do not touch one another, and that repeled each other. We have shewn that, in several Cases, there are Particles endowed with such a Property; * and it is plain enough that it obtains here; but we are entirely ignorant of the Cause of this Force, and it must be look'd upon as a Law of Nature, as is plain from what has been said be-

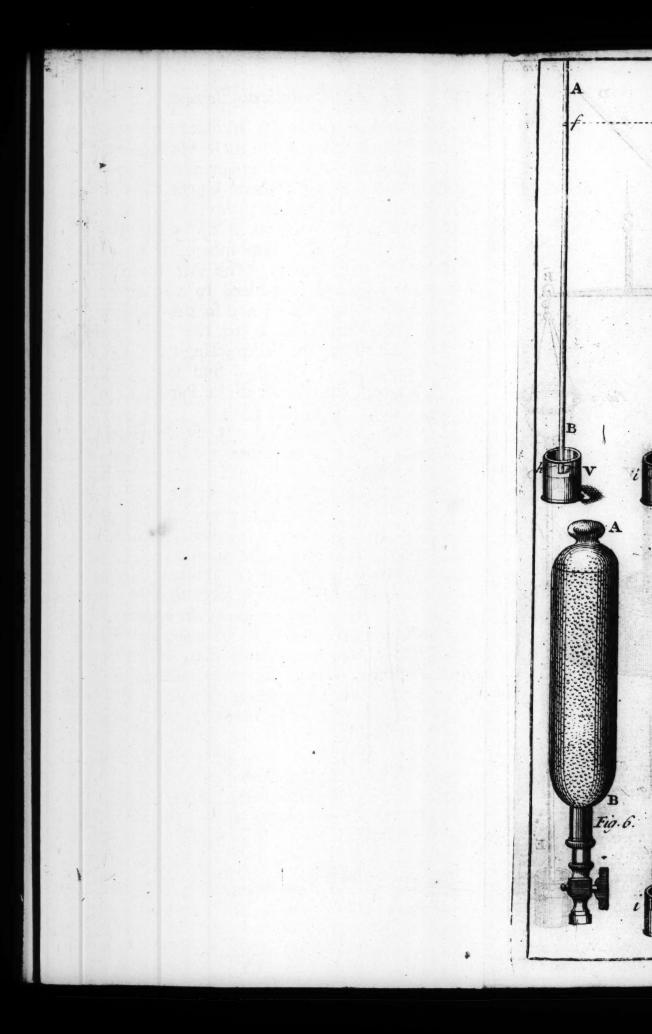
tween Numb. 4. and Numb. 5.

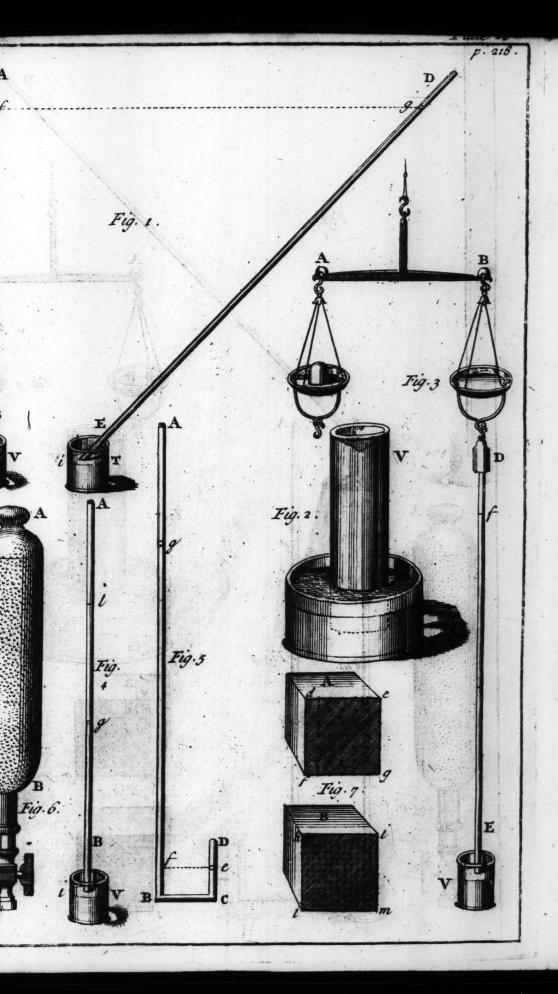
The Force, by which the Particles of the Air fly from each other, increases in the same Ratio as the Distance in which the Centers of the Particles are diminished; that is, that Force is inversely as this Distance. To demonstrate which, let us consider two equal Cubes

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Cubes A and B (Plate XXVI. Fig. 7.) containing unequal Quantities of Air; let the Distances between the Center of the Particles be, as 2 to 1, the Numbers of the Particles will be in the fame, but inverse Ratio, in the Lines de and bi; the Numbers of the Particles acting upon the Surfaces dg and hm are, as I to 4, namely, as the Squares of the Numbers of the Particles in equal Lines, and as the Cubes of those Numbers, that is, as I to 8, fo are the Quantities of Air contained in the Cubes; in which Ratio also are the Forces compressing the Air in the Cubes. * *429 The Forces acting upon the equal Surfaces dg and bm are as the Forces by which the Air is compress'd; * they are also in a Ratio compounded of the Numbers of the Particles acting, and the Action of the fingle Particles; therefore, this compound Ratio is the Ratio of 1 to 8: The first of the compounding Ratio's, as has been faid, is that of 1 to 4; wherefore, necessarily the fecond is that of I to 2, which is the inverse Ratio of the Distances of the Particles. And this Demonstration is general; for by 1 and 8 we express any Cubes whatever; by I and 4, the Squares of the Cube Roots; and lastly, by I and 2, the Roots of those Cubes: This Demonstration proves that the Action, which the Particles continually fuffer from all Sides, is increased between the Ratio in which the Distance of the Centers of the Particles is diminished, whether the Action is to be referred only to neighbouring Particles, or also to those which are more distant. In the first Case the repellent Force itself, which every Particle is endowed with, is as the Action abovementioned, that is, inverfely as the Distance between the Centers of the Particles.

In the fecond Case the repellent Force is equal at all Distances; for then the Action against each

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each Particle depends upon their Number in the fame Line, which Number is inversely as the Diftance between the Number of the Particles. Then also, supposing the Air of the fame Density, the Elasticity will be the greater, where the Quantity of the Air will be the greater; but, as this does not agree with Experiments, therefore, the first Cause must be true.

The Effects of the Elasticity of the Air are like those of its Gravity, and included Air acts by its Elasticity, just as Air not included does by its

The Air which is loaded by the Weight of the

whole Atmosphere, pressing every Way from the very Nature of Liquids, and the Force which

Weight.

it exerts, does no Way depend upon the Elasticity, because, whether you suppose Elasticity, or not, that Force which arises from the Weight of the Atmosphere, and is equal to it, can be no Way changed; but, as the Air is elastic, it is reduced to fuch a Space by the Weight of the Atmofphere, that the Elasticity, which re-acts against *126 the compressing Weight, is equal to that Weight*. But the Elasticity increases and diminishes as the Diftance of the Particles diminishes or increases*, and it is no Matter, whether the Air be retained in a certain Space by the Weight of the Atmofphere, or any other Way; for in either Case it will endeavour to expand itself with the same Force, and press every Way. Therefore, if the Air near the Earth be included in any Vessel,

Experiment 4. Plate XXVII. Fig. 3. Take the Tube mentioned in the first Experiment of the last Chapter, immerge it in Mercury included in the

without altering its Density, the Pressure of

the included Air will be equal to the Weight of

the whole Atmosphere.

the Glass DC, so that the Air, pressing upon the Surface of the Mercury contained in the Vessel U, may have no Communication with the external Air; the Mercury in the Tube is sustained at the same Height by the Elasticity of the Air, as it was sustained in the open Air.

The Tenor of the Air continuing the same, 434 what we have said will always obtain; but this Tenor or Temper of the Air is not always the same; the repellent Force of the Particles is often increased, or diminished, tho' the Distance between their Centers is not changed: I shall speak of this Alteration in the following Book: The Elasticity increases by Heat, and diminishes by Cold.

CHAP XIV. Of the Air-Pump.

HE Elasticity of the Air is the Founda-435 tion of the Constitution of a Machine, by which the Air may be drawn out of any Vessel. This Machine is call'd an Air-Pump, which is made feveral Ways: The chief Part in all of them is a Barrel, or hollow Cylinder of Metal, bored fmooth, and polished in the Inside; in this Barrel must move a Piston, that fills its Bore so exactly as to let no Air slip by. This Piston is thrust down close to the Bottom of the Barrel, and then raifed up in fuch a Manner as to exclude all the Air from the Cavity of the Cylinder or Barrel; if this Cavity communicates with any Vessel, by means of a Pipe at the Bottom of the Barrel, the Air in the Vessel will expand itself, and Part of it will enter into the Barrel, fo that the Air in the Barrel, and in the Veffel, will have the fame Den-Shut up the Communication between the Vessel and Barrel, and letting the Air out of the Barrel,

Barrel, apply the Piston close to the Bottom. If you raise the Piston a second Time, and open the Communication between the Barrel and Vessel above-mentioned, the Density of the Air in the Vessel will again be diminished; and repeating the Motion of the Piston, the Air in the Vessel will be reduced to the least Density. Yet all the Air can never be exhausted by this Method; for at every Stroke the Air does so expand itself, as to have the same Density in the Barrel as in the Vessel, in which last therefore, there is always a little Air lest.

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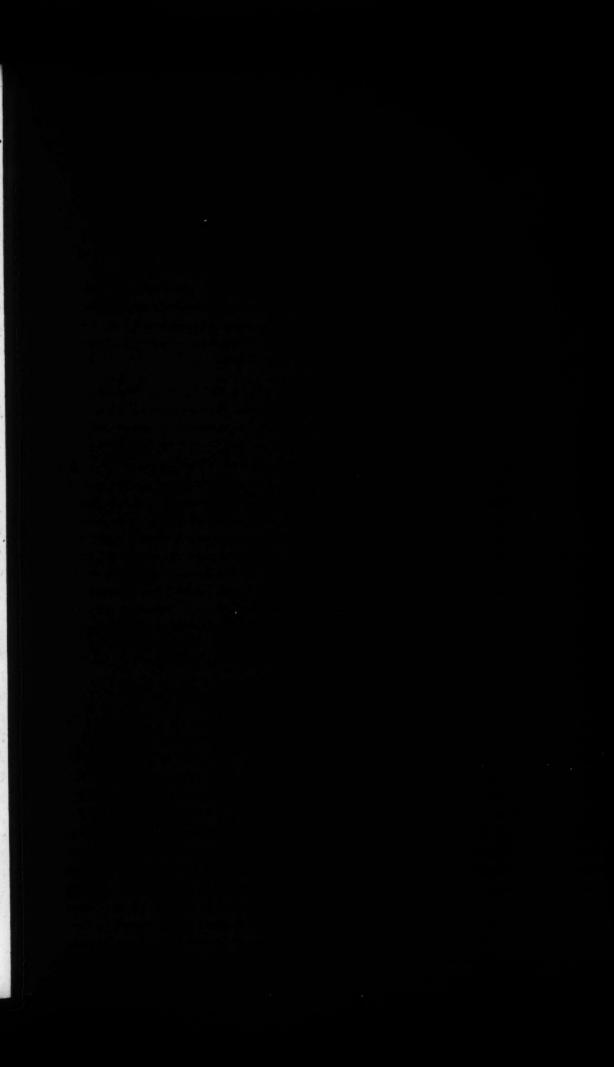
All Air-Pumps have in common the Parts above described, but they differ in several other Things. First, the Communication between the Receiver to be exhausted, and the Cylinder or Barrel, is opened and shut different Ways. Secondly, there are different Ways of getting the Air out of the Cylinder or Barrel, when the Piston is brought to the Bottom. Thirdly, the Pistons differ in different Pumps. Fourthly, the Position of the Cylinder is not the same in all Pumps, Fifthly, there are different Contrivances for moving the Piston.

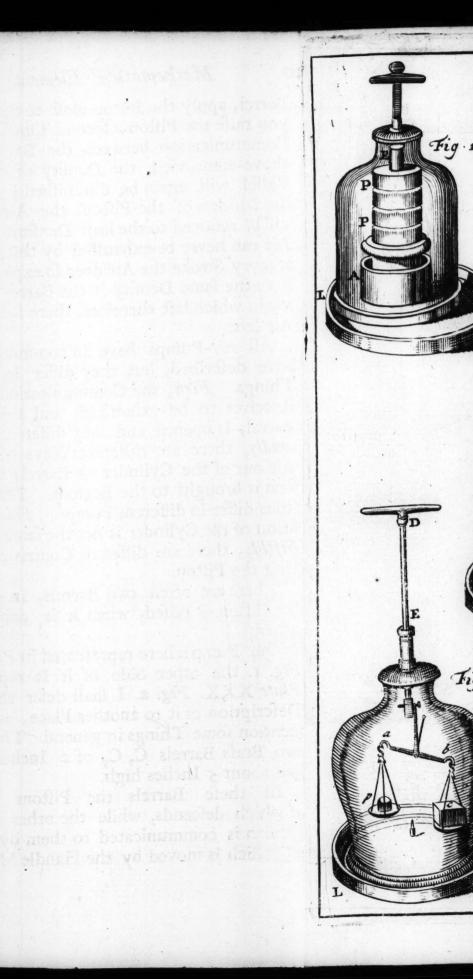
There are often two Barrels, in one of which the Piston is raised, when it is depress'd in the

other.

Our Pump is here represented in Plate XXVII. Fig. 1. the other Side of it is represented in Plate XXX. Fig. 2. I shall defer the particular Description of it to another Place, and only here mention some Things in general. This Pump has two Brass Barrels C, C, of 2 Inches Diameter, and about 5 Inches high.

In these Barrels the Pistons move, one of which descends, while the other rises, which Motion is communicated to them by the Wheel R, which is moved by the Handle MM, Fig. 2, fixed





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fixed to the Axis a. The angular Motion of the Wheel is the eighth Part of a Circle, by which in a lefs Wheel there is produced an angular Motion of 120 Degrees. This leffer Wheel is fixed to a third Wheel, by means of which the Piftons are immediately moved; they make a Stroke of 3 Inches and a half.

The Contrivance of the Piston is much the same as in the Pumps which they use in England; tho' we think that we have made ours more per-

fect, by some Alterations in them.

The Glass is to be exhausted, or set upon the round Plate LL; they communicate with the Barrels, by means of a Pipe, one End of which is at D, and which solder'd to the lower Side of the Plate, the Continuation of this Tube is seen at EE; there are two Cocks in it, E, E, between the Cocks is fixed the Pipe 1, 1, which communicates with the Cylinders C, C.

When the Air is exhausted, one of the Cocks above-mentioned serves to shut the Communication between the Receiver (so the Glasses are call'd from which the Air is to be pumped out) and the Barrels; the other Cock serves to let the Air in again, and to cut off the Communica-

tion with the mercurial Gage.

The mercurial Gage could not be convenient-438 ly represented in this Figure; it serves to determine what Quantity of Air is drawn out of the Receiver, as also what Quantity of Air remains in it; it is likewise of Use for measuring the solid Contents of the Receivers, which ought to be exactly known in several Experiments; our Gage differs from the common Gages in several Respects.

A little Cylinder, with a Screw upon it, is often screwed into the Plate at D, for applying

a Globe to be exhausted to the Pump.

In

In the Middle of the Plate L L there is a Hole, which is shut up with a Screw; but sometimes it serves for joining several Machines to the Plate.

By this Means also there is often applied to the Pump a cylindric Box, sull of Leathers soak'd in Wax, thro' the Center of which a brass Wire passes, which may be moved by the Help of a Handle, so as to communicate Motion into a Place void of Air; the Box has a Cover, which enters into it with a Screw, for pressing the Leathers together, and to prevent the entring in, or escaping out

of the Air; fuch a Box, or Collar of Leathers, is often joined to the Cover which is laid over the Recipients, as may be seen in Fig. 3. Pl. XXVIII.

and in Fig. 2. Plate XXXIII.

When the Receivers are laid upon the Plate L, L, or when the Receivers are floped with Covers, or when the Screws are joined to the Machine, and in general, when the Air is to be hinder'd from running in, we make use of Wax, which is soften'd by mixing as much Oil and Water to it as is found necessary.

CHAP. XV.

Several Experiments concerning the Air's Gravity, and its Spring.

be weighed like other Bodies, and so its Density may be compared with that of other Boweighed, when it is full of Air, and again, when the Air is exhausted, the Difference between their Weights is the Weight of the Air; which Method has this Inconvenience, that such a small Difference of Weight cannot easily be discovered, when a Balance, tho' ever so nice, is loaden with a great Weight; therefore we must make use of the following Method.

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Experiment 1. Plate XXVIII. Fig. 2.] Having 442 exhausted the Air out of the Glass Ball, whose folid Contents are 283 Inches, and having tied fuch a Weight to it, that it may be almost equal in specifick Gravity to Water, let it be immers'd into the Water continued in the Vessel DE, and let it be fastened by a Thread to the Hook of the Scale of the Balance A B, above described; * *271 raife the Balance till you make an Ægulibrium with a very small Weight; if by opening the Cock you let the Air into the Globe, a Weight I, of about 100 Grains, will be required in the opposite Scale to restore the Æquilibrium, sometimes more, or fometimes less, according to the different Tenor of the Air, which here near the Earth is varied according to the different Weight of the Atmosphere, and according to the Difference of Heat and Cold.

Bodies immers'd in Liquids are sustained by them, and the more or less, according to the greater or less Bulk of the Body, * and the Weight *299 loft in that Case is determined from the known Denfity of the Liquid; * by the foregoing Expe- *297 riment, therefore, it may be known, how much Bodies gravitate less in Air than in a Vacuum.

Hence also may be deduced, that Bodies that 443 are in Aquilibrio in the Air, if their Bulks are unequal, will lose their Aguilibrium in a Vacuum: Which is confirmed by the following Experiment.

Experiment 2. Plate XXVIII. Fig. 3.] In the Scales of the Balance a b, lay a Piece of Wax, c, and a Weight of Metal, p, and you will have an Æquilibrium. Hang up the Balance in a Glass Receiver, and, having exhausted the Air, the

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Wax will preponderate, its Bulk being greater than the Bulk of the Body p, it must be more sustained by the Air; and, therefore, when you let the Air into the Receiver again, the Æquilibrium is restored.

The Elasticity or Spring of the Air, which has been proved in Chap. XIII. becomes more sensi-

ble by the following Experiment.

With a small Quantity of Air in it; put a Receiver over it, and pump out the Air, whereby the Pressure upon the external Surface of the Bladder is diminished, and immediately the Air included in the Bladder will expand itself, and swell it out. We have proved, that the Spring of the Air is equal to the Weight of the whole Atmosphere; the following Experiment will make it visible.

445 Experiment 4. Plate XXVIII. Fig. 1.] Take 2 Bladder tied up very close, and not quite full of Air, and put it in a brass Box A, whose Diameter is three Inches and an half; so that the Cover, which is of Wood, and does not exactly fit the Box, may be fustained by the Bladder; you must put the Lead Weights P, P, upon the Cover: They have a Hole in the Middle for a wooden Cylinder E, which is fixed to the Cover, to go thro': When you pump out the Air, the Bladder is fwelled, as in the foregoing Experiment, and by that means the Weights are raised. You may use several Weights according to the Bigness of your Glass Receiver, and tho' they should amount to 60 or 70 Pounds, they would be easily raised. The Gravity of the Air, its Pressure that arises from the Gravity, as also its Elasticity, produce

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very different Effects; some of which I shall select, and confirm by Experiments.

Experiment 5. Plate XXVII. Fig. 3.] To the 446 Hole in the Middle of the under Side of the Air-Pump LL, screw on a small hollow brass Cylinder which has a Hole thro' it, and an open glafs Tube A B cemented to it at Bottom, whose lower End B must be immerged into Mercury. Let Mercury be fustained in the Tube eg, that is close at e, and void of Air in the Manner before-faid. * Set the Veffel U with the Tube up- *422 on the Plate L L, and cover it with a tall Glass DC, fo as to cut off all Communication between the external Air and the Vessel U, as also the Cavity of the Tube AB. The Air in this Tube does, by its Elasticity, hinder the Mercury from rifing up in the Tube, by the Pressure of the external Air. The Air also, that is included in the Receiver DC, does by its Spring fustain the Mercury in the Tube ge. * Pump the Air out *433 of DC; as the Denfity diminishes, the Elasticity does also decrease, * and the Force by which the *430 Mercury is fustained in the Tube ge becomes less, therefore, the Mercury descends. At the fame time the Pressure of the external Air overcomes the Resistance in the Tube AB, and the Mercury ascends in the Tube. The Diminution of the Spring in the Tube A B, and in the Vefiel BC, is the same, and the Effect of the Diminution the same in both Cases; therefore, the Mercury descends as much in the Tube eg as it rises in the Tube AB, which agrees with the Experiment. By this Method the Mercury is raised up to f, while the Tube ge becomes almost wholly empty; when you let in the Air again, the Mercury rifes in the Tube ge, as it is depressed in the Tube AB.

Experiment

- 1447 Experiment 6. PlateXXVIII. Fig.4. Take the little Pump or Syringe A, and its Piston being thrust close to the Bottom, let the Tube which is joined to this Syringe be immerged in Water; when you raise up the Piston, the Water will follow it, and fill up the Cavity between the Bottom of the Pump and the Piston; which Essect arises from the Pressure of the external Air. For this Reason Water does not rise in vacuo.
- Glass Tube bc to the Syringe A, which is fcrewed to the Cover of a Glass Receiver, so that the End c of the Tube may descend below the Surface of the Water in the Vessel U; thrust down the Piston to the Bottom of the Syringe, and let all the Air be pumped out of the Receiver. If then you pull up the Piston, the Water will not rife.
- Force, by which the Air presses upon Bodies, often breaks them, when the Pressure is not equal every Way. Let the Brass Cylinder A be covered with a flat Piece of Glass; when you pump the Air out of this Cylinder, the Plate of Glass will be broken into a great many little Pieces by the Pressure of the external Air.
- Syringe A of an Inch Diameter; push down the Piston to the Bottom of it, and shut up the Hole at the Bottom of the Syringe, and hang on a Weight P of 10 Pounds to the lower End of the Syringe; if you hold the Handle B of the Piston in your Hand, the Syringe will not descend; for it cannot descend, unless the Weight hanging at

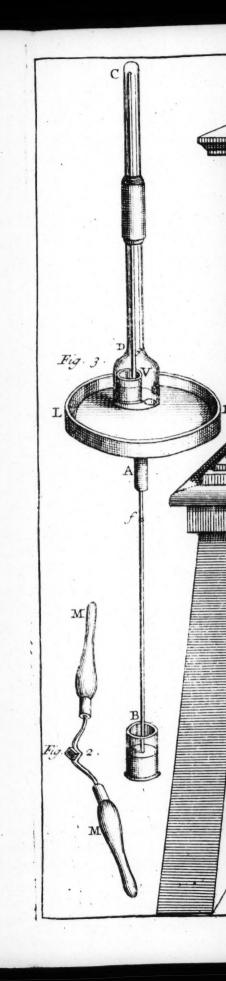
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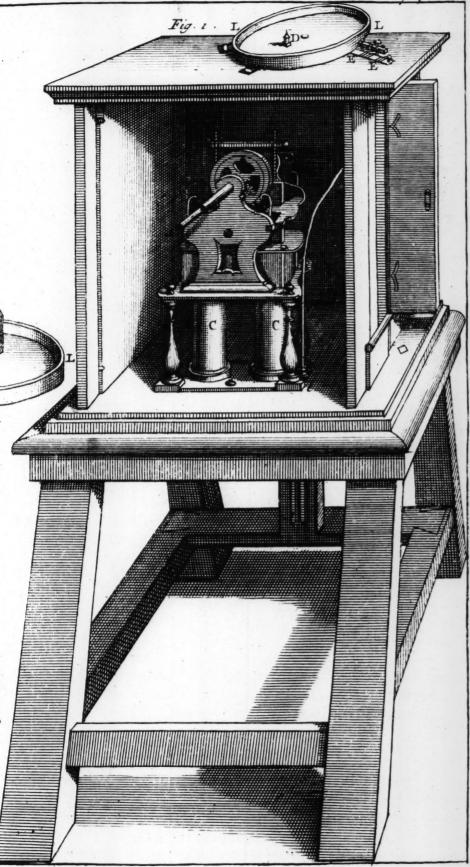
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whi to i the it overcomes the Pressure of the Air and Friction of the Piston; but the Pressure of the Air alone does here exceed 10 Pounds.

Experiment 10. Plate XXIX. Fig. 2.] The Sy-451 ringe descends by the Weight p alone in a Vacuum, which is but just sufficient to overcome the Friction of the Piston.

Experiment 11. Plate XXIX. Fig. 3. We fee a 452 more sensible Effect of the Pressure of the Air. when the two Segments of a Sphere, H and I, are joined together. Let the Brim or Edge of each of them be well polished, so that they may fit together, and, when they are applied close, put a little Wax between, to exclude the Air. There is a Cock in the Segment H, by which the two Segments, when joined together, may be applied to to the Air-Pump, and which must be shut, when you have exhausted the Air. The Segments are suspended by the Ring A, and, by the Help of the Ring Q, you may hang to them the Weights that are laid upon the great wooden Scale T. If the Diameter of the Segments be three Inches and an Half, a Weight of about 140 Pounds will be required to pull them afunder.

Segments be joined together and exhausted, as in the former Experiment; if they be suspended in a Vacuum, with a little Weight P hanging on, which is just able to overcome the Cohesion of the Wax, they will be separated in this Experiment. There must be fastened, to the Plate L L, the little brass Box, or Collar of Leathers, * thro' *439 which a brass Wire that has the Weight hanging to it slips. Lest the Receiver should be broke by the Fall of the lower Segment, you must put under

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der it the hollow wooden Cylinder M, to let it fall into. In this Figure the Segments are fufpended to the Cover of the Receiver which is to be exhausted; they may be also be suspended from a Pillar fastened to the Cylinder M. That the Hemispheres may not be separated without Difficulty, it is not required that they should be empty of Air; as great a Force will be required to separate them as in the 11th Experiment; when having included them in a Vessel, and applied them close together (fo as to leave them full of common Air, and shut the Cock that the Air between them may not be changed;) the Air on the Outside of them in the Vessel, that contains them, is reduced to a double Denfity; which to confirm by an Experiment, we must first describe the Machine with which we make Experiments in compressed Air.

454 Plate XXXI. Fig. 5.] A round brass Plate N is laid upon a Board aa, about 15 Inches long, and 10 wide; the Diameter of this Plate is about 5 or 6 Inches, as you may see by its separated Figure at N, in Plate XXIX. Fig. 4. and has fixed to it here a Cylinder P, which is not perforated, and goes thro' the Board aa. Upon this Plate you must put a Glass UU, about 10 Inches high, that is terminated at each End in a cylindric Form, and the cylindric Parts have brass Rings, or Ferrels, upon them.

The Vessel must have upon it the Cover D. The Pillars CS, CS, are fastened to the Board aa, and go thro' the Wood de, by which the Cover D is firmly joined to the Glass, as also the Glass to the Plate N, by the Force of the Screws ff. It is very necessary to press all these Parts close together, having first spread Wax upon the upper

and lower Edges of the Glass.

The

The Cover is represented in the separated Figure D, Plate XXIX. Fig. 4.] There is fixed to it to the Collar of Leathers, * and, lest the Piece *439 of Wood de should be applied to too small a Surface, the Cover is made in the Shape of a round open Box.

There is a perforated brass Wire C, which goes through the Collar of Leathers, to which a

Cock B is joined.

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Plate XXIX. Fig. 6.] In order to compress 455 the Air in this Vessel, screwing on the Syringe AB to the Cock Blast mentioned, which Syringe has joined to it another Cock, in the Key of which, besides the usual Hole, there is another oblique Hole which goes to f, and by which, when you shut the Communication between the Glass and the Syringe, the Syringe has a Communication with the common Air, and is filled with it, when you raise up the Piston. When you open the Communication between the Glass and the Syringe, by pushing down the Piston, you force the Air which was contained in the Syringe into the Glass; and, by often repeating this Operation, you at last bring it to the Density required.

Experiment 13. Plate XXIX. Fig. 4.] Now, to 456 feparate these Segments or Cups in compressed Air, the Segment I is joined to the Plate N, by Means of the Pillar M L, which has Screws at M and L. The other Segment H, by Screws at F and E, is joined to the Wire C. The Segments must be applied to each other. As for the rest, you must observe what has been said in the Description of the Machine; and the Air must be compressed in the Vessel, so as to have twice the Density of that which is compressed only by the Atmosphere. At P the Ring Q

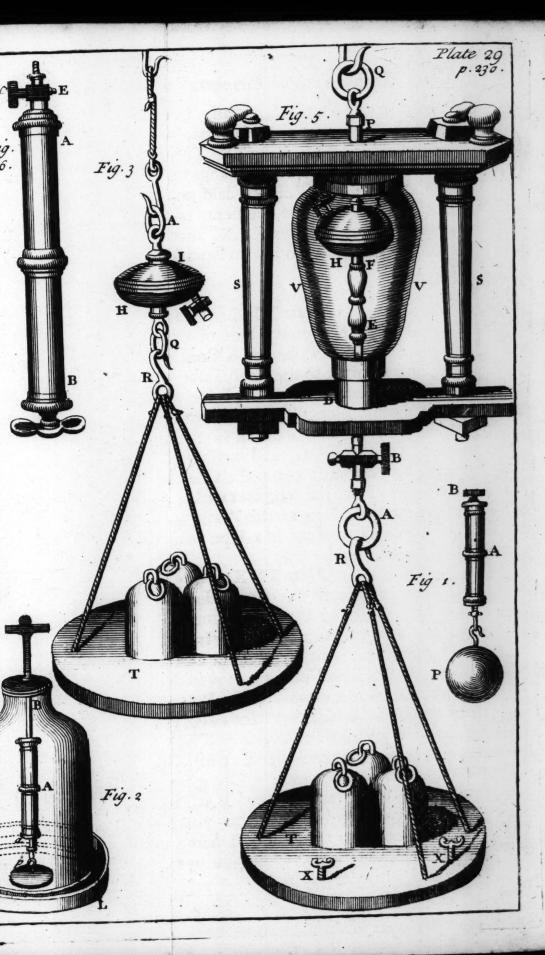
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is joined to the Plate N, as also the Ring A to the Cock B. Invert the Machine, as in Fig. 5. and suspend it by the Ring Q. The Scale T, on which the Weights are laid, hangs upon the Ring A; and, until the Weights, laid on, come to be about 140 Pounds, the Segments will not be separated. Three Screws X, X, hinder the Scale T from descending too low in separating the Segments.

- Tube AB to the under Side of the Air-Pump Plate LL, which Tube has a Cock in its upper Part, and is join'd to the small Tube which stands above the Plate. Put on the Receiver R, which covers the prominent Tube. The End B of the Tube AB must be immersed in the Water contained in the Vessel U, and having exhausted the Vessel R, you must open the Cock; the Water will spout up into the Receiver with a great Force, for the same Reasons as the Water is sustained at * 423 the Height of 32 Foot in a Pipe void of Air.*
- 458 Experiment 15. Plate XXX. Fig. 3. The Air's Elasticity produces the same Effect. Let there be a brass Cylinder U exactly shut. There must be a Hole in the Bottom to pour in Water, which afterwards you shut up with a Screw. To the upper Part of the Vessel there is soldered a Pipe, which goes down almost to the Bottom; and to the other End of it, that stands above the Vessel, a Cock is joined (See Fig. 4.) This Vessel is to be screwed on to the lower Part of LL, the Air-Pump Plate, and from it a Pipe goes quite thro' the Plate, and stands up above it, which is covered by the Receiver R. After you have pumped out the Air, the Vessel U being about two Thirds full of Water, when you open the Cock,

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tle In ma the Water will violently spout up into the Receiver, by the Force of the Spring of the Air contained in the upper Part of the Vessel U. Here the Air presses upon the Surface of the Water, when you open the Cock, the Pressure in the Tube becomes less, therefore the Water must go into the Tube.

Experiment 16. Plate XXX. Fig. 4.] Even in 459 the open Air, the Water will violently spout out of the Vessel U, if, having filled it two Thirds full of Water, the Air be compressed in the upper Part of it, which is done by Help of the Syringe above-mentioned*.

Experiment 17. Plate XXXI. Fig. 1.] Invert the 460 Glass R, and immerge it in the Water contained in U, the Air keeps out the Water at whatever Depth it be immerged; yet the deeper the Glass is put down, the less Space the Air is reduced into.

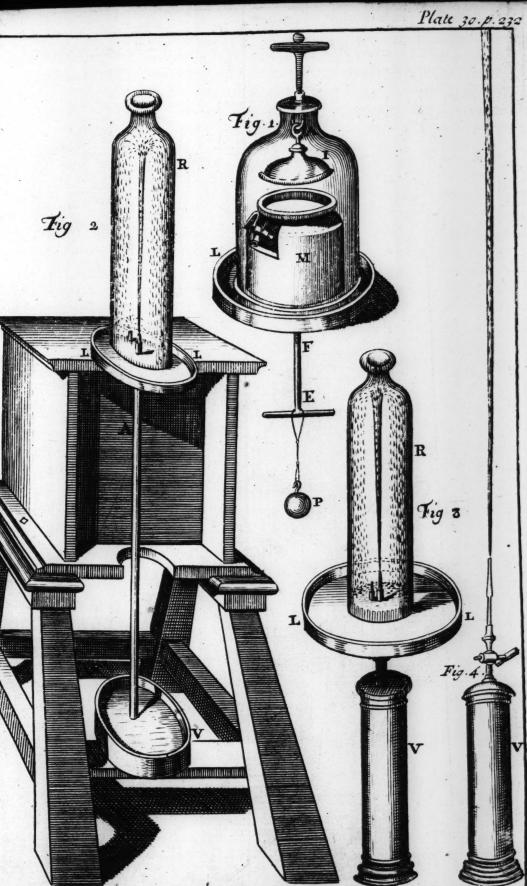
Upon this Principle are made the Machines, in 461 which Divers go down into the Sea. They are made like Bells, and descend by their own Gravity; the Water does not rise up to the Diver in the Bell; fresh Air is sent down continually by Bladders tied to a Rope, which he draws down to him; the Air, heated by his Respiration, rises to the upper Part of the Bell, and is there driven out thro? a Cock, by the Pressure of the Water, that pushes up, and compresses the Air in the lower Part of the Bell; which Pressure overcomes the Force with which the Water endeavours to descend thro' the Cock; for the Pressure of Liquids is increased in Proportion to their Depths.*

tle Figures of Glass that are made hollow, of an Inch and half long, representing Men, which may be had at the Glass-Blowers; these little Q 4 Images

Images have a small Hole in one of their Feet, and are lighter than Water. Immerge them into the Water contained in the Glass A B. Glass is about a Foot, or 15 Inches high, and covered with a Bladder, which is tied fast over the Top. A fmall Quantity of Air is to be left between the Bladder and Surface of the Water. If the Vessel be pressed with the Finger, the Air above-mentioned is reduced to a less Space, and the Surface of the Water is more compressed; the Water, which is more compressed, enters in the little Men thro' the Hole at their Feet, and compresses the Air in their Bodies more than it was. The little Images, becoming heavier, by this Means descend towards the Bottom of the Veffel, and that faster or slower, according to the Bigness of the Hole, and also according as the Specifick Gravity of the Images comes nearer to the Specifick Gravity of the Water. Taking away your Finger, the Air in the little Men, being less compressed, expands itself, and drives out the Water, fo the Images rife up again to the Surface of the Water.

- A63 Experiment 19. Plate XXXI. Fig. 3.] Animals cannot live without Air. If any Animal be included in the Receiver U, and the Air be drawn out, the Animal will immediately be in Convulfions, and will fall down dead, unless the Air be fuddenly re-admitted. Some Animals will live in a Vacuum longer than others.
- Fishes also cannot live without Air; but in others you see no such Change, but the Swelling of their Eyes. What Experiments you make upon Fishes must be made in the Glass Receiver U, which is set upon the Plate of the Air-Pump, and to the Hole,





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Hole, thro' which the Air is drawn out, you must screw on a Pipe, which comes up almost to the upper Part of the Glass U; pour in Water, and then put a Cover over the Glass Receiver U, and exhaust the Air out of the upper Part of it. Having taken away the Pressure of the Air from the Surface of the Water, the Air in the Fish's Body expands itself, by which Means the Fish, becoming lighter, cannot descend in the Water.

Experiment 21. Plate XXXI. Fig. 5.] Experi-465 ments are made upon Animals in compressed Air, by Help of the Machine above described.* In * 454 that Case Animals do not soon die, because the Vessels in the Body are not broken; yet, if they continue long in that condensed Air, it must be hurtful to them; nay, and in a greater Compression of the Air (for which a Vessel of Metal is required) they will die in a little Time.

Experiment 22.] Several Liquors contain Air. 466
If you put them under a Glass Receiver, and draw out the Air, then the Air contained in the Liquors will expand itself and go out. In that Case very often the Action of the Particles of the Liquid, upon one another, is changed, and a Fermentation arises.

CHAP. XVI.

The Description of Several Machines, and the Explanation of their Effects.

[Experiment 1. Plate XXXII. Fig. 1.]

ET one End a, of the Curve Tube a S b, 467

be immerged in Water, whilst the other End

be descended below the Surface of the Water. If

by sucking, or any other Way, the Air be taken

out of this Tube, the Water will run through b.

This Instrument is called a Syphon.

- which drives on the Water in the Syphon, by its Pressure upon the Surface of the Water in the Vessel. The Air does also press against the Water that goes out of the Orifice b, and sustains it. These Pressures are equal, and act contrariwise in the upper Part of the Syphon, with a Force equal to the Weight of the Atmosphere, taking away the Weight of the Pillars of Water which are sustained by the Pressure. The Pillar of the Water, in the Leg Sb, is longer than the opposite Pillar of Water; therefore, the Pressure of the Air is more diminished on the Side bS, and the opposite Pressure overcoming it, the Water slows towards b.
- Experiment 2. Plate XXXI. Fig. 6. The Sy-469 phon above-mentioned has this Inconveniency, that, if once it ceaseth to work, the Water will not run again, unless the Air be drawn out of the Tube afresh. This may be corrected by making a Syphon in the Figure a Sb, whose Legs are equal, and turned up again: For if the Syphon be filled with, and one Leg be immerfed in Water, fo that the Surface of the Water may be above the Orifice, then the Water will run out through the other Leg, for the Reason given in the Explication of the former Experiment. Since the Legs are returned upwards, the Syphon will not be emptied, when the running out of the Water ceases, and so the Syphon, being once filled, is always ready to work its Effect. The Water runs backward or forward thro' it, according as it is higher on one Side or the other.







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Plate XXXII. Fig. 2.] Upon the same Princi-470 ple as the foregoing Machines, is contrived the Syphon for raising Water into a Cistern. The Effect of this Syphon becomes visible by the Help of a Machine made up of two hollow glass Balls H and I, which are joined together by the Tube CDE, the Ball I communicates with the Water to be raised by means of the Tube AB, which comes up almost to the Top of the Ball; to the Ball H at the lower Part is joined the Tube FG, as long as the whole Tube AB.

The Ball H must be filled with Water through a Hole by a Funnel, and then the Hole must be

fhut up close.

In fuch Machines as are applied to Use, for raising Water out of a Reservoir that contains it, the Water is brought away into the Vessel H, and the Communication between the Vessel and the Reservoir is shut up with a Cock.

Experiment 3.] Opening the Cock G, the Water will run out that Way, and the Water will ascend through the Tube AB up into the Vessel I; which being filled, the Water is suffered to run away to the Place where you would have it; and, by repeating the Operation, the Elevation of the Water continues.

Opening the Cock G, the Air presses against the 471 Water going out of the Tube F G; the Air also presses upon the Water in the Reservoir, and sustains that which is in the Tube AB. These Pressures are equal, and if you take from them the Golumns of Water which they sustain, you will have the Forces by which they act upon the Air, contained in the upper Part of the Vessels and the Tube CDE. The Pillar F G, because there is superadded to it the Height of the Water in the Vessel H, does

always

always overcome the Column in the Tube AB, as being longer; therefore, the Pressure at G is less diminished than the other, and so overcome by it, and, therefore, the Water must rise in the

Tube AB, and descend down FG.

To render the Effect of common Pumps visible, let there be a little Pump made of Glass in the following Manner; AB (Plate XXXII. Fig. 3.) must be a Cylinder of Glass, and about an Inch and a half Diameter. In the Bottom of it join a Tube of any Length, as C D. Let the upper Part of it be shut with a leaden Ball, so that the Water may not be able to descend out of the Cylinder, but may easily rise into it, by raising up the Ball, which we make use of here instead of a Valve. The Piston is moved in the Cylinder AB, which, being furrounded with Leather, exactly fills its Cavity: There is a Hole in the Piston, which likewife is stopped with a Ball of Lead instead of a Valve; fo that the Water may rife, but not defcend through the Piston.

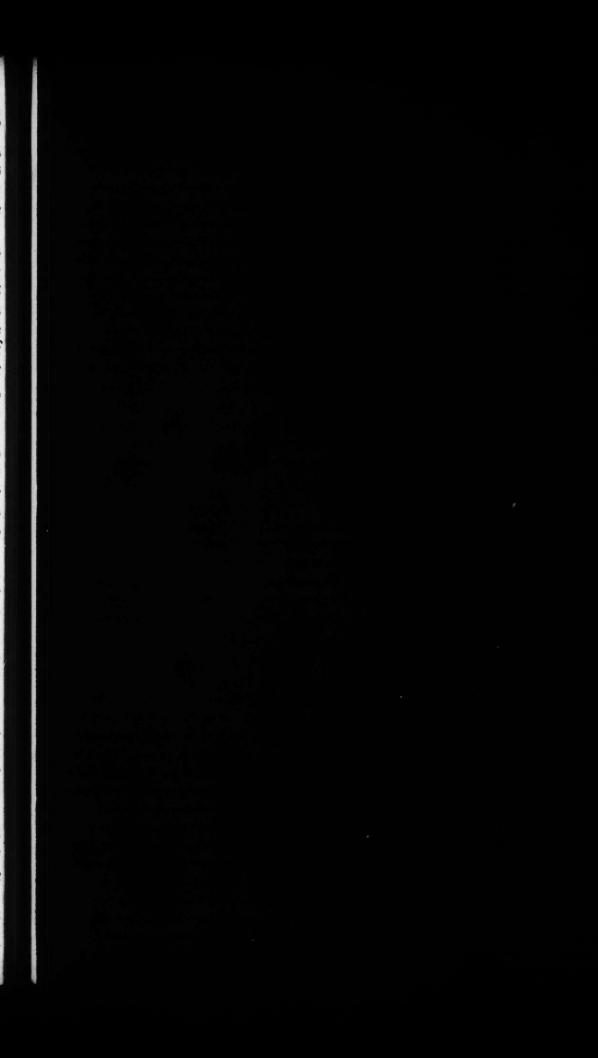
Experiment 4.] Push down the Piston to the Bottom, pour Water upon it to hinder the Passage of the Air; if the End of the Tube CD be immersed into Water, and the Piston be raised, the Water will ascend up into the Cylinder AB

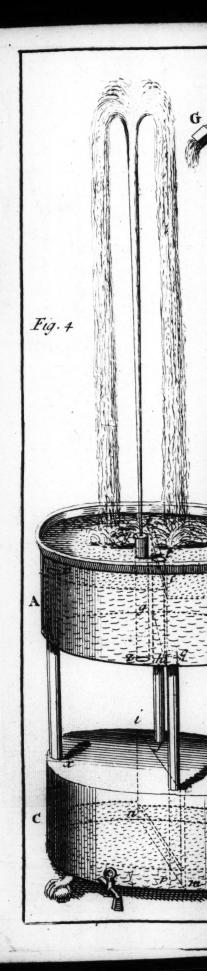
* 447 * from which it cannot descend; wherefore, it comes up through the Piston, when it is pushed down. If you raise the Piston again, the Cylinder is again filled with other Water, and the first Water is raised up into the wooden Cylinder which is joined into the glass one, from which it runs out through the Tube G.

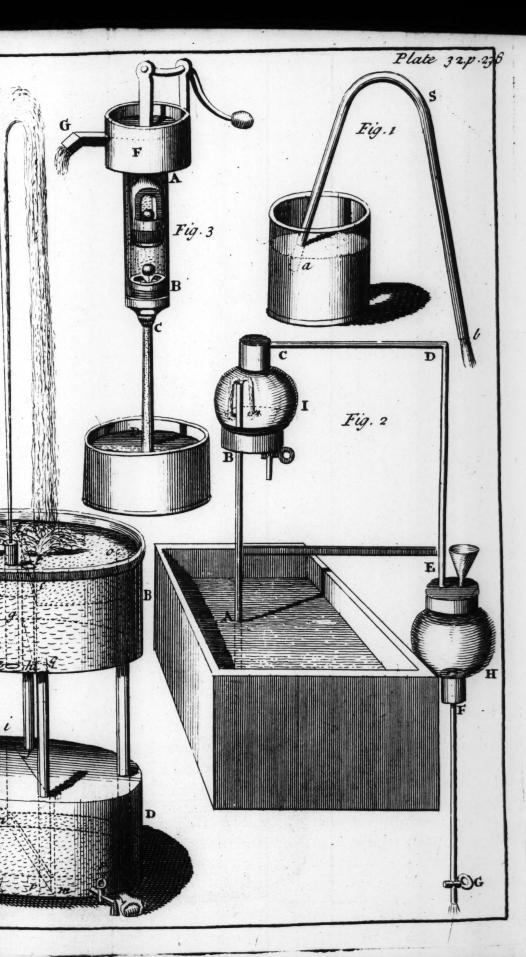
Atmosphere, the Water will not rise in these Ma-

* 423 chines much higer than 32 Foot.

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up w chief clean rufty There are feveral little artificial Fountains, that are called the Fountains of *Hero*; I shall here give the Construction of one of them.

Plate XXXII. Fig. 4.] Let there be two equal 474 elliptical Vessels AB and CD, exactly shut on all Sides, made of one Sort of Metal.

In each of them, there is a Separation passing through the Center of the Ellipse, which divides

the whole Vessel into two equal Parts.

The Separation mni, in the Vessel DC, is perpendicular to the Axis of the Ellipse, the Separation cfgh of the other Vessel must be inclined to that Axis.

There is a Brim raifed round about the upper

Part of the Vessel ACB, to make a Bason.

Four Tubes are joined to these Vessels: The first op goes through the Cavity B of the Vessel AB, without having any Communication with it, and descends almost to the Bottom of the Cavity D; the second st is soldered to the upper Part of the Cavity D, and ascends to the upper Part of the Cavity B, but not quite so high as to touch the upper Plate of it. The third qr reaches from the lower Part of the Cavity B, almost to the Bottom of the Cavity C; the 4th, xu, is made fast to the upper Part of the Cavity C, and reaches almost to the upper Part of the Cavity A.

Lastly, there is a Tube zy, which, going thro' the upper Plate, is soldered to it, and reaches down so deep in the Cavity A, that its End z

is but a little Way off of the Bottom.

There are Cocks joined to every one of the Cavities; or else they have other Holes that are shut up with Screws that have Leathers on them; the chief Use of them is to let out the Water very clean from the Cavities, lest they should grow rusty, when the Machine in not in Use.

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Experiment 5.] Pour in Water through the Tube op, so as to fill the Cavity D; if you continue to pour in Water, it will rise up through the Tube st, and then descend through qr into the Cavity C, which is also filled, the Air ascending up through xu, and going out through xy.

Turn the Machine upfide down, opening the Cocks of the Cavity C and D, the Water will defeend into the Cavities B and A. Having again that the Cocks, as also the Hole y of the Tube zy, set the Machine again the right Side upwards, and pour in Water again through the Tube op, till the upper Surface of the Machine be covered with Water. Now, if the Hole y be opened, the Water will spout up to almost twice the Height of the Machine, and the Motion of the Water will continue, till the Cavity A be emptied of its Water. The Height of the spouting Water will continually diminish, and at last it will not be double the Distance of the Vessels.

475

The Effect of this Machine is to be attributed to the Compression of the Air in the Vessels. The Pressure of the Atmosphere at o and y, as also in the Vessels, is equal, and these Pressures destroy one another, therefore, they are not to be considered in the Examination of the Machine. When at last the Water is poured into the Tube ap, it is fustained in it by the Pressure of the Air contained in the Cavity D, and acting upon the Surface of the Water which stands at a small Height in that Cavity; which Air, therefore, is compressed by the Weight of the Water, whose Height is po. We speak of the Pressure, by which the Pressure of the Atmosphere is overcome. The Air in the upper Part of the Cavity B communicates with the Air above-mentioned by the Tube st, and is equally compressed, and acts with the same Force upon

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upon the Surface of the Water in that Cavity. This Pressure is to be added to the Pressure arising from the Height of the Water, in order to have the Force by which the Air is compressed in the Cavity C, as also in the upper Part of the Cavity A, by reason of the Communication through the Tube xu. The Pressure, therefore, upon the Surface of the Water in that Cavity A, is equal to a Pillar of Water, whose Height is almost double the Weight of the whole Machine. And, therefore, it spouts as if it was pressed by such a whole Column; that is, to a Height not much wanting from the Height of that whole Column. *

The Height is continually diminished, for the Columns of Water, which compress the Air, continually become shorter, because the Water ascends in the Cavities C and D, and its Height is diminished in the Cavity B. In the same Time the Cavity A is continually evacuated, and the Water ascends through a greater Space, before it comes to y; therefore, it is driven to a less Height

above y.

CHAP. XVII.

Of the undulatory Motion of the Air, where we shall treat of Sound.

I f the Air be agitated in any Manner, the Par-476 ticles moved recede from their Place, and drive the neighbouring Particles into a less Space; and as the Air is dilated in one Place, it is compressed in the Place next to it; the compressed Air, by the Restitution of the Spring, not only returns to its first State, but is also dilated by the Motion acquired by the Particles.

The Air, being first dilated by that Motion, is restored to its first State, and the Air is compres-

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fed towards other Parts. This again obtains, when the Air last compressed expands itself, by which a Compression of Air is again produced; therefore, from any Agitation there arises a Motion analogous to the Motion of a Wave on the Surface of

*402 Water. * The Air is compressed in that Manner with a Dilation following, so as to make what is *703 called a Wave of Air: * Compressed Air always dilates itself every Way, and the Motion of these

478 Waves is the Motion of a Sphere expanding itself in the same Manner as the Waves move circularly

*405 upon the Surface of the Water. *

478 Whilst a Wave moves in the Air, where-ever it passes, the Particles are removed from their Place, and return to it, running through a very short Space in going and coming.

Plate XXXIII. Fig. 1.] Now, to explain the Laws of this Motion, let us conceive Particles of Air to be placed at equal Distances, and to be in a Right Line, as a, b, c d, &c. and f. Let the Wave be supposed to move along that Line; now let us suppose it to be come forward along that Line, as far as between b and p; and that the Air is dilated between b and b, but compressed between b and p, as all this is represented in Line 1.

479 The greatest Density is at m, which is the Middle between h and p, and the greatest Dilation, be-

tween b and b, is in the Middle e.

480 Wherever the neighbouring Particles are not equally distant, the Motion, arising from Elasticity, causes the less distant Particles to move towards

*432 those that are most distant; * and this Motion alone, abstracting from all other Motion acquired, is to be examined.

Between b and e there is a Motion from b towards e, that is, conspiring with the Motion of the Waves; there is also such a Motion between m and p.

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But there is a contrary Motion between e and 482

m, and it is directed from m towards e.

At m and e, where the Directions of the Mo-483 tions are changed, no Action arises from the Elasticity, because the neighbouring Parts are placed at equal Distances among themselves.

In the Places b, h, and p, the Difference of the 484 neighbouring Parts is the greatest of all, and therefore, there is the greatest Action of the Elasticity.

From this it follows, that a Particle, according to its different Place in a Wave, fuffers a different Action from the Elasticity by which its Motion is generated, accelerated, diminished or destroyed; therefore, the Direction of the Motion of a Particle cannot be determined from the Action of the above-mentioned Direction only, and does not always agree with that Direction, and the Motion of the single Particles is changed every Moment.

All the Particles between b and p are removed according to the Order of the Letters. The Particles between b and p continue their Motion, and the rest between b and b return towards b, as

will be faid hereafter.

These continue in the Motion by which they return, until, by the Action of the Elasticity, whose Direction is changed in the Point e, the Motion acquired anew be destroyed; in which Case a Particle, as b, returns to rest, and its first State. In the following Moment the Particle c comes to rest in its first State, but p comes forward to q, as in the Line 2, and fuccessively in equal Moments, the Wave has all the Politions which are here represented in the Lines 1, 2, 3, &c. 485 and 13; and, whilft the Wave, from the Position in the Line 1, comes to the Polition in the Line 13, it runs thro' its whole Breadth. The Particle p, in that Motion, goes and returns, and the Mo-R tion

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tion of it is made sensible in the Figure, and, as it plainly appears, this Particle goes successively through all the Situations of the Particles; in the Waves all the Particles singly are agitated by the like Motion.

backward and forward, is analagous to the Motion of a vibrating Pendulum, whilft it performs two Ofcillations, that is, does once go forward and backward. A Pendulum descends in its Oscillation, and the Motion acquired conspires with the Motion of Gravity, and is accelerated by it, until it comes down to the lowest Part of the Arc to be described, that is, the Middle of the Way to be run through; the Pendulum goes on by the Motion acquired, which is destroyed by the Action of Gravity, whose Direction changes in this Point, whilst the Body ascends up the other Part of the Arc to be described: This Body returns by the same Laws.

The Particle p is moved by the Elasticity, and this Motion is accelerated by the Action of the Elasticity, until it comes to the Situation of the

* 481 Particle m, the Line 1, * which Situation is feen in Line 4, in which the Particle p is, in the Middle Point of the Space, to be run through by the Motion backward and forward. By the Motion

* 482 acquired, though Gravity acts against it, *it perseveres in its Motion, until, by the Action of the said Elasticity, the Motion be wholly destroyed, which happens, when it has gone through a Space equal to that in which it was generated; then the Particle is in the Position which is seen in Line 7, which answers to the Situation of the Particle b in Line 1. Then, by the Elasticity, the Particle returns, and is accelerated, until it has acquired the Situation of the Particle e, in

482 Line 1, * as in Line 10, that is, until, as in

Line 4, it comes again to the Point that is in the Middle of the Way to be run through. The Particle continues in its Return, until by the Action of the Elasticity, whose Direction is again changed *, the whole Motion is destroyed; and then *483 the Particle returns to its first Position, as in the Line 13, and there, not being agitated by any new Motion, it remains at rest. Therefore, the 487 Motion of the tremulous Body, by which the Air is agitated, ceasing, there are no new Waves generated, and the Number of the Waves is the same as the Number of the Agitations of that Body.

If, after two Vibrations of a Pendulum, the Action of Gravity should cease, as in the Air, after the going and returning of a Particle, the Action of the Elasticity on that Particle ceases, the Motion of a Particle of Air would wholly agree with the Action of a Pendulum. In the middle Point of the Arc, which is to be run thro' in the Oscillation, there is no Action of Gravity, and its Direction is changed; in the middle Point of the Space to be gone thro' by the Particle p in its going and coming, in which it is in the 4th and 10th Line, the Situation of this Particle agrees with the Situation of the Particles m and e in Line 1, in which Points there is no Action of Elasticity, and its Direction is changed *. In a Pendulum, the more a Body ofcilla- *483 ting is diftant from the lowest Point or Middle of the Arc to be described, by so much greater is the Force of Gravity acting upon it; the more also the Particle p is distant from the Space to be run thro', the more is the Action of the Elasticity upon it; and in the Lines 1, 7, and 13, the Particle is most distant from the Point above-mentioned, and its Situation there agrees with the Points b, b and p in the Line 1, in which the Action of the Elasticity is greatest of all *.

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According to which Law, fince this Action of Elasticity increases with the increased Distance of the often mentioned middle Point, it is determined from the very Law of the Elasticity of the Air, whose Particles drive one another away with a Force which is inversely as the Distance between

432 the Centers of the Particles: and it is demonstrated, that the Action of Elasticity upon such a Particle, as p, is increased or diminished in Proportion to the Distance of the middle Point of the Space to be run thro': And, therefore, also in that Part there is an Analogy between the Motion of a Particle and the Motion of a Pendulum

*156 oscillating in a Cycloid *.

If the Breadth of the Wave remaining, the Particles run out thro' a greater Space, the Compression and Dilatation of the Air in the Wave will be greater, and there will be a greater Action of Elasticity, and that greater in the same Ratio in which the Space gone thro' in the going and coming is increased: And the Motion of a Particle, as p in this Case, differs from the Motion in the foregoing Case, as the unequal Oscillations of different Pendulums differ; which, as they are performed in *156 equal Times*, the same will also obtain here.

Therefore, a Particle, as p, if the Breadth of the Wave continues the same, goes and comes in the same Time, thro' whatever Space it be carried out of its Place; that is, the Wave will go

488 its Breadth in the same Time; therefore, all equal Waves, whether the Air be more or less agitated,

are equally (wift.

Now let us examine unequal Waves; let 'em be as A to B, and let the Space gone thro' by the Particles, in the Motion of each of them in going and coming, be in the same Ratio; in that Case the Compressions and Dilatations in correspondent

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fpondent Places will be equal; the Actions, therefore, from the Elasticity, don't differ in correspondent Distances from the middle Point of the Spaces to be run thro' by the Particles, in their going and coming. Therefore, those Motions are analogous to the Motions of two Pendulums, whose Lengths are as A and B, and which run thro' similar Arcs; for, in the correspondent Points of those Arcs, the Action of Gravity is the same.

In Pendulums the Action of Gravity increases as the increased Quantity of Matter, and whatever be this Quantity, the Motion is equally swift, when the Gravity is not changed; on the contrary, the Action of Elasticity is determined in the Motion of Waves, and depends upon the Distance between the Particles and the Velocity, which is generated from it, the Elasticity remaining the same, is inversly, as the Quantity of Matter to be moved.* In the Waves above-mentioned, * 65 the Quantities of Matter are as the Breadth of 490 the Waves a and b, and the Velocities generated by the Elasticity are, therefore, in correspondent Points as b to a. Therefore, these Motions are analogous to the Motions of Pendulums describing fimilar Arcs, and moved with different Forces of Gravity, which are to one another as B to A; for, in correspondent Points of similar Arcs, the Celerities arising from different Gravities are as those Gravities.

Now to compare the Motion of Waves with the Motion of Pendulums, we must consider Pendulums differing in Length, and on which different Forces of Gravity act*, and we have shewn * 489 what these Causes produce singly in the Duration of the Vibrations.* Both these are to be * 158 joined together, and the Squares of the Times of the Oscillation of Pendulums, whose Motions

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*480 tioned Waves, are as the Length A and B, * and
158 inverfely, as the Gravities B and A: * That is,

again directly, as A and B; the Ratio of which Ratio's is a Ratio, compounded of the Squares of the Quantities A and B. Therefore, the Times of the Oscillations are as A and B, and the Times are in the same Ratio in which the Particles of the Waves go and come; that is, the Waves run through their Breadths, which are as A to B; which Times are, therefore, as the Spaces gone thro' by the Waves, and, therefore, the Motions are equally swift. If the Space be changed thro' which the Particles go and come, the Velocity

*488 of the Waves is not changed; * wherefore, the Proportion which we have put down for a Demonstration, between the Spaces gone thro' by the Particles in their going and coming, may be neglected, and the Proposition will be generally

491 true, that Waves, whether equal or any Way unequal, move with the same Velocity.

the Air is not changed; but the Elasticity remaining the same, the Density of the Air often varies; and the Elasticity may be changed, the Density remaining the same; lastly, both are often liable to be changed.

In the first Case, supposing both the Waves to be equal, and also the Spaces thro' which the Particles go and come, the Celerities arising from the Elasticity, which is always the same, are invested as the Densities *; but this Variation of

450 lums, with the Variation of the Gravity, in which Cases the Squares of the Celerities of the

therefore, in Wavesthe Squares of their Celerities are inversely

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inversely as the Densities. The Supposition of the Equality of the Waves, and the Spaces gone thro' by the Particles, does not hinder this Demonstration from being univerfal.*

* 488 When the Density remains the same, but the Elasticity is changed, the Celerity arising from it va-493 ries in the same Ratio as the Elasticity; wherefore, from the Demonstration of the foregoing Proposition in this Case, the Squares of the Celerities of the Waves are as the Degrees of the Elasticity.

If the Elasticity and the Density differ, the Squares 494 of the Velocities of the Waves will be in a Ratio compounded of the direct Ratio of the Elasticity*, and the inverse Ratio of the Density.* 492

If the Density and the Elasticity increase or de-495 crease in the same Ratio, the inverse Ratio of the Density will destroy the direct Ratio of the Elasticity, and the Celerity of the Waves will not be

changed.

This last Case happens in the Compression of 496 the Air.* Therefore, from the changed Height of * 430 the Pillar of Mercury, which is sustained in a Tube void of Air by the Pressure of the Atmosphere*, * which shews, that the Weight, by which the Air is compress'd near the Earth, is changed, we must 497 not judge the Celerity of the Waves to be changed. For the same Reason, the Waves are moved with the same Celerity in the Top of a Mountain as in a Valley; unless there be a Change of the Elasticity itself, by reason of the Cold, which is almost always more intense on the Top of a Mountain than in a Valley; and this would occasion the Waves to move flower.* 493

It is plain also, that the Waves move faster in 498 Summer than in Winter.*

The Celerity of the Waves is compared to 499 the Celerity which a Body acquires in falling, by determining, from the known Height of the Mer-

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Mercury, which weighs equally with the Pref-

* 442 of the Air *; the Height of the Atmosphere, supposing it every where equally dense with the Air near the Earth; the Velocity of the Waves will be the same as a Body could acquire in falling from balf that Height. Which Velocity, from what has been said, may be easily discovered by Expe-

157 riments made upon Pendulums.*

If the Weight, by which the Air is compress'd, be diminish'd, the Air expands itself in the same

* 42 Ratio *; and supposing the Atmosphere every where of the same Density, its Height does not vary, which agrees with what has been said, that the Velocity of the Waves is the same in different

* 496 Compressions of the Atmosphere.*

The Motion of the Air, which we consider in this Computation, arises from Elasticity alone, and the Computation would be exact, if the Particles themselves had not a sensible Proportion to the Interstices between them; but if we suppose here that they bear a sensible Proportion to them, the Motion of the Waves will be swifter; for it is propagated through solid Bodies in an Instant, which must also be referred to heterogeneous Corpuscules swimming in the Air.

of which, before we speak, we must lay down fomething in general relating to Sensation.

So strict is the Union of the Body and the Mind, that some Motions in the Body do, as it were, cohere with certain Ideas in the Mind, and they cannot be separated from each other. From the Motion of the Body are new Ideas every Moment excited in the Mind, and such are the Ideas of all sensible Objects; yet we find nothing common between the Motion in the Body and the Idea.

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Idea in the Mind. We cannot perceive what Connection is here, nor that any Connection is possible. There are an infinite Number of Things hidden from us, of which we have not so much as an Idea.

The undulatory Motion of the Air agitates 503 the Tympanum, or Drum of the Ear, by which Means a Motion is communicated to the Air contained in that Organ, which, being carried to the auditory Nerve, excites in the Mind the Idea of Sound.

The Structure of the Ear, both internal and external, is wonderful; but here we treat of the Motion of the Air; that it is the Vehicle of Sound, is proved by the following Experiment.

Experiment 1. Plate XXXIII. Fig. 2. Take the leaden Plate O, which has two cylindric Pillars of the same Metal C, C, fixed to it; join a little Bell A to the brass Wire BD, and let it be tied with Strings to the Pillars C, C; lay the Plate O upon the brass Plate of the Air-Pump, putting between a little Cushion of Cotton, or Raw-Silk; fet a Receiver on over all this Apparatus. Cover the Receiver with a Plate that has the Collar of Leathers screwed to it, through which the brass Wire DE can slip up and down*; to the * 440 brass Wire you must fasten the Plate e f, so that, by turning the Wire round, the Bell A may be agitated. Pump out the Air from the Receiver, and shaking the Bell in the Manner before described, you will not hear the Sound. By turning the Wire DE, the Bell will move backward and forward feveral times; but we are only to observe that Motion in which the Plate e f doth not touch the Wire bd. Letting in the Air, the Sound will be heard as before.

From

Sound, and that Sound is moved thro' it without the Air's being carried from one Place to another, it evidently follows, that in Sound there is an undulatory Motion of the Air, and that Sound arises from the tremulous Motion of Bodies. That this obtains in Cords, or Strings of musical Instruments, no Body doubts, since by giving them a tremulous Agitation they produce a Sound. In great Bells, and several other Bodies, this tremulous Motion is very sensible; but it will become visible by the following Experiment made upon a founding Glass Bell.

Experiment 2.] Let the Glass Bell C C be fix'd with Plaster, or Cement, to a wooden Screw, by Means of which it may be made very fast to the transverse Piece of Wood AB; this Wood must be sustain'd by two wooden Pillars S S, to which it is firmly join'd with Screws and Nuts. There is a Pin, with a Screw upon it, that goes through one of the Pillars, just even with the Mouth of the Bell; so, by screwing it forwards or backwards, you may set it nearer to, or farther from, the Edge of the Bell. If this Distance be very small, and the Bell be struck, it will, by its tremulous Motion, strike several Times against the Pin with its Edge.

506 Hence we deduce, that a Body, that is struck, continues to give a Sound some Time after the Blow; the agitated Fibre will continue his Vibra-

* 215 tion some Time, on Account of the Elasticity *; we often see, as in Experiment 1. that a Body gives a Sound, tho' the Air, agitated by it, has no Communication with the outward Air; whence it 507 follows, that, by the Agitation of the Air, the Fibres

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of which Bodies consist are mov'd; which Motion is transferr'd into the external Air.

This Translation of the Sound, by the tremulous Motion of the Fibres, is very remarkable; and how the Communication of this Motion extends itself, will appear by a single Experiment.

Experiment 3. Plate XXXIII. Fig. 2.] This Experiment differs from the first only in this; that if, instead of tying the Bell to the leaden Machine COC, it be fastened to the Ends of a brass Plate bent in the Figure of a double Gnomon, which is made fast by a Screw to the Plate of the Air-Pump, and the Air be pumped out, and the Bell shak'd in the same Manner as in the first Experiment; you will find but very little Difference between the Sound that is made, when the Air is exhausted, and when the Air is re-admitted.

The tremulous Motion of the Parts of the Bell is communicated to the brass Wire bd, so as to move the Strings by which the Bell is suspended, and this Motion is transferred to the bent brass Plate; the Screw, with which this Plate is joined to the brass Plate of the Air-Pump, touches the Plate, and communicates a tremulous Motion to it, by which the Air is agitated, and the Sound of the Bell is heard.

The Celerity of the Sound is the same as the Cele- 508 rity of the Waves, which firike the Ear; and to this must be referred what has been faid of their *491 Celerity. * In respect to Numb. 499, it is to be 492, 493. observed, that the Celerity of Sound can no Way 494, be determined by Calculation; for the Propor-495. tion, between the Diameters of the Particles and 496, 497, in the Interstices between them, is not known, 498, 499, neither how large a Space the heterogeneous Particles take up in the Air.

The Celerity of Sound may be immediately

determin'd by an Experiment.

Noise, and a Spectator stands at any known Distance from the Fire, who, with a short Pendulum, measures the Time between seeing the Light, and hearing the Sound, he will have the Celerity of the Sound; for the Motion of Light, at least, thro' the Space as such an Experiment can be made in, is instantaneous.

pear'd, that Sound run 1800 French Feet in a fecond Minute of Time; but this Celerity is not

* 498 constant.*

511 If at the same Time in which the Velocity of the Sound is determin'd by this Method, there

* 422 be made the two Experiments above-named *, 499 one may, by Calculation, determine the Motion

description of Sound by the Elasticity of the Air*, and by comparing it with the Velocity immediately mention'd, you will have the Acceleration of the Sound, from the Thickness of the Particles, and 512 the heterogeneous Matter.

491 The Celerity of the Sound is equable *, yet in going through a greater Space, it is sometimes ac-

* 493 celerated or retarded *, from the different Degree of Elasticity in different Places, in which there

* 434 are different Degrees of Heat or Cold.*

The Celerity of the Sound does not much differ, whether it goes with the Wind, or against the Wind. By the Wind a certain Quantity of Air is carried from one Place to another; the Sound is accelerated as long as it moves through that Part of the Air, if the Direction of the Sound be the same with the Direction of the Wind; but as Sound moves very swift, in a very short Time it

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will run through the Air which is agitated by the Wind, and the Acceleration does not last long, which, indeed, is not very great; for the most violent Winds, which are strong enough to root up Trees, and blow down Houses, have their Celerity to the Celerity of the Sound, but about as one to 33; by the same Argument it is prov'd, that no sensible Retardation is occasioned by the Wind, when the Sound moves against it.

The Space which the Particles run through, as they come and go, may be increas'd and diminished by the Wind, therefore, the Sound may be heard at a greater or smaller Distance, according to the Direction of the Wind.

The Intensity of the Sound depends upon the Strokes of the Air on the auditory Nerve, and these Strokes are as the Quantities of Motion

in the Air.

Whence it follows, that, cæteris paribus, the 515 Intensity of the Sound is as the Space run through by the Particles in their going and coming *.

All Things remaining as before, if the Weight 53, by which the Air is compressed be changed, the 63. Celerity does not vary *, but the Density is chan- *496, ged in the same Ratio as the Weight *.

Therefore, cateris paribus, the Intensity of the 516 Sound is as the Weight by which the Air is compres'd*, that is, this Intensity increases and de-*62 creases, as the Pillar of Mercury, which is in A-quilibrio, with the Weight of the Atmosphere.

Experiment 4. Plate XXXIII. Fig. 3.] Shake the Bell A in compressed Air * exactly in the *454. Manner as it was shak'd in Vacuo, in Experim. 1. and the Sound will be increased; which will again be diminished, if opening the Bell you let the Air return to its first State.

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As the Intensity of the Sound in compress'd Air, included in a Vessel, is greater, so the Fibres, of which the Glass VV is made, are agitated, and a greater Agitation is communicated to the external Air.

If all Things remain as before, but the Elasticity be increas'd, the Density is diminished in the same *430 Ratio as the Elasticity is increas'd*, but the Celerity increases as the Square Root of the Elasticity increases as the Square Root of the Elasticity increases as the Square Root of the Elasticity increases as the Square Root of the Elasticity

*493 sticity *; therefore, the Intensity of the Sound is directly as the Square Root of the Elasticity, and in-

versely as the Elasticity itself *; but the Ratio, compounded of these, is the inverse Ratio of the above-mention'd Square Root of the Elasticity.

The Intensity of the Sound is diminished, therefore, as its Velocity is increas'd; and in Summer,
cæteris paribus, the Intensity of Sound is less than
in Winter; yet, in Summer, Bodies do more easily
transmit Sound: Because their Parts cohere less
strictly, as will be explain'd at a proper Time, and
they do more easily acquire a tremulous Motion.

Experiment 5. Plate XXXIII. Fig. 5.] Hang up the Bell A in a Glass, and opening the Cock, that the Air in the Glass may have Communication with the external Air, let the Glass be shaked, and the Distance be determined when the Sound can be heard; warm the Glass and repeat the Experiment, and the Sound will be heard at a greater Distance.

The Intensity of Sound, consider'd in general, is in a compound Ratio of the Space run thro' by the Par-

515 ticles, in their going backward and forward, of *116 the Weight compressing the Air*; and lastly, of the *517 inverse Ratio of the Square Root of the Elasticity.*

There is also a Difference in Sound, from the Number of the Vibrations of the Fibres of the Body

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Body which produce the Sound, that is, of the Number of the Waves produced in a certain Time, according to the different Number of the Percussions in the Ear, the Mind receiving a different Sensation.

A Musical Tone depends upon this Number of 522 Vibrations, which is said to be the more acute, according as the Returns in the Air are more frequent; and more grave, the less the Number of the Waves is; and the Degrees of the Sharpness of the different Sounds are to one another, as the Number of the Waves which are produced in the Air at the same Time.

A Tone does not depend upon the Intensity of the 524 Sound, and an agitated Cord gives the same Sound, whether it vibrates through a greater or a less

Space.*

Concords arise from the Agreement between the 525 different Motions of the Air, which affect the Au-

ditory Nerves at the same Time.

If two tremulous Bodies perform their Vibra-526 tions in the fame Time, there will be no Difference between their Tones, and this Agreement, which is the most perfect of all, is call'd *Unison*.

If the Vibrations are as 1 to 2, this Confonance, 527

or Agreement, is call'd Octave, or Diapason.

Supposing the Vibrations as 2 to 3, that is, if 528 the second Vibration of one Body always agrees with the third of another, such a Consonance is call'd a Fifth, or Diapente.

Vibrations, which are as 3 to 4, give a Confo-529

nance which is call'd a Fourth, or Diatesfaron.

Ditonus is, when the Returns of the Air are 530

as 4 to 5.

And Sesquiditonus is a Consonance, from a Con-531 course of the fifth Vibration of one Body with the sixth of another.

A Confonance from the Agitation of Cords, if they be of the same Kind, is easily determin'd by knowing their Dimensions and Tension.

332 Cæteris paribus, if the Lengths of two Cords are as the Number of Returns in a Consonance, you will have the Consonance between the Sounds

* 259 which the Strings produce.*

533 The same obtains, if, cæteris paribus, the Dia-

* 260 meters have the aforesaid Proportion.*

534 And also, if, cæteris paribus, the Proportion of the Vibration in a Consonance be given between the

* 258 Square Roots of the Tensions.*

Kind, if the Ratio be compounded of the fame Kind, if the Ratio be compounded of the direct Ratio of the Lengths and of the Diameters, and the inverse Ratio of the Square Roots of the Tenfions, be the Ratio between the Numbers of Vibrations perform'd in the same Time in any Consonance whatever, you will have that Consonance by * 261 the Agitation of those Cords. *

All these have been experimentally try'd by Musicians; they have observ'd a very remarkable Phænomenon relating to these Cords, whose different Cases very well deserve to be explained.

form their Vibration in equal Times; if you give Motion to the one, the other will also move. Every Wave of the Air, arising from the tremulous Motion of the first String, strikes the second String, and gives it a little Motion; the String, from the least Motion, goes backward and forward several

* 257 Times *, and is mov'd by the Stroke of the first Wave, whilst the second Wave comes forward, whose Motion conspires with the Motion of the

* 257 String *, and accelerates it. What is faid of the fecond Wave must also be referr'd to the other Waves that follow, and there will be an Accea:

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and fore Acceleration, 'till the Motion of both Strings be almost equal.

From the same Demonstration it follows, that 537 an agitated String will communicate Motion to another, which performs two or three Vibrations,

whilst the first performs but one.

Now, if the agitated String performs feveral Vibrations, whilft the String that is to be mov'd by the Air can perform but one, from the foregoing Demonstration it would follow, that it must communicate a particular Motion to it. To difcover which, it is to be observed, that the Duration of the Vibration and the Length of the String are reciprocal; fo that, every Thing else continuing as before, the determin'd Length can no Way be separated from the unchang'd Duration of the Vibration. If, therefore, any String be struck with several Strokes, by which, Motion is communicated to it, and the Strokes are more frequent than what is agreeable to the Length of the String, that Part of it, whose Length agrees with the Time of the communicated Vibration, will be agitated as much, and there will be, as it were, an undulatory Motion communicated to the String; the Length of the Waves in the String will depend upon the Duration of the communicated Vibration, that is, upon the Time between the Strokes.

Take two Strings, in such Proportion that one 538 may vibrate twice, whilft the other vibrates but once, and let the first String be put in Motion; the Duration of the Vibrations, which are communicated to the last String with the Motion of the Air, agrees with a String of half its Length*, and such is the Length of the Waves in it: Therefore, by the communicative Motion, the String is divided into two equal Parts, and the Middle Point

Point is at rest. This is confirm'd by an Experiment, if you lay a Piece of Paper upon the String to which the Motion is communicated; for it will remain at rest, if you lay it upon the Middle of the String, but any other Part of it will be affected with a tremulous Motion.

der to cause Motion in another, performs three Visbrations, whilst the String, to be mov'd, performs but one, the last will be divided into three Parts by the communicated Motion, and there will be two Points of Rest, which may be confirm'd by the same Experiment above-mention'd. All other Cases that have communicated Motion, which are observ'd by Musicians, are easily deduced from what has been said.

* 406 flexion of the Waves in Water *, may be referr'd
408 to their Reflexion in Air, the Elasticity in this
409 Cause producing the same Effect as the Pressure

of the rais'd Water in that.

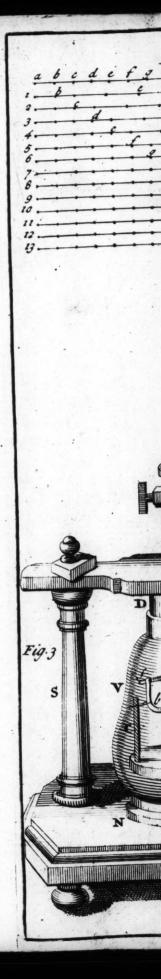
541 From the Reflexion of the Sound there often arises a Repetition of it, which is call'd an Eccho. If different Parts of the same Wave, expanding

* 477 itself into a Sphere *, strike upon different Surfaces, so that being reflected they concur together, the Motion of the Air will be stronger there, and the Sound will be heard. The same Sound is often repeated different Times from the different Parts of the same Way reflected to different Distances, and some of which also successively concur at the

542 same Place. Such a Repetition sometimes happens from the Reslexion being repeated.

The Sound is often increas'd by Reflexion in a Tute: The most perfect Figure of all that can be given to such a Tube is that of a Parabola, revolving about a Line a Quarter of an Inch distant from

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Boo the fetti and be f acqu chir of The the Axis. For if any one speaks in such a Tube, setting his Mouth in the Axis of the Machine, and in the Focus of the Parabola, the Waves will be so reslected, that every one of their Parts will acquire a Motion parallel to the Axis of the Machine, whereby the Force of the Wave, and also of the Sound, will be very much increased. There must be a Mouth-Piece to sit the Lips fixed to the End of the Tube.

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FINIS.



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